



MOSEK Optimization Toolbox for  
MATLAB  
*Release 9.3.21*

MOSEK ApS

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# Chapter 1

## Introduction

The **MOSEK** Optimization Suite 9.3.21 is a powerful software package capable of solving large-scale optimization problems of the following kind:

- linear,
- conic:
  - conic quadratic (also known as second-order cone),
  - involving the exponential cone,
  - involving the power cone,
  - semidefinite,
- convex quadratic and quadratically constrained,
- integer.

In order to obtain an overview of features in the **MOSEK** Optimization Suite consult the [product introduction](#) guide.

The most widespread class of optimization problems is *linear optimization problems*, where all relations are linear. The tremendous success of both applications and theory of linear optimization can be ascribed to the following factors:

- The required data are simple, i.e. just matrices and vectors.
- Convexity is guaranteed since the problem is convex by construction.
- Linear functions are trivially differentiable.
- There exist very efficient algorithms and software for solving linear problems.
- Duality properties for linear optimization are nice and simple.

Even if the linear optimization model is only an approximation to the true problem at hand, the advantages of linear optimization may outweigh the disadvantages. In some cases, however, the problem formulation is inherently nonlinear and a linear approximation is either intractable or inadequate. *Conic optimization* has proved to be a very expressive and powerful way to introduce nonlinearities, while preserving all the nice properties of linear optimization listed above.

The fundamental expression in linear optimization is a linear expression of the form

$$Ax - b \geq 0.$$

In conic optimization this is replaced with a wider class of constraints

$$Ax - b \in \mathcal{K}$$

where  $\mathcal{K}$  is a *convex cone*. For example in 3 dimensions  $\mathcal{K}$  may correspond to an ice cream cone. The conic optimizer in **MOSEK** supports a number of different types of cones  $\mathcal{K}$ , which allows a surprisingly large number of nonlinear relations to be modeled, as described in the **MOSEK** [Modeling Cookbook](#), while preserving the nice algorithmic and theoretical properties of linear optimization.

## 1.1 Why the Optimization Toolbox for MATLAB?

The Optimization Toolbox for MATLAB provides access to most of the functionality of **MOSEK** from a MATLAB environment. In addition the toolbox includes functions that replace functions from the MATLAB optimization toolbox available from MathWorks.

The Optimization Toolbox for MATLAB provides access to:

- Linear Optimization (LO)
- Conic Quadratic (Second-Order Cone) Optimization (CQO, SOCO)
- Power Cone Optimization
- Conic Exponential Optimization (CEO)
- Convex Quadratic and Quadratically Constrained Optimization (QO, QCQO)
- Semidefinite Optimization (SDO)
- Mixed-Integer Optimization (MIO)

as well as to additional functions for:

- problem analysis,
- sensitivity analysis,
- infeasibility diagnostics.

## Chapter 2

# Contact Information

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Website	<a href="http://mosek.com">mosek.com</a>	
Email		
	<a href="mailto:sales@mosek.com">sales@mosek.com</a>	Sales, pricing, and licensing
	<a href="mailto:support@mosek.com">support@mosek.com</a>	Technical support, questions and bug reports
	<a href="mailto:info@mosek.com">info@mosek.com</a>	Everything else.
Mailing Address		
	MOSEK ApS	
	Fruebjergvej 3	
	Symbion Science Park, Box 16	
	2100 Copenhagen O	
	Denmark	

You can get in touch with **MOSEK** using popular social media as well:

<b>Blogger</b>	<a href="https://blog.mosek.com/">https://blog.mosek.com/</a>
<b>Google Group</b>	<a href="https://groups.google.com/forum/#!forum/mosek">https://groups.google.com/forum/#!forum/mosek</a>
<b>Twitter</b>	<a href="https://twitter.com/mosektw">https://twitter.com/mosektw</a>
<b>Linkedin</b>	<a href="https://www.linkedin.com/company/mosek-aps">https://www.linkedin.com/company/mosek-aps</a>
<b>Youtube</b>	<a href="https://www.youtube.com/channel/UCvIyectEVLp31NXeD5mIbEw">https://www.youtube.com/channel/UCvIyectEVLp31NXeD5mIbEw</a>

In particular **Twitter** is used for news, updates and release announcements.

## Chapter 3

# License Agreement

Before using the **MOSEK** software, please read the license agreement available in the distribution at <MSKHOME>/mosek/9.3/mosek-eula.pdf or on the **MOSEK** website <https://mosek.com/products/license-agreement>.

**MOSEK** uses some third-party open-source libraries. Their license details follows.

### ***zlib***

**MOSEK** includes the *zlib* library obtained from the [zlib website](#). The license agreement for *zlib* is shown in [Listing 3.1](#).

Listing 3.1: *zlib* license.

```
zlib.h -- interface of the 'zlib' general purpose compression library
version 1.2.7, May 2nd, 2012

Copyright (C) 1995-2012 Jean-loup Gailly and Mark Adler

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Jean-loup Gailly          Mark Adler
jloup@gzip.org            madler@alumni.caltech.edu
```

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**MOSEK** includes the floating point formatting library developed by David M. Gay obtained from the [netlib website](#). The license agreement for *fplib* is shown in [Listing 3.2](#).

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```
/*
 *
 * The author of this software is David M. Gay.
 *
 * Copyright (c) 1991, 2000, 2001 by Lucent Technologies.
 *
 * Permission to use, copy, modify, and distribute this software for any
 * purpose without fee is hereby granted, provided that this entire notice
 * is included in all copies of any software which is or includes a copy
 * or modification of this software and in all copies of the supporting
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 *
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 *
 *****/
```

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For Zstandard software

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```

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### Security exception in MacOS 10.15+ (Catalina)

If an attempt to run **MOSEK** on Mac OS 10.15 (Catalina) and later produces security exceptions (developer cannot be verified and similar) then use `xattr` to remove the quarantine attribute from all **MOSEK** executables and binaries. This can be done in one go with

```
xattr -dr com.apple.quarantine mosek
```

where `mosek` is the folder which contains the full **MOSEK** installation or **MOSEK** binaries. See <https://themosekblog.blogspot.com/2019/12/macos-1015-catalina-mosek-installation.html> for more information. If that does not help, use the system settings to allow running arbitrary unverified applications.

# Chapter 5

## Design Overview

### 5.1 Modeling

Optimization Toolbox for MATLAB is an interface for specifying optimization problems directly in matrix form. It means that an optimization problem such as:

$$\begin{array}{ll}\text{minimize} & c^T x \\ \text{subject to} & Ax \leq b, \\ & x \in \mathcal{K}\end{array}$$

or

$$\begin{array}{ll}\text{minimize} & c^T x \\ \text{subject to} & Ax \leq b, \\ & Fx + g \in \mathcal{K}\end{array}$$

is specified by describing the matrices  $A$ ,  $F$ , vectors  $b, c, g$  and a list of cones  $\mathcal{K}$  directly.

The main characteristics of this interface are:

- **Simplicity:** once the problem data is assembled in matrix form, it is straightforward to input it into the optimizer.
- **Exploiting sparsity:** data is entered in sparse format, enabling huge, sparse problems to be defined and solved efficiently.
- **Efficiency:** the API incurs almost no overhead between the user's representation of the problem and **MOSEK**'s internal one.

Optimization Toolbox for MATLAB does not aid with modeling. It is the user's responsibility to express the problem in **MOSEK**'s standard form, introducing, if necessary, auxiliary variables and constraints. See [Sec. 12](#) for the precise formulations of problems **MOSEK** solves.

### 5.2 “Hello World!” in MOSEK

Here we present the most basic workflow pattern when using Optimization Toolbox for MATLAB.

#### Create a prob structure

Optimization problems using Optimization Toolbox for MATLAB are specified using a *prob* structure that describes the numerical data of the problem. In most cases it consists of matrices of floating-point numbers.

## Retrieving the solutions

When the problem is set up, the optimizer is invoked with the call to `mosekopt`. The call will return a response and a structure containing the solution to all variables. See further details in [Sec. 7](#).

We refer also to [Sec. 7](#) for information about more advanced mechanisms of interacting with the solver.

## Source code example

Below is the most basic code sample that defines and solves a trivial optimization problem

$$\begin{array}{ll}\text{minimize} & x \\ \text{subject to} & 2.0 \leq x \leq 3.0.\end{array}$$

For simplicity the example does not contain any error or status checks.

Listing 5.1: “Hello World!” in MOSEK

```
prob.a = sparse(0,1) % 0 linear constraints, 1 variable
prob.c = [1.0]' % Only objective coefficient
prob.blx= [2.0]' % Lower bound(s) on variable(s)
prob.bux= [3.0]' % Upper bound(s) on variable(s)

% Optimize
[r, res] = mosekopt('minimize', prob);

% Print answer
res.sol.itr.xx
```

## Chapter 6

# Optimization Tutorials

In this section we demonstrate how to set up basic types of optimization problems. Each short tutorial contains a working example of formulating problems, defining variables and constraints and retrieving solutions.

### 6.1 Linear Optimization

The simplest optimization problem is a purely linear problem. A *linear optimization problem* is a problem of the following form:

Minimize or maximize the objective function

$$\sum_{j=0}^{n-1} c_j x_j + c^f$$

subject to the linear constraints

$$l_k^c \leq \sum_{j=0}^{n-1} a_{kj} x_j \leq u_k^c, \quad k = 0, \dots, m-1,$$

and the bounds

$$l_j^x \leq x_j \leq u_j^x, \quad j = 0, \dots, n-1.$$

The problem description consists of the following elements:

- $m$  and  $n$  — the number of constraints and variables, respectively,
- $x$  — the variable vector of length  $n$ ,
- $c$  — the coefficient vector of length  $n$

$$c = \begin{bmatrix} c_0 \\ \vdots \\ c_{n-1} \end{bmatrix},$$

- $c^f$  — fixed term in the objective,
- $A$  — an  $m \times n$  matrix of coefficients

$$A = \begin{bmatrix} a_{0,0} & \cdots & a_{0,(n-1)} \\ \vdots & \cdots & \vdots \\ a_{(m-1),0} & \cdots & a_{(m-1),(n-1)} \end{bmatrix},$$



### Example: Linear optimization using `mosekopt`

The function `msklpopt` is just a wrapper around the `mosekopt`, which is the main interface to **MOSEK** and is the only choice for more complicated problems, for instance with conic constraints. We demonstrate how to solve (6.1) directly with `mosekopt`. The following MATLAB code demonstrate how to set up the `prob` structure for the example (6.1) and solve the problem using `mosekopt`.

Listing 6.2: Script implementing problem (6.1) using `mosekopt`.

```
function lo2()
clear prob;

% Specify the c vector.
prob.c = [3 1 5 1]';

% Specify a in sparse format.
subi = [1 1 1 2 2 2 2 3 3];
subj = [1 2 3 1 2 3 4 2 4];
valij = [3 1 2 2 1 3 1 2 3];

prob.a = sparse(subi,subj,valij);

% Specify lower bounds of the constraints.
prob.blc = [30 15 -inf]';

% Specify upper bounds of the constraints.
prob.buc = [30 inf 25 ]';

% Specify lower bounds of the variables.
prob.blx = zeros(4,1);

% Specify upper bounds of the variables.
prob.bux = [inf 10 inf inf]';

% Perform the optimization.
[r,res] = mosekopt('maximize',prob);

% Show the optimal x solution.
res.sol.bas.xx
```

Please note that

- A MATLAB structure named `prob` containing all the relevant problem data is defined.
- All fields of this structure are optional except `prob.a` which is required to be a **sparse** matrix. The dimension of this matrix determine the number of constraints and variables in the problem.
- Different parts of the solution can be accessed as described in Sec. 7.1.

### Example: Linear optimization using `linprog`

**MOSEK** also provides a function `linprog` with a function of the same name from the MATLAB Optimization Toolbox. Consult Sec. 10.1 for details.

Listing 6.3: Script implementing problem (6.1) using `linprog`.

```
f = - [3 1 5 1]'; % minus because we maximize
A = [[-2 -1 -3 -1]; [0 2 0 3]];
b = [-15 25]';
Aeq = [3 1 2 0];
```

(continues on next page)





```

% Lower bounds of variables.
prob.blx = sparse(3,1);

% Upper bounds of variables.
prob.bux = []; % There are no bounds.

[r,res] = mosekopt('minimize',prob);

% Display return code.
fprintf('Return code: %d\n',r);

% Display primal solution for the constraints.
res.sol.itr.xc'

% Display primal solution for the variables.
res.sol.itr.xx'

```

This sequence of commands looks much like the one that was used to solve the linear optimization example using *mosekopt* except that the definition of the  $Q$  matrix in `prob.mosekopt` requires that  $Q$  is specified in a sparse format. Indeed the vectors `qosubi`, `qosubj`, and `qoval` are used to specify the coefficients of  $Q$  in the objective using the principle

$$Q_{\text{qosubi}(t),\text{qosubj}(t)} = \text{qoval}(t), \text{ for } t = 1, \dots, \text{length}(\text{qosubi}).$$

An important observation is that due to  $Q$  being symmetric, only the lower triangular part of  $Q$  should be specified.

### Using *mskqpopt*

In Listing 6.5 we show how to use *mskqpopt* to solve problem (6.4).

Listing 6.5: Function solving problem (6.4) using *mskqpopt*.

```

function qo1()

% Set up Q.
q = [[2 0 -1];[0 0.2 0];[-1 0 2]];

% Set up the linear part of the problem.
c = [0 -1 0]';
a = ones(1,3);
blc = [1.0];
buc = [inf];
blx = sparse(3,1);
bux = [];

% Optimize the problem.
[res] = mskqpopt(q,c,a,blc,buc,blx,bux);

% Show the primal solution.
res.sol.itr.xx

```

It should be clear that the format for calling *mskqpopt* is very similar to calling *msklpopt* except that the  $Q$  matrix is included as the first argument of the call. Similarly, the solution can be inspected by viewing the `res.sol` field.



















```

prob.buc = [b k];

% Dimensions of PSD variables
prob.bardim = [3, 4];

% Coefficients in the objective
[r1,c1,v1] = find(tril(C1));
[r2,c2,v2] = find(tril(C2));

prob.barc.subj = [ repmat(1,length(v1),1);           % Which PSD variable (j)
                  repmat(2,length(v2),1) ];
prob.barc.subk = [r1; r2];                          % Which matrix entry and
↳value ((k,l)->v)
prob.barc.subl = [c1; c2];
prob.barc.val = [v1; v2];

% Coefficients in the constraints
[r1,c1,v1] = find(tril(A1));
[r2,c2,v2] = find(tril(A2));

prob.bara.subi = [ones(length(v1)+length(v2),1);    % Which constraint (i)
                  2];
prob.bara.subj = [ repmat(1,length(v1),1);
                  repmat(2,length(v2),1);
                  2];                                % Which PSD variable (j)
prob.bara.subk = [r1; r2; 2];                        % Which matrix entry and
↳value ((k,l)->v)
prob.bara.subl = [c1; c2; 1];
prob.bara.val = [v1; v2; 0.5];

% Solve with log output
[r, res] = mosekopt('write(test.ptf) minimize echo(10)', prob);

% Retrieve the result assuming primal and dual feasible
X1 = zeros(3);
X1([1,2,3,5,6,9]) = res.sol.itr.barx(1:6);
X1 = X1 + tril(X1,-1)';

X2 = zeros(4);
X2([1,2,3,4,6,7,8,11,12,16]) = res.sol.itr.barx(7:16);
X2 = X2 + tril(X2,-1)';

X1
X2

```

The numerical values of  $\bar{X}_j$  are returned in `res.sol.itr.barx`; the lower triangular part of each  $\bar{X}_j$  is stacked column-by-column into an array, and each array is then concatenated forming a single array `res.sol.itr.barx` representing  $\bar{X}_1, \dots, \bar{X}_p$ . Similarly, the dual semidefinite variables  $\bar{S}_j$  are recovered through `res.sol.itr.bars`.



```

% The power cone for (x_1+x_2+0.1, 1, t_2) \in POW3^(1/4,3/4)
FP2 = sparse([1 1 zeros(1,2); zeros(1,4); zeros(1,2) 0 1]);
gP2 = [0.1 1 0]';
cP2 = [res.symbcon.MSK_CT_PPOW 3 2 1.0 3.0];

```

Once affine conic descriptions of all cones are ready it remains to stack them vertically into the matrix  $F$  and vector  $g$  and concatenate the cone descriptions in one list. Below is the full code for problem (6.14).

Listing 6.12: Script implementing conic version of problem (6.13).

```

function affcol()

[rcode, res] = mosekopt('symbcon echo(0)');
prob = [];

% Variables [x1; x2; t1; t2]
prob.c = [0, 0, 1, 1];

% Linear inequality x_1 - x_2 <= 1
prob.a = sparse([1, -1, 0, 0]);
prob.buc = 1;
prob.blc = [];

% The quadratic cone
FQ = sparse([zeros(1,4); speye(2) zeros(2,2)]);
gQ = [1 -0.5 -0.6]';
cQ = [res.symbcon.MSK_CT_QUAD 3];

% The power cone for (x_1, 1, t_1) \in POW3^(1/3,2/3)
FP1 = sparse([1 0 zeros(1,2); zeros(1,4); zeros(1,2) 1 0]);
gP1 = [0 1 0]';
cP1 = [res.symbcon.MSK_CT_PPOW 3 2 1/3 2/3];

% The power cone for (x_1+x_2+0.1, 1, t_2) \in POW3^(1/4,3/4)
FP2 = sparse([1 1 zeros(1,2); zeros(1,4); zeros(1,2) 0 1]);
gP2 = [0.1 1 0]';
cP2 = [res.symbcon.MSK_CT_PPOW 3 2 1.0 3.0];

% All cones
prob.f = [FQ; FP1; FP2];
prob.g = [gQ; gP1; gP2];
prob.cones = [cQ cP1 cP2];

[r, res] = mosekopt('maximize', prob);

res.sol.itr.pobjval
res.sol.itr.xx(1:2)

```































```

elseif strcmp(solsta, 'MSK_SOL_STA_PRIMAL_INFEASIBLE_CER')
    fprintf('Primal infeasibility certificate found.');
```

*% The solutions status is unknown. The termination code  
% indicates why the optimizer terminated prematurely.*

```

    fprintf('The solution status is unknown.\n');
    fprintf('Termination code: %s (%d) %s.\n', res.rcodestr, res.rcode, res.
→rmsg);
    else
        fprintf('An unexpected solution status is obtained.');
```

*end*

```

    else
        fprintf('Error during optimization: %s (%d) %s.\n', res.rcodestr, res.rcode,
→ res.rmsg);
    end

    else
        fprintf('Could not read input file, error: %s (%d) %s.\n', res.rcodestr, res.
→rcode, res.rmsg)
    end
end
end
```

## 7.3 Input/Output

### 7.3.1 Stream logging

By default the solver prints a log output analogous to the one produced by the command-line version of **MOSEK**. Logging may be turned off using the command `echo(0)`, for example:

```
[r, res] = mosekopt('minimize echo(0)', prob);
```

Log output may be redirected to a file using the command `log`, for example:

```
[r, res] = mosekopt('minimize log(fileName.txt)', prob);
```

Note that in recent versions of MATLAB the log is not displayed on screen until optimization is completed, which may be an inconvenience for longer tasks. The log written to a file does not have this issue.

Note also that leaving log output on can lead to a dramatic slowdown, visible especially on very small problems.

It is also possible to register a user-defined callback function that will receive and handle all log output, see the *callback* argument of *mosekopt*.









(continued from previous page)

```
callback.iter      = 'callback_handler';      % Defined in callback_handler.m
callback.iterhandle = data;

% Perform the optimization.
[r,res] = mosekopt('minimize echo(0)',prob,[],callback);
```

## 7.7 MOSEK OptServer

**MOSEK** provides an easy way to offload optimization problem to a remote server. This section demonstrates related functionalities from the client side, i.e. sending optimization tasks to the remote server and retrieving solutions.

Setting up and configuring the remote server is described in a separate manual for the OptServer.

### 7.7.1 Synchronous Remote Optimization

In synchronous mode the client sends an optimization problem to the server and blocks, waiting for the optimization to end. Once the result has been received, the program can continue. This is the simplest mode all it takes is to provide the address of the server before starting optimization. The rest of the code remains untouched.

Note that it is impossible to recover the job in case of a broken connection.

#### Source code example

Listing 7.7: Using the OptServer in synchronous mode.

```
function opt_server_sync(inputfile, addr)
clear prob;
clear param;
clear optserver;

% We read some problem from a file or set it up here
cmd = sprintf('read(%s)', inputfile);
[r,res] = mosekopt(cmd);
prob = res.prob;

% OptServer data
% "host" should be 'http://server:port'
optserver.host = addr;

% Perform the optimization with full log output.
[r,res] = mosekopt(sprintf('%s echo(10)', prob.objsense), prob, [], [], optserver);

% Use the optimal x solution.
xx = res.sol.bas.xx;
```



























Table 8.1: List of commands of the MOSEK Python Console.

Command	Description
help [command]	Print list of commands or info about a specific command
log filename	Save the session to a file
intro	Print MOSEK splashscreen
testlic	Test the license system
read filename	Load problem from file
reread	Reload last problem file
solve [options]	Solve current problem
write filename	Write current problem to file
param [name [value]]	Set a parameter or get parameter values
paramdef	Set all parameters to default values
paramdiff	Show parameters with non-default values
info [name]	Get an information item
anapro	Analyze problem data
hist	Plot a histogram of problem data
histsol	Plot a histogram of the solutions
spy	Plot the sparsity pattern of the A matrix
truncate epsilon	Truncate small coefficients down to 0
resobj [fac]	Rescale objective by a factor
anasol	Analyze solutions
removeitg	Remove integrality constraints
removecones	Remove all cones and leave just the linear part
infsub	Replace current problem with its infeasible subproblem
writesol basename	Write solution(s) to file(s) with given basename
delsol	Remove all solutions from the task
optserver [url]	Use an OptServer to optimize
exit	Leave





```

[comment]
An example of small QO problem from Boyd and Vandenberghe, "Convex Optimization",  

↪page 189 ex 4.3  

The solution is (1,0.5,-1)  

[/comment]

[variables]
x0 x1 x2
[/variables]

[objective min]
0.5 (13 x0^2 + 17 x1^2 + 12 x2^2 + 24 x0 * x1 + 12 x1 * x2 - 4 x0 * x2 ) - 22 x0 -  

↪14.5 x1 + 12 x2 + 1  

[/objective]

[bounds]
[b] -1 <= * <= 1 [/b]
[/bounds]

```

The objective function is convex, the minimum is attained for  $x^* = (1, 0.5, -1)$ . The conversion will introduce first a variable  $x_3$  in the objective function such that  $x_3 \geq 1/2x^T Qx$  and then convert the latter directly in conic form. The converted problem follows:

$$\begin{aligned}
&\text{minimize} && -22x_0 - 14.5x_1 + 12x_2 + x_3 + 1 \\
&\text{subject to} && 3.61x_0 + 3.33x_1 - 0.55x_2 - x_6 = 0 \\
& && +2.29x_1 + 3.42x_2 - x_7 = 0 \\
& && 0.81x_1 - x_8 = 0 \\
& && -x_3 + x_4 = 0 \\
& && x_5 = 1 \\
& && (x_4, x_5, x_6, x_7, x_8) \in \mathcal{Q}_\nabla \\
& && -1 \leq x_0, x_1, x_2 \leq 1
\end{aligned}$$

We obtain the reformulation as follows:

```

% prob is a quadratic problem
[r, res] = mosekopt('toconic prob', prob)
probConic = res.prob
mosekopt('write(conic.opf)', probConic)

```

and the output is:

```

[comment]
  Written by MOSEK version 8.1.0.19
  Date 21-08-17
  Time 10:53:36
[/comment]

[hints]
[hint NUMVAR] 9 [/hint]
[hint NUMCON] 4 [/hint]
[hint NUMANZ] 11 [/hint]
[hint NUMQNZ] 0 [/hint]
[hint NUMCONE] 1 [/hint]
[/hints]

[variables disallow_new_variables]
x0000_x0 x0001_x1 x0002_x2 x0003 x0004
x0005 x0006 x0007 x0008
[/variables]

```

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```
prob.sol.bas = bas;

[rcode,res] = mosekopt('minimize',prob,param);

% The new primal optimal solution
res.sol.bas.xx'
```

### 9.2.3 Fixing a variable

In e.g. branch-and-bound methods for integer programming problems it is necessary to reoptimize the problem after a variable has been fixed to a value. This can easily be achieved as follows:

Listing 9.3: Hot-start with a fixed variable.

```
prob.blx(4) = 1;
prob.bux    = [inf inf inf 1]';

% Reuse the basis.
prob.sol.bas = res.sol.bas;

[rcode,res] = mosekopt('minimize',prob,param);

% Display the optimal solution.
res.sol.bas.xx'
```

### 9.2.4 Adding a new constraint

Now assume that the constraint

$$x_1 + x_2 \geq 2$$

should be added to the problem and the problem should be reoptimized. The following example demonstrates how to do this.

Listing 9.4: Hot-start when adding a new constraint.

```
% Modify the problem.
prob.a      = [prob.a; sparse([1.0 1.0 0.0 0.0])];
prob.blc    = [prob.blc; 2.0];
prob.buc    = [prob.buc; inf];

% Obtain the previous optimal basis.
bas         = res.sol.bas;

% Set the solution to the modified problem.
bas.skc     = [bas.skc; 'BS'];
bas.xc      = [bas.xc; bas.xx(1)+bas.xx(2)];
bas.y       = [bas.y; 0.0];
bas.slc     = [bas.slc; 0.0];
bas.suc     = [bas.suc; 0.0];

% Reuse the basis.
prob.sol.bas = bas;

% Reoptimize.
[rcode,res] = mosekopt('minimize',prob,param);
```

(continues on next page)



```
% Obtain the previous optimal basis.
bas      = res.sol.bas;

% Set the solution to the modified problem.
bas.xx    = bas.xx(1:end-1);
bas.skx    = bas.skx(1:end-1,:);
bas.slx    = bas.slx(1:end-1);
bas.sux    = bas.sux(1:end-1);

% Reuse the basis.
prob.sol.bas = bas;

% Reoptimize.
[rcode,res] = mosekopt('minimize',prob,param);

res.sol.bas.xx'
```

# Chapter 10

## Technical guidelines

This section contains some more in-depth technical guidelines for Optimization Toolbox for MATLAB, not strictly necessary for basic use of **MOSEK**.

### 10.1 Integration with MATLAB

#### The `mosekopt` MEX file

The central part of Optimization Toolbox for MATLAB is the `mosekopt` MEX file. It provides an interface to **MOSEK** that is employed by all the other functions provided in the toolbox. Therefore, we recommend to `mosekopt` function if possible because that give rise to the least overhead and provides the maximum of features.

#### Compatibility with the MATLAB Optimization Toolbox

For compatibility with the MATLAB Optimization Toolbox, **MOSEK** provides the following functions:

- `linprog`: Solves linear optimization problems.
- `intlinprog`: Solves a linear optimization problem with integer constrained variables.
- `quadprog`: Solves quadratic optimization problems.
- `lsqlin`: Minimizes a least-squares objective with linear constraints.
- `lsqnonneg`: Minimizes a least-squares objective with nonnegativity constraints.
- `mskoptimget`: Getting an `options` structure for MATLAB compatible functions.
- `mskoptimset`: Setting up an `options` structure for MATLAB compatible functions.

These functions are described in detail in [Sec. 15.2](#). The functions `mskoptimget` and `mskoptimset` are not fully compatible with the MATLAB counterparts, `optimget` and `optimset`, so the **MOSEK** versions should only be used in conjunction with the **MOSEK** implementations of `linprog`, etc., and similarly `optimget` should be used in conjunction with the MATLAB implementations.

#### Caveats using the MATLAB compiler

When using **MOSEK** with the MATLAB compiler it is necessary manually:

- to remove `mosekopt.m` before compilation,
- copy the MEX file to the directory with MATLAB binary files and
- copy the `mosekopt.m` file back after compilation.



Starting the optimization when no license tokens are available will result in an error.

Default behaviour of the license system can be changed in several ways:

- Setting the parameter *MSK\_IPAR\_CACHE\_LICENSE* to "*MSK\_OFF*" will force **MOSEK** to return the license token immediately after the optimization completed.
- Setting the parameter *MSK\_IPAR\_LICENSE\_WAIT* will force **MOSEK** to wait until a license token becomes available instead of returning with an error.
- All licenses currently checked out and not in use can be released on demand using the **nokeepenv** command of *mosekopt*.

```
mosekopt('nokeepenv');
```

# Chapter 11

## Case Studies

In this section we present some case studies in which the Optimization Toolbox for MATLAB is used to solve real-life applications. These examples involve some more advanced modeling skills and possibly some input data. The user is strongly recommended to first read the basic tutorials of [Sec. 6](#) before going through these advanced case studies.

- *Portfolio Optimization*
  - **Keywords:** Markowitz model, variance, risk, efficient frontier, transaction cost, market impact cost, cardinality constraints
  - **Type:** Conic Quadratic, Power Cone, Mixed-Integer
- *Least squares and other norm minimization problems*
  - **Keywords:** Least squares, regression, 2-norm, 1-norm, p-norm, ridge, lasso
  - **Type:** Conic Quadratic, Power Cone
- *Robust linear optimization*
  - **Keywords:** Robust optimization, ellipsoidal uncertainty
  - **Type:** Conic Quadratic

### 11.1 Portfolio Optimization

In this section the Markowitz portfolio optimization problem and variants are implemented using Optimization Toolbox for MATLAB.

- *Basic Markowitz model*
- *Efficient frontier*
- *Factor model and efficiency*
- *Market impact costs*
- *Transaction costs*
- *Cardinality constraints*









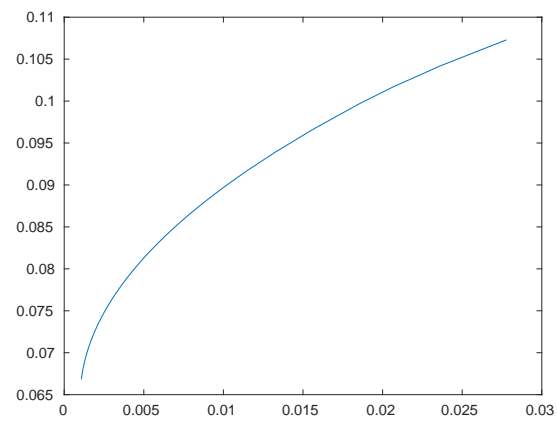


Fig. 11.1: The efficient frontier for the sample data.





## Example code

Listing 11.3 demonstrates how to compute an optimal portfolio when market impact cost are included.

Listing 11.3: Implementation of model (11.10).

```
function [x, t] = MarkowitzWithMarketImpact(n,mu,GT,x0,w,gamma,m)

[rcode, res] = mosekopt('symbcon');

% unrolled variable ordered as (x, t)
prob = [];
prob.c = [mu; zeros(n,1)];

In = speye(n);
On = sparse([], [], [], n, n);

% Linear part
% [ e' m' ] * [ x; t ] = w + e'*x0
prob.a = [ ones(1,n), m' ];
prob.blc = [ w + sum(x0) ];
prob.buc = [ w + sum(x0) ];

% No shortselling and no other bounds
prob.blx = [ zeros(n,1); -inf*ones(n,1) ];
prob.bux = inf*ones(2*n,1);

% Affine conic constraints representing [ gamma, GT*x ] in quadratic cone
prob.f = sparse([ zeros(1,2*n); [GT On] ]);
prob.g = [gamma; zeros(n,1)];
prob.cones = [ res.symbcon.MSK_CT_QUAD n+1 ];

% Extend the affine conic constraints
% with power cones representing t(i) >= |x(i)-x0(i)|^1.5
fi = [];
fj = [];
g = [];
fv = repmat([1; 1], n, 1);
for k=1:n
    fi = [fi; 3*k-2; 3*k];
    fj = [fj; n+k; k];
    g = [g; 0; 1; -x0(k)];
end
prob.f = [prob.f; sparse(fi, fj, fv)];
prob.g = [prob.g; g];
prob.cones = [prob.cones repmat([res.symbcon.MSK_CT_PPOW, 3, 2, 2.0, 1.0], 1, n) ];

[rcode,res] = mosekopt('maximize echo(0)',prob,[]);

x = res.sol.itr.xx(1:n);
t = res.sol.itr.xx(n+(1:n));
```

In the last part of the code we extend the affine conic constraint with triples of the form  $(t_k, 1, x_k - x_k^0)$ . Such a triple is constructed as an affine conic constraint with:

$$\begin{bmatrix} e_{n+k}^T \\ 0 \\ e_k^T \end{bmatrix} \cdot \begin{bmatrix} x \\ t \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \\ -x_k^0 \end{bmatrix}$$







## 11.2 Least Squares and Other Norm Minimization Problems

A frequently occurring problem in statistics and in many other areas of science is a norm minimization problem

$$\begin{array}{ll} \text{minimize} & \|Fx - g\|, \\ \text{subject to} & Ax = b, \end{array} \quad (11.13)$$

where  $x \in \mathbb{R}^n$  and of course we can allow other types of constraints. The objective can involve various norms: infinity norm, 1-norm, 2-norm,  $p$ -norms and so on. For instance the most popular case of the 2-norm corresponds to the least squares linear regression, since it is equivalent to minimization of  $\|Fx - g\|_2^2$ .

### 11.2.1 Least squares, 2-norm

In the case of the 2-norm we specify the problem directly in conic quadratic form

$$\begin{array}{ll} \text{minimize} & t, \\ \text{subject to} & (t, Fx - g) \in \mathcal{Q}^{k+1}, \\ & Ax = b. \end{array} \quad (11.14)$$

The first constraint of the problem can be represented as an affine conic constraint. This leads to the following model.

Listing 11.6: Script solving problem (11.14)

```
% Least squares regression
% minimize \|Fx-g\|_2
function x = norm_lse(F,g,A,b)
clear prob;
[r, res] = mosekopt('symbcon');
n = size(F,2);
k = size(g,1);
m = size(A,1);

% Linear constraints in [x; t]
prob.a = [A, zeros(m,1)];
prob.buc = b;
prob.blc = b;
prob.blx = -inf*ones(n+1,1);
prob.bux = inf*ones(n+1,1);
prob.c = [zeros(n,1); 1];

% Affine conic constraint
prob.f = sparse([zeros(1,n), 1; F, zeros(k,1)]);
prob.g = [0; -g];
prob.cones = [ res.symbcon.MSK_CT_QUAD k+1 ];

% Solve
[r, res] = mosekopt('minimize echo(0)', prob);
x = res.sol.itr.xx(1:n);
end
```







The power cones can be added one by one to the structure representing affine conic constraints. Each power cone will require one  $r_i$ , one copy of  $t$  and one row from  $F$  and  $g$ . An alternative solution is to create the vector

$$[r_1; \dots; r_k; t; \dots; t; Fx - g]$$

and then reshuffle its elements into

$$[r_1; t; F_1x - g_1; \dots; r_k; t; F_kx - g_k]$$

using an appropriate permutation matrix. This approach is demonstrated in the code below.

Listing 11.10: Script solving problem (11.20)

```
% P-norm minimization
% minimize \|Fx-g\|_p
function x = norm_p_norm(F,g,A,b,p)
clear prob;
[r, res] = mosekopt('symbcon');
n = size(F,2);
k = size(g,1);
m = size(A,1);

% Linear constraints in [x; r; t]
prob.a = [A, zeros(m,k+1); zeros(1,n), ones(1,k), -1];
prob.buc = [b; 0];
prob.blc = [b; 0];
prob.blx = -inf*ones(n+k+1,1);
prob.bux = inf*ones(n+k+1,1);
prob.c = [zeros(n+k,1); 1];

% Permutation matrix which picks triples (r_i, t, F_ix-g_i)
M = [];
for i=1:3
    M = [M, sparse(i:3:3*k, 1:k, ones(k,1), 3*k, k)];
end

% Affine conic constraint
prob.f = M * sparse([zeros(k,n), eye(k), zeros(k,1); zeros(k,n+k), ones(k,1); F,
↳ zeros(k,k+1)]);
prob.g = M * [zeros(2*k,1); -g];
prob.cones = [ repmat([res.symbcon.MSK_CT_PPOW, 3, 2, 1.0, p-1], 1, k) ];

% Solve
[r, res] = mosekopt('minimize echo(0)', prob);
x = res.sol.itr.xx(1:n);
end
```

## 11.3 Robust linear Optimization

In most linear optimization examples discussed in this manual it is implicitly assumed that the problem data, such as  $c$  and  $A$ , is known with certainty. However, in practice this is seldom the case, e.g. the data may just be roughly estimated, affected by measurement errors or be affected by random events.

In this section a robust linear optimization methodology is presented which removes the assumption that the problem data is known exactly. Rather it is assumed that the data belongs to some set, i.e. a box or an ellipsoid.

The computations are performed using the **MOSEK** optimization toolbox for MATLAB but could equally well have been implemented using the **MOSEK** API.





















```

                                0, ones(1,n), 0];
prob.a                        = sparse(A);
prob.blc                      = [0;1];
prob.buc                      = [inf;1];
prob.blx                      = [-inf;zeros(n,1);0];
prob.bux                      = inf*ones(n+2,1);
F                             = [zeros(1,n+1), 1; ...
                                zeros(n,1), diag(sigma), zeros(n,1)];
prob.f                        = sparse(F);
prob.cones                    = [ sym.MSK_CT_QUAD n+1 ];

% Run mosekopt
[r,res]=mosekopt('maximize echo(3)',prob);

xx = res.sol.itr.xx;
t  = xx(1);

disp(sprintf('Robust optimal value: %5.4f',t));
x = max(xx(2:1+n),zeros(n,1));

if draw == true
    % Display the solution
    plot([1:1:n],x,'-m');
    grid on;

    disp('Press <Enter> to run simulations');
    pause

    % Run simulations

    Nsim = 10000;
    out  = zeros(Nsim,1);
    for i=1:Nsim,
        returns = delta+(2*rand(1,n)-1).*sigma;
        out(i)  = returns*x;
    end;
    disp(sprintf('Actual returns over %d simulations:',Nsim));
    disp(sprintf('Min=%5.4f Mean=%5.4f Max=%5.4f StD=%5.2f',...
                min(out),mean(out),max(out),std(out)));
    hist(out);
end

```

Here are the results displayed by the script:

Listing 11.15: Output of script *rlo2.m*.

```

Robust optimal value: 1.3428
Actual returns over 10000 simulations:
Min=1.5724 Mean=1.6965 Max=1.8245 StD= 0.03

```

Please note that with our set-up there is exactly one asset with guaranteed return greater than 1 – asset # 1 (bank savings, return 1.04, zero volatility). Consequently, the interval robust counterpart (11.38) prescribes to put our #1 in the bank, thus getting a 4% profit. In contrast to this, the diversified portfolio given by the optimal solution of (11.39) never yields profit less than 57.2%, and yields at average a 69.67% profit with pretty low (0.03) standard deviation. We see that in favorable circumstances the ellipsoidal robust counterpart of an uncertain linear program indeed is less conservative than, although basically as reliable as, the interval robust counterpart.

Finally, let us compare our results with those given by the nominal optimal solution. The latter

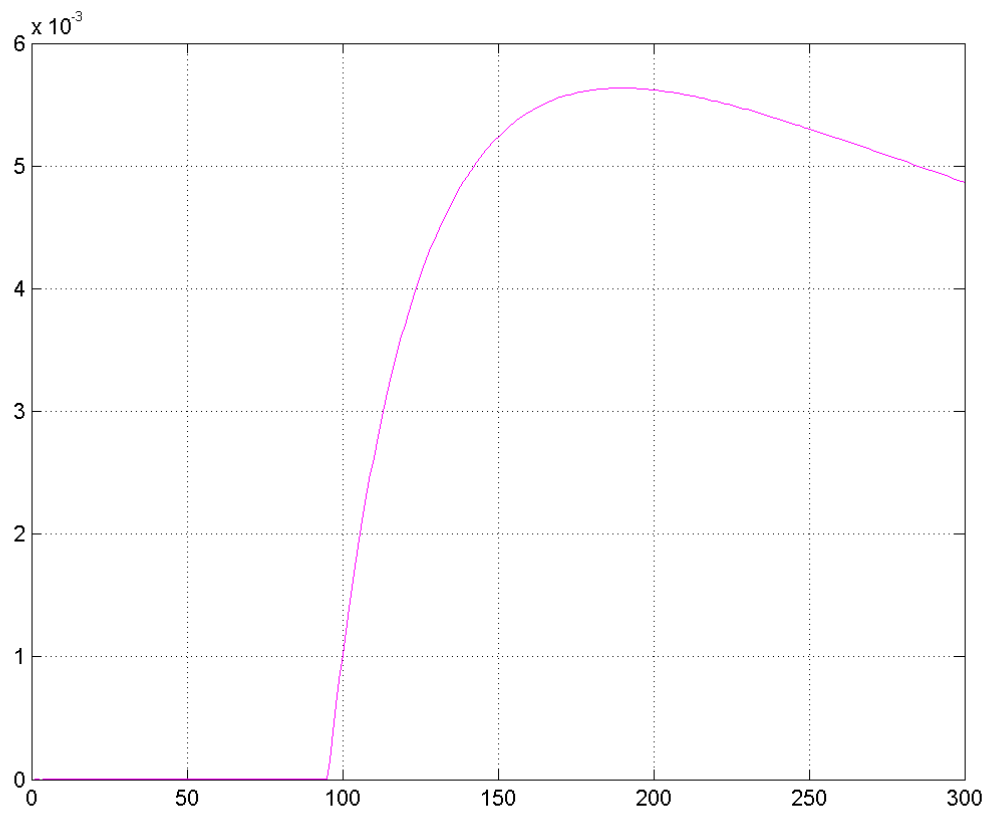


Fig. 11.4: Distribution of investments among the assets in the optimal solution of.



# Chapter 12

## Problem Formulation and Solutions

In this chapter we will discuss the following issues:

- The formal, mathematical formulations of the problem types that **MOSEK** can solve and their duals.
- The solution information produced by **MOSEK**.
- The infeasibility certificate produced by **MOSEK** if the problem is infeasible.

For the underlying mathematical concepts, derivations and proofs see the [Modeling Cookbook](#) or any book on convex optimization. This chapter explains how the related data is organized specifically within the **MOSEK** API.

### 12.1 Linear Optimization

**MOSEK** accepts linear optimization problems of the form

$$\begin{array}{llllll} \text{minimize} & & c^T x + c^f & & & \\ \text{subject to} & l^c & \leq & Ax & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x, \end{array} \quad (12.1)$$

where

- $m$  is the number of constraints.
- $n$  is the number of decision variables.
- $x \in \mathbb{R}^n$  is a vector of decision variables.
- $c \in \mathbb{R}^n$  is the linear part of the objective function.
- $c^f \in \mathbb{R}$  is a constant term in the objective
- $A \in \mathbb{R}^{m \times n}$  is the constraint matrix.
- $l^c \in \mathbb{R}^m$  is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$  is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$  is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$  is the upper limit on the activity for the variables.

Lower and upper bounds can be infinite, or in other words the corresponding bound may be omitted.

A primal solution ( $x$ ) is *(primal) feasible* if it satisfies all constraints in (12.1). If (12.1) has at least one primal feasible solution, then (12.1) is said to be (primal) feasible. In case (12.1) does not have a feasible solution, the problem is said to be *(primal) infeasible*.



















## Duality

The dual of problem (12.24) is

$$\begin{aligned}
& \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x - \dot{y}^T g + c^f \\
& \text{subject to} && \\
& && A^T y + s_l^x - s_u^x + F^T \dot{y} = c, \\
& && -y + s_l^c - s_u^c = 0, \\
& && \bar{C}_j - \sum_{i=0}^{m-1} y_i \bar{A}_{ij} = \bar{S}_j, && j = 0, \dots, p-1 \\
& && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\
& && \dot{y} \in \mathcal{K}^*, \\
& && \bar{S}_j \in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1.
\end{aligned} \tag{12.25}$$

Duality and infeasibility certificates behave analogously as in Sec. 12.2.

## Remark

A problem of this form is internally converted into the problem:

$$\begin{aligned}
& \text{minimize} && \sum_{j=1}^n c_j x_j + \sum_{j=1}^p \langle \bar{C}_j, \bar{X}_j \rangle + c^f \\
& \text{subject to} && l_i^c \leq \sum_{j=1}^n a_{ij} x_j + \sum_{j=1}^p \langle \bar{A}_{ij}, \bar{X}_j \rangle \leq u_i^c, \quad i = 1, \dots, m, \\
& && g_i \leq z_i - \sum_{j=1}^n f_{ij} x_j \leq g_i, \quad i = 1, \dots, k, \\
& && l_j^x \leq x_j \leq u_j^x, \quad j = 1, \dots, n, \\
& && z \in \mathcal{K}, \\
& && \bar{X}_j \in \mathcal{S}_+^{r_j}, && j = 1, \dots, p
\end{aligned} \tag{12.26}$$

which conforms with the format in Sec. 12.2 and Sec. 12.3. The reformulated problem has  $n+k$  variables,  $m+k$  linear constraints and in total  $k$  variables in cones. The new columns and rows are appended at the end of the original ones. If a problem with affine conic constraints is saved to a file then this reformulation will be written.

# Chapter 13

## Optimizers

The most essential part of **MOSEK** are the optimizers:

- *primal simplex* (linear problems),
- *dual simplex* (linear problems),
- *interior-point* (linear, quadratic and conic problems),
- *mixed-integer* (problems with integer variables).

The structure of a successful optimization process is roughly:

- **Presolve**
  1. *Elimination*: Reduce the size of the problem.
  2. *Dualizer*: Choose whether to solve the primal or the dual form of the problem.
  3. *Scaling*: Scale the problem for better numerical stability.
- **Optimization**
  1. *Optimize*: Solve the problem using selected method.
  2. *Terminate*: Stop the optimization when specific termination criteria have been met.
  3. *Report*: Return the solution or an infeasibility certificate.

The preprocessing stage is transparent to the user, but useful to know about for tuning purposes. The purpose of the preprocessing steps is to make the actual optimization more efficient and robust. We discuss the details of the above steps in the following sections.

### 13.1 Presolve

Before an optimizer actually performs the optimization the problem is preprocessed using the so-called presolve. The purpose of the presolve is to

1. remove redundant constraints,
2. eliminate fixed variables,
3. remove linear dependencies,
4. substitute out (implied) free variables, and
5. reduce the size of the optimization problem in general.

After the presolved problem has been optimized the solution is automatically postsolved so that the returned solution is valid for the original problem. Hence, the presolve is completely transparent. For further details about the presolve phase, please see [AA95] and [AGMeszarosX96].

It is possible to fine-tune the behavior of the presolve or to turn it off entirely. If presolve consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This is done by setting the parameter `MSK_IPAR_PRESOLVE_USE` to `"MSK_PRESOLVE_MODE_OFF"`. The two most time-consuming steps of the presolve are



## Scaling

Problems containing data with large and/or small coefficients, say  $1.0e + 9$  or  $1.0e - 7$ , are often hard to solve. Significant digits may be truncated in calculations with finite precision, which can result in the optimizer relying on inaccurate data. Since computers work in finite precision, extreme coefficients should be avoided. In general, data around the same *order of magnitude* is preferred, and we will refer to a problem, satisfying this loose property, as being *well-scaled*. If the problem is not well scaled, **MOSEK** will try to scale (multiply) constraints and variables by suitable constants. **MOSEK** solves the scaled problem to improve the numerical properties.

The scaling process is transparent, i.e. the solution to the original problem is reported. It is important to be aware that the optimizer terminates when the termination criterion is met on the scaled problem, therefore significant primal or dual infeasibilities may occur after unscaling for badly scaled problems. The best solution of this issue is to reformulate the problem, making it better scaled.

By default **MOSEK** heuristically chooses a suitable scaling. The scaling for interior-point and simplex optimizers can be controlled with the parameters `MSK_IPAR_INTPNT_SCALING` and `MSK_IPAR_SIM_SCALING` respectively.

## 13.2 Linear Optimization

### 13.2.1 Optimizer Selection

Two different types of optimizers are available for linear problems: The default is an interior-point method, and the alternative is the simplex method (primal or dual). The optimizer can be selected using the parameter `MSK_IPAR_OPTIMIZER`.

#### The Interior-point or the Simplex Optimizer?

Given a linear optimization problem, which optimizer is the best: the simplex or the interior-point optimizer? It is impossible to provide a general answer to this question. However, the interior-point optimizer behaves more predictably: it tends to use between 20 and 100 iterations, almost independently of problem size, but cannot perform warm-start. On the other hand the simplex method can take advantage of an initial solution, but is less predictable from cold-start. The interior-point optimizer is used by default.

#### The Primal or the Dual Simplex Variant?

**MOSEK** provides both a primal and a dual simplex optimizer. Predicting which simplex optimizer is faster is impossible, however, in recent years the dual optimizer has seen several algorithmic and computational improvements, which, in our experience, make it faster on average than the primal version. Still, it depends much on the problem structure and size. Setting the `MSK_IPAR_OPTIMIZER` parameter to `"MSK_OPTIMIZER_FREE_SIMPLEX"` instructs **MOSEK** to choose one of the simplex variants automatically.

To summarize, if you want to know which optimizer is faster for a given problem type, it is best to try all the options.

### 13.2.2 The Interior-point Optimizer

The purpose of this section is to provide information about the algorithm employed in the **MOSEK** interior-point optimizer for linear problems and about its termination criteria.









































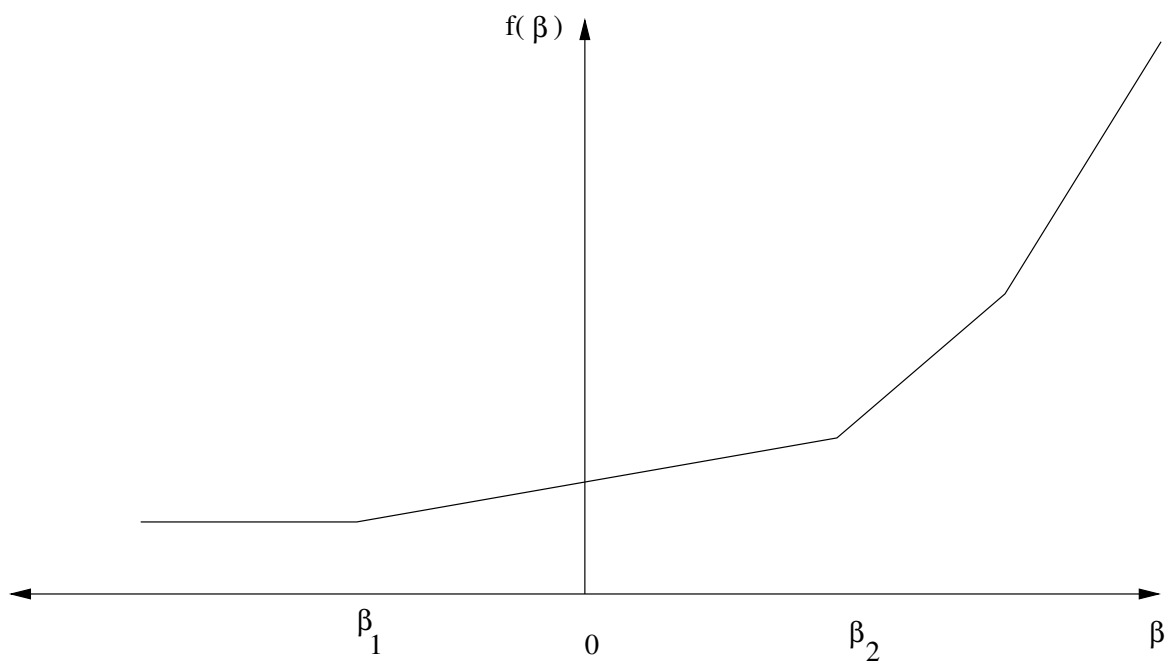


Fig. 14.1:  $\beta = 0$  is in the interior of linearity interval.

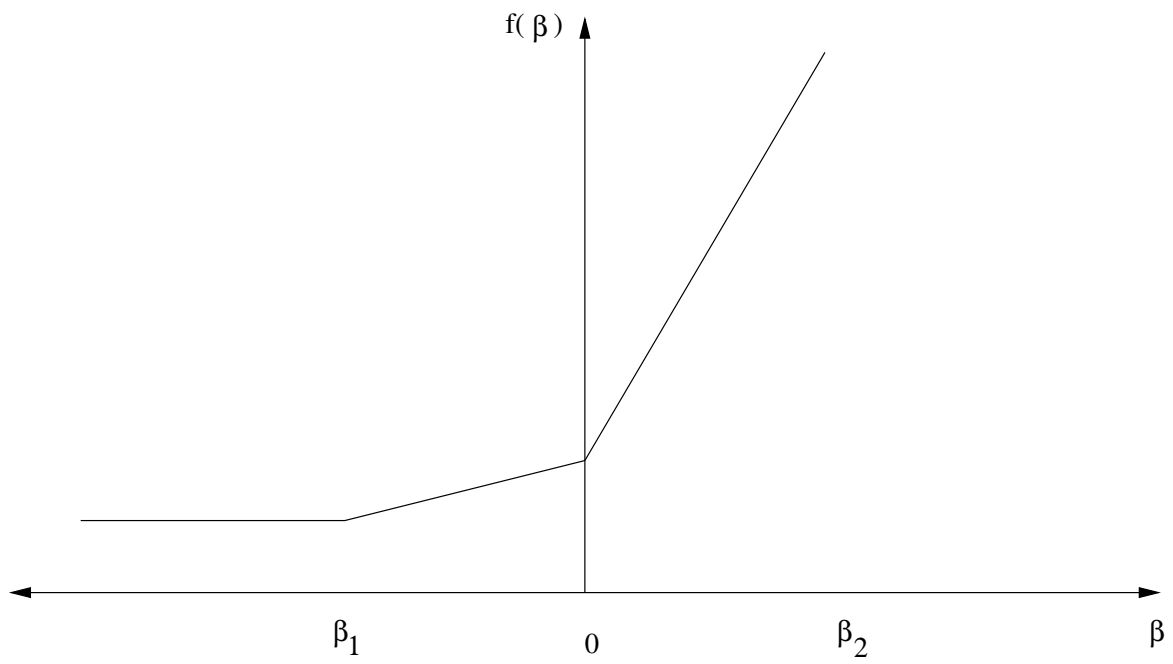


Fig. 14.2:  $\beta = 0$  is a breakpoint.











(continued from previous page)

```
var = 5, beta_1 = Inf, beta_2 = 500.0, delta_1 = 0.0,delta_2 = 0.0
var = 6, beta_1 = Inf, beta_2 = 500.0, delta_1 = 0.0,delta_2 = 0.0
var = 7, beta_1 = -0.0, beta_2 = 500.0, delta_1 = 2.0,delta_2 = 2.0
Sensitivity for coefficients in objective:
var = 1, beta_1 = Inf, beta_2 = 3.0, delta_1 = 300.0,delta_2 = 300.0
var = 2, beta_1 = Inf, beta_2 = Inf, delta_1 = 100.0,delta_2 = 100.0
var = 3, beta_1 = -2.0, beta_2 = Inf, delta_1 = 0.0,delta_2 = 0.0
var = 4, beta_1 = Inf, beta_2 = 2.0, delta_1 = 500.0,delta_2 = 500.0
var = 5, beta_1 = -3.0, beta_2 = Inf, delta_1 = 500.0,delta_2 = 500.0
var = 6, beta_1 = Inf, beta_2 = 2.0, delta_1 = 500.0,delta_2 = 500.0
var = 7, beta_1 = -2.0, beta_2 = Inf, delta_1 = 0.0,delta_2 = 0.0
```

# Chapter 15

## Toolbox API Reference

- *General API conventions.*
- **Command reference:**
  - *Complete list of functions*
  - *mosekopt* - the main interface
  - *Data structures*
- **Optimizer parameters:**
  - *Double, Integer, String*
  - *Full list*
  - *Browse by topic*
- **Optimizer information items:**
  - *Double, Integer, Long*
- *Optimizer response codes*
- *Constants*
- *Functions compatible with the MATLAB Optimization Toolbox*
- *Nonlinear API (mskenopt, mskscopt, mskgpopt)*

### 15.1 API conventions

#### Problem setup

An optimization problem in Optimization Toolbox for MATLAB is specified using the *prob* structure. The specification of numerical part of the data can be found in [Sec. 15.3.1](#).

#### Constants

Constants mentioned in [Sec. 15.7](#) and [Sec. 15.5](#) can be used as strings or as symbolic constants. To get the structure with all symbolic constants available execute:

```
[r, res] = mosekopt('symbcon');
```

They can later be used simply as, for example:

```
res.symbcon.MSK_IPAR_OPTIMIZER
```















- **options** [in] (struct) – An optimization options structure (optional). See the *mskoptimset* function for the definition of the optimizations options structure. This function uses the options
  - *.Diagnostics*
  - *.Display*
  - *.MaxIter*
  - *.Write*

#### Return

- **x** (double[]) – The  $x$  solution.
- **fval** (double) – The optimal objective value i.e.  $\frac{1}{2}x^T Hx + f^T x$ .
- **exitflag** (int) – A scalar which has the interpretation:
  - $< 0$  The problem is likely to be either primal or dual infeasible.
  - $= 0$  The maximum number of iterations was reached.
  - $> 0$   $x$  is an optimal solution.
- **output** (struct) – A structure with the following fields
  - *.iterations* Number of iterations spent to reach the optimum.
  - *.algorithm* Always defined as 'MOSEK'.
- **lambda** (struct) – A structure with the following fields
  - *.lower* Lagrange multipliers for lower bounds  $l$ .
  - *.upper* Lagrange multipliers for upper bounds  $u$ .
  - *.ineqlin* Lagrange multipliers for inequalities.
  - *.eqlin* Lagrange multipliers for equalities.

## 15.3 Data Structures and Notation

We specify the notation and data structures used in the interface.

#### Problem definition

- *prob* — describes an optimization problem.
- *cones* — description of cones.
- *names* — names of objects in the optimization problem.
- *barc*, *bara* — description of the semidefinite part.

#### Solutions

- *res* — result returned by *mosekopt*.
- *solver\_solutions* — solutions.
- *solution* — one solution.

#### Other

- *primal\_repair* — used in feasibility repair.
- *prisen*, *prisen\_data*, *duasen* — used in sensitivity analysis.
- *callback* — used to set up a callback function.
- *optserver* — used to set up remote optimization.

















### Basis identification

- *MSK\_DPAR\_SIM\_LU\_TOL\_REL\_PIV*
- *MSK\_IPAR\_BI\_CLEAN\_OPTIMIZER*
- *MSK\_IPAR\_BI\_IGNORE\_MAX\_ITER*
- *MSK\_IPAR\_BI\_IGNORE\_NUM\_ERROR*
- *MSK\_IPAR\_BI\_MAX\_ITERATIONS*
- *MSK\_IPAR\_INTPNT\_BASIS*
- *MSK\_IPAR\_LOG\_BI*
- *MSK\_IPAR\_LOG\_BI\_FREQ*

### Conic interior-point method

- *MSK\_DPAR\_INTPNT\_CO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_REL\_GAP*

### Data check

- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL*
- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_HUGE*
- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_LARGE*
- *MSK\_DPAR\_DATA\_TOL\_AIJ\_HUGE*
- *MSK\_DPAR\_DATA\_TOL\_AIJ\_LARGE*
- *MSK\_DPAR\_DATA\_TOL\_BOUND\_INF*
- *MSK\_DPAR\_DATA\_TOL\_BOUND\_WRN*
- *MSK\_DPAR\_DATA\_TOL\_C\_HUGE*
- *MSK\_DPAR\_DATA\_TOL\_CJ\_LARGE*
- *MSK\_DPAR\_DATA\_TOL\_QIJ*
- *MSK\_DPAR\_DATA\_TOL\_X*
- *MSK\_DPAR\_SEMIDEFINITE\_TOL\_APPROX*
- *MSK\_IPAR\_CHECK\_CONVEXITY*
- *MSK\_IPAR\_LOG\_CHECK\_CONVEXITY*

## Data input/output

- *MSK\_IPAR\_INFEAS\_REPORT\_AUTO*
- *MSK\_IPAR\_LOG\_FILE*
- *MSK\_IPAR\_OPF\_WRITE\_HEADER*
- *MSK\_IPAR\_OPF\_WRITE\_HINTS*
- *MSK\_IPAR\_OPF\_WRITE\_LINE\_LENGTH*
- *MSK\_IPAR\_OPF\_WRITE\_PARAMETERS*
- *MSK\_IPAR\_OPF\_WRITE\_PROBLEM*
- *MSK\_IPAR\_OPF\_WRITE\_SOL\_BAS*
- *MSK\_IPAR\_OPF\_WRITE\_SOL\_ITG*
- *MSK\_IPAR\_OPF\_WRITE\_SOL\_ITR*
- *MSK\_IPAR\_OPF\_WRITE\_SOLUTIONS*
- *MSK\_IPAR\_PARAM\_READ\_CASE\_NAME*
- *MSK\_IPAR\_PARAM\_READ\_IGN\_ERROR*
- *MSK\_IPAR\_PTF\_WRITE\_TRANSFORM*
- *MSK\_IPAR\_READ\_DEBUG*
- *MSK\_IPAR\_READ\_KEEP\_FREE\_CON*
- *MSK\_IPAR\_READ\_LP\_DROP\_NEW\_VARS\_IN\_BOU*
- *MSK\_IPAR\_READ\_LP\_QUOTED\_NAMES*
- *MSK\_IPAR\_READ\_MPS\_FORMAT*
- *MSK\_IPAR\_READ\_MPS\_WIDTH*
- *MSK\_IPAR\_READ\_TASK\_IGNORE\_PARAM*
- *MSK\_IPAR\_SOL\_READ\_NAME\_WIDTH*
- *MSK\_IPAR\_SOL\_READ\_WIDTH*
- *MSK\_IPAR\_WRITE\_BAS\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_BAS\_HEAD*
- *MSK\_IPAR\_WRITE\_BAS\_VARIABLES*
- *MSK\_IPAR\_WRITE\_COMPRESSION*
- *MSK\_IPAR\_WRITE\_DATA\_PARAM*
- *MSK\_IPAR\_WRITE\_FREE\_CON*
- *MSK\_IPAR\_WRITE\_GENERIC\_NAMES*
- *MSK\_IPAR\_WRITE\_GENERIC\_NAMES\_IO*
- *MSK\_IPAR\_WRITE\_IGNORE\_INCOMPATIBLE\_ITEMS*
- *MSK\_IPAR\_WRITE\_INT\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_INT\_HEAD*
- *MSK\_IPAR\_WRITE\_INT\_VARIABLES*

- *MSK\_IPAR\_WRITE\_LP\_FULL\_OBJ*
- *MSK\_IPAR\_WRITE\_LP\_LINE\_WIDTH*
- *MSK\_IPAR\_WRITE\_LP\_QUOTED\_NAMES*
- *MSK\_IPAR\_WRITE\_LP\_STRICT\_FORMAT*
- *MSK\_IPAR\_WRITE\_LP\_TERMS\_PER\_LINE*
- *MSK\_IPAR\_WRITE\_MPS\_FORMAT*
- *MSK\_IPAR\_WRITE\_MPS\_INT*
- *MSK\_IPAR\_WRITE\_PRECISION*
- *MSK\_IPAR\_WRITE\_SOL\_BARVARIABLES*
- *MSK\_IPAR\_WRITE\_SOL\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_SOL\_HEAD*
- *MSK\_IPAR\_WRITE\_SOL\_IGNORE\_INVALID\_NAMES*
- *MSK\_IPAR\_WRITE\_SOL\_VARIABLES*
- *MSK\_IPAR\_WRITE\_TASK\_INC\_SOL*
- *MSK\_IPAR\_WRITE\_XML\_MODE*
- *MSK\_SPAR\_BAS\_SOL\_FILE\_NAME*
- *MSK\_SPAR\_DATA\_FILE\_NAME*
- *MSK\_SPAR\_DEBUG\_FILE\_NAME*
- *MSK\_SPAR\_INT\_SOL\_FILE\_NAME*
- *MSK\_SPAR\_ITR\_SOL\_FILE\_NAME*
- *MSK\_SPAR\_MIO\_DEBUG\_STRING*
- *MSK\_SPAR\_PARAM\_COMMENT\_SIGN*
- *MSK\_SPAR\_PARAM\_READ\_FILE\_NAME*
- *MSK\_SPAR\_PARAM\_WRITE\_FILE\_NAME*
- *MSK\_SPAR\_READ\_MPS\_BOU\_NAME*
- *MSK\_SPAR\_READ\_MPS\_OBJ\_NAME*
- *MSK\_SPAR\_READ\_MPS\_RAN\_NAME*
- *MSK\_SPAR\_READ\_MPS\_RHS\_NAME*
- *MSK\_SPAR\_SENSITIVITY\_FILE\_NAME*
- *MSK\_SPAR\_SENSITIVITY\_RES\_FILE\_NAME*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_UPR*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_UPR*
- *MSK\_SPAR\_STAT\_FILE\_NAME*
- *MSK\_SPAR\_STAT\_KEY*
- *MSK\_SPAR\_STAT\_NAME*
- *MSK\_SPAR\_WRITE\_LP\_GEN\_VAR\_NAME*

## Debugging

- *MSK\_IPAR\_AUTO\_SORT\_A\_BEFORE\_OPT*

## Dual simplex

- *MSK\_IPAR\_SIM\_DUAL\_CRASH*
- *MSK\_IPAR\_SIM\_DUAL\_RESTRICT\_SELECTION*
- *MSK\_IPAR\_SIM\_DUAL\_SELECTION*

## Infeasibility report

- *MSK\_IPAR\_INFEAS\_GENERIC\_NAMES*
- *MSK\_IPAR\_INFEAS\_REPORT\_LEVEL*
- *MSK\_IPAR\_LOG\_INFEAS\_ANA*

## Interior-point method

- *MSK\_DPAR\_CHECK\_CONVEXITY\_REL\_TOL*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_DSAFE*
- *MSK\_DPAR\_INTPNT\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_TOL\_PATH*
- *MSK\_DPAR\_INTPNT\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_PSAFE*
- *MSK\_DPAR\_INTPNT\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_TOL\_REL\_STEP*
- *MSK\_DPAR\_INTPNT\_TOL\_STEP\_SIZE*

- *MSK\_DPAR\_QCQO\_REFORMULATE\_REL\_DROP\_TOL*
- *MSK\_IPAR\_BI\_IGNORE\_MAX\_ITER*
- *MSK\_IPAR\_BI\_IGNORE\_NUM\_ERROR*
- *MSK\_IPAR\_INTPNT\_BASIS*
- *MSK\_IPAR\_INTPNT\_DIFF\_STEP*
- *MSK\_IPAR\_INTPNT\_HOTSTART*
- *MSK\_IPAR\_INTPNT\_MAX\_ITERATIONS*
- *MSK\_IPAR\_INTPNT\_MAX\_NUM\_COR*
- *MSK\_IPAR\_INTPNT\_MAX\_NUM\_REFINEMENT\_STEPS*
- *MSK\_IPAR\_INTPNT\_OFF\_COL\_TRH*
- *MSK\_IPAR\_INTPNT\_ORDER\_GP\_NUM\_SEEDS*
- *MSK\_IPAR\_INTPNT\_ORDER\_METHOD*
- *MSK\_IPAR\_INTPNT\_PURIFY*
- *MSK\_IPAR\_INTPNT\_REGULARIZATION\_USE*
- *MSK\_IPAR\_INTPNT\_SCALING*
- *MSK\_IPAR\_INTPNT\_SOLVE\_FORM*
- *MSK\_IPAR\_INTPNT\_STARTING\_POINT*
- *MSK\_IPAR\_LOG\_INTPNT*

#### License manager

- *MSK\_IPAR\_CACHE\_LICENSE*
- *MSK\_IPAR\_LICENSE\_DEBUG*
- *MSK\_IPAR\_LICENSE\_PAUSE\_TIME*
- *MSK\_IPAR\_LICENSE\_SUPPRESS\_EXPIRE\_WRNS*
- *MSK\_IPAR\_LICENSE\_TRH\_EXPIRY\_WRN*
- *MSK\_IPAR\_LICENSE\_WAIT*

#### Logging

- *MSK\_IPAR\_LOG*
- *MSK\_IPAR\_LOG\_ANA\_PRO*
- *MSK\_IPAR\_LOG\_BI*
- *MSK\_IPAR\_LOG\_BI\_FREQ*
- *MSK\_IPAR\_LOG\_CUT\_SECOND\_OPT*
- *MSK\_IPAR\_LOG\_EXPAND*
- *MSK\_IPAR\_LOG\_FEAS\_REPAIR*
- *MSK\_IPAR\_LOG\_FILE*

- *MSK\_IPAR\_LOG\_INCLUDE\_SUMMARY*
- *MSK\_IPAR\_LOG\_INFEAS\_ANA*
- *MSK\_IPAR\_LOG\_INTPNT*
- *MSK\_IPAR\_LOG\_LOCAL\_INFO*
- *MSK\_IPAR\_LOG\_MIO*
- *MSK\_IPAR\_LOG\_MIO\_FREQ*
- *MSK\_IPAR\_LOG\_ORDER*
- *MSK\_IPAR\_LOG\_PRESOLVE*
- *MSK\_IPAR\_LOG\_RESPONSE*
- *MSK\_IPAR\_LOG\_SENSITIVITY*
- *MSK\_IPAR\_LOG\_SENSITIVITY\_OPT*
- *MSK\_IPAR\_LOG\_SIM*
- *MSK\_IPAR\_LOG\_SIM\_FREQ*
- *MSK\_IPAR\_LOG\_STORAGE*

#### **Mixed-integer optimization**

- *MSK\_DPAR\_MIO\_MAX\_TIME*
- *MSK\_DPAR\_MIO\_REL\_GAP\_CONST*
- *MSK\_DPAR\_MIO\_TOL\_ABS\_GAP*
- *MSK\_DPAR\_MIO\_TOL\_ABS\_RELAX\_INT*
- *MSK\_DPAR\_MIO\_TOL\_FEAS*
- *MSK\_DPAR\_MIO\_TOL\_REL\_DUAL\_BOUND\_IMPROVEMENT*
- *MSK\_DPAR\_MIO\_TOL\_REL\_GAP*
- *MSK\_IPAR\_LOG\_MIO*
- *MSK\_IPAR\_LOG\_MIO\_FREQ*
- *MSK\_IPAR\_MIO\_BRANCH\_DIR*
- *MSK\_IPAR\_MIO\_CONIC\_OUTER\_APPROXIMATION*
- *MSK\_IPAR\_MIO\_CUT\_CLIQUE*
- *MSK\_IPAR\_MIO\_CUT\_CMIR*
- *MSK\_IPAR\_MIO\_CUT\_GMI*
- *MSK\_IPAR\_MIO\_CUT\_IMPLIED\_BOUND*
- *MSK\_IPAR\_MIO\_CUT\_KNAPSACK\_COVER*
- *MSK\_IPAR\_MIO\_CUT\_SELECTION\_LEVEL*
- *MSK\_IPAR\_MIO\_FEASPUMP\_LEVEL*
- *MSK\_IPAR\_MIO\_HEURISTIC\_LEVEL*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_BRANCHES*

- *MSK\_IPAR\_MIO\_MAX\_NUM\_RELAXS*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_ROOT\_CUT\_ROUNDS*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_SOLUTIONS*
- *MSK\_IPAR\_MIO\_NODE\_OPTIMIZER*
- *MSK\_IPAR\_MIO\_NODE\_SELECTION*
- *MSK\_IPAR\_MIO\_PERSPECTIVE\_REFORMULATE*
- *MSK\_IPAR\_MIO\_PROBING\_LEVEL*
- *MSK\_IPAR\_MIO\_PROPAGATE\_OBJECTIVE\_CONSTRAINT*
- *MSK\_IPAR\_MIO\_RINS\_MAX\_NODES*
- *MSK\_IPAR\_MIO\_ROOT\_OPTIMIZER*
- *MSK\_IPAR\_MIO\_ROOT\_REPEAT\_PRESOLVE\_LEVEL*
- *MSK\_IPAR\_MIO\_SEED*
- *MSK\_IPAR\_MIO\_VB\_DETECTION\_LEVEL*

## Output information

- *MSK\_IPAR\_INFEAS\_REPORT\_LEVEL*
- *MSK\_IPAR\_LICENSE\_SUPPRESS\_EXPIRE\_WRNS*
- *MSK\_IPAR\_LICENSE\_TRH\_EXPIRY\_WRN*
- *MSK\_IPAR\_LOG*
- *MSK\_IPAR\_LOG\_BI*
- *MSK\_IPAR\_LOG\_BI\_FREQ*
- *MSK\_IPAR\_LOG\_CUT\_SECOND\_OPT*
- *MSK\_IPAR\_LOG\_EXPAND*
- *MSK\_IPAR\_LOG\_FEAS\_REPAIR*
- *MSK\_IPAR\_LOG\_FILE*
- *MSK\_IPAR\_LOG\_INCLUDE\_SUMMARY*
- *MSK\_IPAR\_LOG\_INFEAS\_ANA*
- *MSK\_IPAR\_LOG\_INTPNT*
- *MSK\_IPAR\_LOG\_LOCAL\_INFO*
- *MSK\_IPAR\_LOG\_MIO*
- *MSK\_IPAR\_LOG\_MIO\_FREQ*
- *MSK\_IPAR\_LOG\_ORDER*
- *MSK\_IPAR\_LOG\_RESPONSE*
- *MSK\_IPAR\_LOG\_SENSITIVITY*
- *MSK\_IPAR\_LOG\_SENSITIVITY\_OPT*
- *MSK\_IPAR\_LOG\_SIM*

- *MSK\_IPAR\_LOG\_SIM\_FREQ*
- *MSK\_IPAR\_LOG\_SIM\_MINOR*
- *MSK\_IPAR\_LOG\_STORAGE*
- *MSK\_IPAR\_MAX\_NUM\_WARNINGS*

#### Overall solver

- *MSK\_IPAR\_BI\_CLEAN\_OPTIMIZER*
- *MSK\_IPAR\_INFEAS\_PREFER\_PRIMAL*
- *MSK\_IPAR\_LICENSE\_WAIT*
- *MSK\_IPAR\_MIO\_MODE*
- *MSK\_IPAR\_OPTIMIZER*
- *MSK\_IPAR\_PRESOLVE\_LEVEL*
- *MSK\_IPAR\_PRESOLVE\_MAX\_NUM\_REDUCTIONS*
- *MSK\_IPAR\_PRESOLVE\_USE*
- *MSK\_IPAR\_PRIMAL\_REPAIR\_OPTIMIZER*
- *MSK\_IPAR\_SENSITIVITY\_ALL*
- *MSK\_IPAR\_SENSITIVITY\_OPTIMIZER*
- *MSK\_IPAR\_SENSITIVITY\_TYPE*
- *MSK\_IPAR\_SOLUTION\_CALLBACK*

#### Overall system

- *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO*
- *MSK\_IPAR\_INTPNT\_MULTI\_THREAD*
- *MSK\_IPAR\_LICENSE\_WAIT*
- *MSK\_IPAR\_LOG\_STORAGE*
- *MSK\_IPAR\_MT\_SPINCOUNT*
- *MSK\_IPAR\_NUM\_THREADS*
- *MSK\_IPAR\_REMOVE\_UNUSED\_SOLUTIONS*
- *MSK\_IPAR\_TIMING\_LEVEL*
- *MSK\_SPAR\_REMOTE\_ACCESS\_TOKEN*

## Presolve

- *MSK\_DPAR\_PRESOLVE\_TOL\_ABS\_LINDEP*
- *MSK\_DPAR\_PRESOLVE\_TOL\_AIJ*
- *MSK\_DPAR\_PRESOLVE\_TOL\_REL\_LINDEP*
- *MSK\_DPAR\_PRESOLVE\_TOL\_S*
- *MSK\_DPAR\_PRESOLVE\_TOL\_X*
- *MSK\_IPAR\_PRESOLVE\_ELIMINATOR\_MAX\_FILL*
- *MSK\_IPAR\_PRESOLVE\_ELIMINATOR\_MAX\_NUM\_TRIES*
- *MSK\_IPAR\_PRESOLVE\_LEVEL*
- *MSK\_IPAR\_PRESOLVE\_LINDEP\_ABS\_WORK\_TRH*
- *MSK\_IPAR\_PRESOLVE\_LINDEP\_REL\_WORK\_TRH*
- *MSK\_IPAR\_PRESOLVE\_LINDEP\_USE*
- *MSK\_IPAR\_PRESOLVE\_MAX\_NUM\_PASS*
- *MSK\_IPAR\_PRESOLVE\_MAX\_NUM\_REDUCTIONS*
- *MSK\_IPAR\_PRESOLVE\_USE*

## Primal simplex

- *MSK\_IPAR\_SIM\_PRIMAL\_CRASH*
- *MSK\_IPAR\_SIM\_PRIMAL\_RESTRICT\_SELECTION*
- *MSK\_IPAR\_SIM\_PRIMAL\_SELECTION*

## Progress callback

- *MSK\_IPAR\_SOLUTION\_CALLBACK*

## Simplex optimizer

- *MSK\_DPAR\_BASIS\_REL\_TOL\_S*
- *MSK\_DPAR\_BASIS\_TOL\_S*
- *MSK\_DPAR\_BASIS\_TOL\_X*
- *MSK\_DPAR\_SIM\_LU\_TOL\_REL\_PIV*
- *MSK\_DPAR\_SIMPLEX\_ABS\_TOL\_PIV*
- *MSK\_IPAR\_BASIS\_SOLVE\_USE\_PLUS\_ONE*
- *MSK\_IPAR\_LOG\_SIM*
- *MSK\_IPAR\_LOG\_SIM\_FREQ*
- *MSK\_IPAR\_LOG\_SIM\_MINOR*
- *MSK\_IPAR\_SENSITIVITY\_OPTIMIZER*
- *MSK\_IPAR\_SIM\_BASIS\_FACTOR\_USE*
- *MSK\_IPAR\_SIM\_DEGEN*

- *MSK\_IPAR\_SIM\_DUAL\_PHASEONE\_METHOD*
- *MSK\_IPAR\_SIM\_EXPLOIT\_DUPVEC*
- *MSK\_IPAR\_SIM\_HOTSTART*
- *MSK\_IPAR\_SIM\_HOTSTART\_LU*
- *MSK\_IPAR\_SIM\_MAX\_ITERATIONS*
- *MSK\_IPAR\_SIM\_MAX\_NUM\_SETBACKS*
- *MSK\_IPAR\_SIM\_NON\_SINGULAR*
- *MSK\_IPAR\_SIM\_PRIMAL\_PHASEONE\_METHOD*
- *MSK\_IPAR\_SIM\_REFACTOR\_FREQ*
- *MSK\_IPAR\_SIM\_REFORMULATION*
- *MSK\_IPAR\_SIM\_SAVE\_LU*
- *MSK\_IPAR\_SIM\_SCALING*
- *MSK\_IPAR\_SIM\_SCALING\_METHOD*
- *MSK\_IPAR\_SIM\_SEED*
- *MSK\_IPAR\_SIM\_SOLVE\_FORM*
- *MSK\_IPAR\_SIM\_STABILITY\_PRIORITY*
- *MSK\_IPAR\_SIM\_SWITCH\_OPTIMIZER*

#### **Solution input/output**

- *MSK\_IPAR\_INFEAS\_REPORT\_AUTO*
- *MSK\_IPAR\_SOL\_FILTER\_KEEP\_BASIC*
- *MSK\_IPAR\_SOL\_FILTER\_KEEP\_RANGED*
- *MSK\_IPAR\_SOL\_READ\_NAME\_WIDTH*
- *MSK\_IPAR\_SOL\_READ\_WIDTH*
- *MSK\_IPAR\_WRITE\_BAS\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_BAS\_HEAD*
- *MSK\_IPAR\_WRITE\_BAS\_VARIABLES*
- *MSK\_IPAR\_WRITE\_INT\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_INT\_HEAD*
- *MSK\_IPAR\_WRITE\_INT\_VARIABLES*
- *MSK\_IPAR\_WRITE\_SOL\_BARVARIABLES*
- *MSK\_IPAR\_WRITE\_SOL\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_SOL\_HEAD*
- *MSK\_IPAR\_WRITE\_SOL\_IGNORE\_INVALID\_NAMES*
- *MSK\_IPAR\_WRITE\_SOL\_VARIABLES*
- *MSK\_SPAR\_BAS\_SOL\_FILE\_NAME*

- *MSK\_SPAR\_INT\_SOL\_FILE\_NAME*
- *MSK\_SPAR\_ITR\_SOL\_FILE\_NAME*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_UPR*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_UPR*

### Termination criteria

- *MSK\_DPAR\_BASIS\_REL\_TOL\_S*
- *MSK\_DPAR\_BASIS\_TOL\_S*
- *MSK\_DPAR\_BASIS\_TOL\_X*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_REL\_GAP*
- *MSK\_DPAR\_LOWER\_OBJ\_CUT*
- *MSK\_DPAR\_LOWER\_OBJ\_CUT\_FINITE\_TRH*
- *MSK\_DPAR\_MIO\_MAX\_TIME*
- *MSK\_DPAR\_MIO\_REL\_GAP\_CONST*
- *MSK\_DPAR\_MIO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_OPTIMIZER\_MAX\_TIME*
- *MSK\_DPAR\_UPPER\_OBJ\_CUT*
- *MSK\_DPAR\_UPPER\_OBJ\_CUT\_FINITE\_TRH*









































**Default** -1  
**Accepted** [-1; 2]  
**Example** param.MSK\_IPAR\_MIO\_FEASPUMP\_LEVEL = -1  
**Groups** *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_HEURISTIC\_LEVEL

Controls the heuristic employed by the mixed-integer optimizer to locate an initial good integer feasible solution. A value of zero means the heuristic is not used at all. A larger value than 0 means that a gradually more sophisticated heuristic is used which is computationally more expensive. A negative value implies that the optimizer chooses the heuristic. Normally a value around 3 to 5 should be optimal.

**Default** -1  
**Accepted** [-inf; +inf]  
**Example** param.MSK\_IPAR\_MIO\_HEURISTIC\_LEVEL = -1  
**Groups** *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_MAX\_NUM\_BRANCHES

Maximum number of branches allowed during the branch and bound search. A negative value means infinite.

**Default** -1  
**Accepted** [-inf; +inf]  
**Example** param.MSK\_IPAR\_MIO\_MAX\_NUM\_BRANCHES = -1  
**Groups** *Mixed-integer optimization, Termination criteria*

#### MSK\_IPAR\_MIO\_MAX\_NUM\_RELAXS

Maximum number of relaxations allowed during the branch and bound search. A negative value means infinite.

**Default** -1  
**Accepted** [-inf; +inf]  
**Example** param.MSK\_IPAR\_MIO\_MAX\_NUM\_RELAXS = -1  
**Groups** *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_MAX\_NUM\_ROOT\_CUT\_ROUNDS

Maximum number of cut separation rounds at the root node.

**Default** 100  
**Accepted** [0; +inf]  
**Example** param.MSK\_IPAR\_MIO\_MAX\_NUM\_ROOT\_CUT\_ROUNDS = 100  
**Groups** *Mixed-integer optimization, Termination criteria*

#### MSK\_IPAR\_MIO\_MAX\_NUM\_SOLUTIONS

The mixed-integer optimizer can be terminated after a certain number of different feasible solutions has been located. If this parameter has the value  $n > 0$ , then the mixed-integer optimizer will be terminated when  $n$  feasible solutions have been located.

**Default** -1  
**Accepted** [-inf; +inf]  
**Example** param.MSK\_IPAR\_MIO\_MAX\_NUM\_SOLUTIONS = -1  
**Groups** *Mixed-integer optimization, Termination criteria*

#### MSK\_IPAR\_MIO\_MODE

Controls whether the optimizer includes the integer restrictions when solving a (mixed) integer optimization problem.

**Default** *"SATISFIED"*  
**Accepted** *"IGNORED", "SATISFIED"*









































"MSK\_RES\_WRN\_LP\_DROP\_VARIABLE" (85)  
 Ignored a variable because the variable was not previously defined. Usually this implies that a variable appears in the bound section but not in the objective or the constraints.

"MSK\_RES\_WRN\_NZ\_IN\_UPR\_TRI" (200)  
 Non-zero elements specified in the upper triangle of a matrix were ignored.

"MSK\_RES\_WRN\_DROPPED\_NZ\_QOBJ" (201)  
 One or more non-zero elements were dropped in the Q matrix in the objective.

"MSK\_RES\_WRN\_IGNORE\_INTEGER" (250)  
 Ignored integer constraints.

"MSK\_RES\_WRN\_NO\_GLOBAL\_OPTIMIZER" (251)  
 No global optimizer is available.

"MSK\_RES\_WRN\_MIO\_INFEASIBLE\_FINAL" (270)  
 The final mixed-integer problem with all the integer variables fixed at their optimal values is infeasible.

"MSK\_RES\_WRN\_SOL\_FILTER" (300)  
 Invalid solution filter is specified.

"MSK\_RES\_WRN\_UNDEF\_SOL\_FILE\_NAME" (350)  
 Undefined name occurred in a solution.

"MSK\_RES\_WRN\_SOL\_FILE\_IGNORED\_CON" (351)  
 One or more lines in the constraint section were ignored when reading a solution file.

"MSK\_RES\_WRN\_SOL\_FILE\_IGNORED\_VAR" (352)  
 One or more lines in the variable section were ignored when reading a solution file.

"MSK\_RES\_WRN\_TOO\_FEW\_BASIS\_VARS" (400)  
 An incomplete basis has been specified. Too few basis variables are specified.

"MSK\_RES\_WRN\_TOO\_MANY\_BASIS\_VARS" (405)  
 A basis with too many variables has been specified.

"MSK\_RES\_WRN\_LICENSE\_EXPIRE" (500)  
 The license expires.

"MSK\_RES\_WRN\_LICENSE\_SERVER" (501)  
 The license server is not responding.

"MSK\_RES\_WRN\_EMPTY\_NAME" (502)  
 A variable or constraint name is empty. The output file may be invalid.

"MSK\_RES\_WRN\_USING\_GENERIC\_NAMES" (503)  
 Generic names are used because a name is not valid. For instance when writing an LP file the names must not contain blanks or start with a digit.

"MSK\_RES\_WRN\_LICENSE\_FEATURE\_EXPIRE" (505)  
 The license expires.

"MSK\_RES\_WRN\_PARAM\_NAME\_DOU" (510)  
 The parameter name is not recognized as a double parameter.

"MSK\_RES\_WRN\_PARAM\_NAME\_INT" (511)  
 The parameter name is not recognized as an integer parameter.

"MSK\_RES\_WRN\_PARAM\_NAME\_STR" (512)  
 The parameter name is not recognized as a string parameter.

"MSK\_RES\_WRN\_PARAM\_STR\_VALUE" (515)  
 The string is not recognized as a symbolic value for the parameter.

"MSK\_RES\_WRN\_PARAM\_IGNORED\_CMIO" (516)  
 A parameter was ignored by the conic mixed integer optimizer.

"MSK\_RES\_WRN\_ZEROS\_IN\_SPARSE\_ROW" (705)  
 One or more (near) zero elements are specified in a sparse row of a matrix. Since, it is redundant to specify zero elements then it may indicate an error.

"MSK\_RES\_WRN\_ZEROS\_IN\_SPARSE\_COL" (710)  
 One or more (near) zero elements are specified in a sparse column of a matrix. It is redundant to specify zero elements. Hence, it may indicate an error.

"MSK\_RES\_WRN\_INCOMPLETE\_LINEAR\_DEPENDENCY\_CHECK" (800)  
 The linear dependency check(s) is incomplete. Normally this is not an important warning unless the optimization problem has been formulated with linear dependencies. Linear dependencies may prevent **MOSEK** from solving the problem.





"MSK\_RES\_ERR\_OLDER\_DLL" (1035)  
The dynamic link library is older than the specified version.

"MSK\_RES\_ERR\_NEWER\_DLL" (1036)  
The dynamic link library is newer than the specified version.

"MSK\_RES\_ERR\_LINK\_FILE\_DLL" (1040)  
A file cannot be linked to a stream in the DLL version.

"MSK\_RES\_ERR\_THREAD\_MUTEX\_INIT" (1045)  
Could not initialize a mutex.

"MSK\_RES\_ERR\_THREAD\_MUTEX\_LOCK" (1046)  
Could not lock a mutex.

"MSK\_RES\_ERR\_THREAD\_MUTEX\_UNLOCK" (1047)  
Could not unlock a mutex.

"MSK\_RES\_ERR\_THREAD\_CREATE" (1048)  
Could not create a thread. This error may occur if a large number of environments are created and not deleted again. In any case it is a good practice to minimize the number of environments created.

"MSK\_RES\_ERR\_THREAD\_COND\_INIT" (1049)  
Could not initialize a condition.

"MSK\_RES\_ERR\_UNKNOWN" (1050)  
Unknown error.

"MSK\_RES\_ERR\_SPACE" (1051)  
Out of space.

"MSK\_RES\_ERR\_FILE\_OPEN" (1052)  
Error while opening a file.

"MSK\_RES\_ERR\_FILE\_READ" (1053)  
File read error.

"MSK\_RES\_ERR\_FILE\_WRITE" (1054)  
File write error.

"MSK\_RES\_ERR\_DATA\_FILE\_EXT" (1055)  
The data file format cannot be determined from the file name.

"MSK\_RES\_ERR\_INVALID\_FILE\_NAME" (1056)  
An invalid file name has been specified.

"MSK\_RES\_ERR\_INVALID\_SOL\_FILE\_NAME" (1057)  
An invalid file name has been specified.

"MSK\_RES\_ERR\_END\_OF\_FILE" (1059)  
End of file reached.

"MSK\_RES\_ERR\_NULL\_ENV" (1060)  
`env` is a NULL pointer.

"MSK\_RES\_ERR\_NULL\_TASK" (1061)  
`task` is a NULL pointer.

"MSK\_RES\_ERR\_INVALID\_STREAM" (1062)  
An invalid stream is referenced.

"MSK\_RES\_ERR\_NO\_INIT\_ENV" (1063)  
`env` is not initialized.

"MSK\_RES\_ERR\_INVALID\_TASK" (1064)  
The `task` is invalid.

"MSK\_RES\_ERR\_NULL\_POINTER" (1065)  
An argument to a function is unexpectedly a NULL pointer.

"MSK\_RES\_ERR\_LIVING\_TASKS" (1066)  
All tasks associated with an environment must be deleted before the environment is deleted. There are still some undeleted tasks.

"MSK\_RES\_ERR\_BLANK\_NAME" (1070)  
An all blank name has been specified.

"MSK\_RES\_ERR\_DUP\_NAME" (1071)  
The same name was used multiple times for the same problem item type.

"MSK\_RES\_ERR\_FORMAT\_STRING" (1072)  
The name format string is invalid.

"MSK\_RES\_ERR\_INVALID\_OBJ\_NAME" (1075)  
An invalid objective name is specified.

"MSK\_RES\_ERR\_INVALID\_CON\_NAME" (1076)  
An invalid constraint name is used.

"MSK\_RES\_ERR\_INVALID\_VAR\_NAME" (1077)  
An invalid variable name is used.

"MSK\_RES\_ERR\_INVALID\_CONE\_NAME" (1078)  
An invalid cone name is used.

"MSK\_RES\_ERR\_INVALID\_BARVAR\_NAME" (1079)  
An invalid symmetric matrix variable name is used.

"MSK\_RES\_ERR\_SPACE\_LEAKING" (1080)  
**MOSEK** is leaking memory. This can be due to either an incorrect use of **MOSEK** or a bug.

"MSK\_RES\_ERR\_SPACE\_NO\_INFO" (1081)  
No available information about the space usage.

"MSK\_RES\_ERR\_READ\_FORMAT" (1090)  
The specified format cannot be read.

"MSK\_RES\_ERR\_MPS\_FILE" (1100)  
An error occurred while reading an MPS file.

"MSK\_RES\_ERR\_MPS\_INV\_FIELD" (1101)  
A field in the MPS file is invalid. Probably it is too wide.

"MSK\_RES\_ERR\_MPS\_INV\_MARKER" (1102)  
An invalid marker has been specified in the MPS file.

"MSK\_RES\_ERR\_MPS\_NULL\_CON\_NAME" (1103)  
An empty constraint name is used in an MPS file.

"MSK\_RES\_ERR\_MPS\_NULL\_VAR\_NAME" (1104)  
An empty variable name is used in an MPS file.

"MSK\_RES\_ERR\_MPS\_UNDEF\_CON\_NAME" (1105)  
An undefined constraint name occurred in an MPS file.

"MSK\_RES\_ERR\_MPS\_UNDEF\_VAR\_NAME" (1106)  
An undefined variable name occurred in an MPS file.

"MSK\_RES\_ERR\_MPS\_INV\_CON\_KEY" (1107)  
An invalid constraint key occurred in an MPS file.

"MSK\_RES\_ERR\_MPS\_INV\_BOUND\_KEY" (1108)  
An invalid bound key occurred in an MPS file.

"MSK\_RES\_ERR\_MPS\_INV\_SEC\_NAME" (1109)  
An invalid section name occurred in an MPS file.

"MSK\_RES\_ERR\_MPS\_NO\_OBJECTIVE" (1110)  
No objective is defined in an MPS file.

"MSK\_RES\_ERR\_MPS\_SPLITTED\_VAR" (1111)  
All elements in a column of the  $A$  matrix must be specified consecutively. Hence, it is illegal to specify non-zero elements in  $A$  for variable 1, then for variable 2 and then variable 1 again.

"MSK\_RES\_ERR\_MPS\_MUL\_CON\_NAME" (1112)  
A constraint name was specified multiple times in the ROWS section.

"MSK\_RES\_ERR\_MPS\_MUL\_QSEC" (1113)  
Multiple QSECTIONS are specified for a constraint in the MPS data file.

"MSK\_RES\_ERR\_MPS\_MUL\_QOBJ" (1114)  
The Q term in the objective is specified multiple times in the MPS data file.

"MSK\_RES\_ERR\_MPS\_INV\_SEC\_ORDER" (1115)  
The sections in the MPS data file are not in the correct order.

"MSK\_RES\_ERR\_MPS\_MUL\_CSEC" (1116)  
Multiple CSECTIONs are given the same name.

"MSK\_RES\_ERR\_MPS\_CONE\_TYPE" (1117)  
Invalid cone type specified in a CSECTION.

"MSK\_RES\_ERR\_MPS\_CONE\_OVERLAP" (1118)  
A variable is specified to be a member of several cones.

"MSK\_RES\_ERR\_MPS\_CONE\_REPEAT" (1119)  
A variable is repeated within the CSECTION.

"MSK\_RES\_ERR\_MPS\_NON\_SYMMETRIC\_Q" (1120)  
A non symmetric matrix has been speciefied.

"MSK\_RES\_ERR\_MPS\_DUPLICATE\_Q\_ELEMENT" (1121)  
Duplicate elements is specfied in a  $Q$  matrix.

"MSK\_RES\_ERR\_MPS\_INVALID\_OBJSENSE" (1122)  
An invalid objective sense is specified.

"MSK\_RES\_ERR\_MPS\_TAB\_IN\_FIELD2" (1125)  
A tab char occurred in field 2.

"MSK\_RES\_ERR\_MPS\_TAB\_IN\_FIELD3" (1126)  
A tab char occurred in field 3.

"MSK\_RES\_ERR\_MPS\_TAB\_IN\_FIELD5" (1127)  
A tab char occurred in field 5.

"MSK\_RES\_ERR\_MPS\_INVALID\_OBJ\_NAME" (1128)  
An invalid objective name is specified.

"MSK\_RES\_ERR\_LP\_INCOMPATIBLE" (1150)  
The problem cannot be written to an LP formatted file.

"MSK\_RES\_ERR\_LP\_EMPTY" (1151)  
The problem cannot be written to an LP formatted file.

"MSK\_RES\_ERR\_LP\_DUP\_SLACK\_NAME" (1152)  
The name of the slack variable added to a ranged constraint already exists.

"MSK\_RES\_ERR\_WRITE\_MPS\_INVALID\_NAME" (1153)  
An invalid name is created while writing an MPS file. Usually this will make the MPS file unreadable.

"MSK\_RES\_ERR\_LP\_INVALID\_VAR\_NAME" (1154)  
A variable name is invalid when used in an LP formatted file.

"MSK\_RES\_ERR\_LP\_FREE\_CONSTRAINT" (1155)  
Free constraints cannot be written in LP file format.

"MSK\_RES\_ERR\_WRITE\_OPF\_INVALID\_VAR\_NAME" (1156)  
Empty variable names cannot be written to OPF files.

"MSK\_RES\_ERR\_LP\_FILE\_FORMAT" (1157)  
Syntax error in an LP file.

"MSK\_RES\_ERR\_WRITE\_LP\_FORMAT" (1158)  
Problem cannot be written as an LP file.

"MSK\_RES\_ERR\_READ\_LP\_MISSING\_END\_TAG" (1159)  
Syntax error in LP file. Possibly missing End tag.

"MSK\_RES\_ERR\_LP\_FORMAT" (1160)  
Syntax error in an LP file.

"MSK\_RES\_ERR\_WRITE\_LP\_NON\_UNIQUE\_NAME" (1161)  
An auto-generated name is not unique.

"MSK\_RES\_ERR\_READ\_LP\_NONEXISTING\_NAME" (1162)  
A variable never occurred in objective or constraints.

"MSK\_RES\_ERR\_LP\_WRITE\_CONIC\_PROBLEM" (1163)  
The problem contains cones that cannot be written to an LP formatted file.

"MSK\_RES\_ERR\_LP\_WRITE\_GECO\_PROBLEM" (1164)  
The problem contains general convex terms that cannot be written to an LP formatted file.

"MSK\_RES\_ERR\_WRITING\_FILE" (1166)  
An error occurred while writing file

"MSK\_RES\_ERR\_PTF\_FORMAT" (1167)  
Syntax error in an PTF file

"MSK\_RES\_ERR\_OPF\_FORMAT" (1168)  
Syntax error in an OPF file

"MSK\_RES\_ERR\_OPF\_NEW\_VARIABLE" (1169)  
Introducing new variables is now allowed. When a [variables] section is present, it is not allowed to introduce new variables later in the problem.

"MSK\_RES\_ERR\_INVALID\_NAME\_IN\_SOL\_FILE" (1170)  
An invalid name occurred in a solution file.

"MSK\_RES\_ERR\_LP\_INVALID\_CON\_NAME" (1171)  
A constraint name is invalid when used in an LP formatted file.

"MSK\_RES\_ERR\_OPF\_PREMATURE\_EOF" (1172)  
Premature end of file in an OPF file.

"MSK\_RES\_ERR\_JSON\_SYNTAX" (1175)  
Syntax error in an JSON data

"MSK\_RES\_ERR\_JSON\_STRING" (1176)  
Error in JSON string.

"MSK\_RES\_ERR\_JSON\_NUMBER\_OVERFLOW" (1177)  
Invalid number entry - wrong type or value overflow.

"MSK\_RES\_ERR\_JSON\_FORMAT" (1178)  
Error in an JSON Task file

"MSK\_RES\_ERR\_JSON\_DATA" (1179)  
Inconsistent data in JSON Task file

"MSK\_RES\_ERR\_JSON\_MISSING\_DATA" (1180)  
Missing data section in JSON task file.

"MSK\_RES\_ERR\_ARGUMENT\_LENNEQ" (1197)  
Incorrect length of arguments.

"MSK\_RES\_ERR\_ARGUMENT\_TYPE" (1198)  
Incorrect argument type.

"MSK\_RES\_ERR\_NUM\_ARGUMENTS" (1199)  
Incorrect number of function arguments.

"MSK\_RES\_ERR\_IN\_ARGUMENT" (1200)  
A function argument is incorrect.

"MSK\_RES\_ERR\_ARGUMENT\_DIMENSION" (1201)  
A function argument is of incorrect dimension.

"MSK\_RES\_ERR\_SHAPE\_IS\_TOO\_LARGE" (1202)  
The size of the n-dimensional shape is too large.

"MSK\_RES\_ERR\_INDEX\_IS\_TOO\_SMALL" (1203)  
An index in an argument is too small.

"MSK\_RES\_ERR\_INDEX\_IS\_TOO\_LARGE" (1204)  
An index in an argument is too large.

"MSK\_RES\_ERR\_PARAM\_NAME" (1205)  
The parameter name is not correct.

"MSK\_RES\_ERR\_PARAM\_NAME\_DOU" (1206)  
The parameter name is not correct for a double parameter.

"MSK\_RES\_ERR\_PARAM\_NAME\_INT" (1207)  
The parameter name is not correct for an integer parameter.

"MSK\_RES\_ERR\_PARAM\_NAME\_STR" (1208)  
The parameter name is not correct for a string parameter.

"MSK\_RES\_ERR\_PARAM\_INDEX" (1210)  
Parameter index is out of range.

"MSK\_RES\_ERR\_PARAM\_IS\_TOO\_LARGE" (1215)  
The parameter value is too large.

"MSK\_RES\_ERR\_PARAM\_IS\_TOO\_SMALL" (1216)  
The parameter value is too small.

"MSK\_RES\_ERR\_PARAM\_VALUE\_STR" (1217)  
The parameter value string is incorrect.

"MSK\_RES\_ERR\_PARAM\_TYPE" (1218)  
The parameter type is invalid.

"MSK\_RES\_ERR\_INF\_DOU\_INDEX" (1219)  
A double information index is out of range for the specified type.

"MSK\_RES\_ERR\_INF\_INT\_INDEX" (1220)  
An integer information index is out of range for the specified type.

"MSK\_RES\_ERR\_INDEX\_ARR\_IS\_TOO\_SMALL" (1221)  
An index in an array argument is too small.

"MSK\_RES\_ERR\_INDEX\_ARR\_IS\_TOO\_LARGE" (1222)  
An index in an array argument is too large.

"MSK\_RES\_ERR\_INF\_LINT\_INDEX" (1225)  
A long integer information index is out of range for the specified type.







"MSK\_RES\_ERR\_INFINITY\_BOUND" (1400)  
 A numerically huge bound value is specified.

"MSK\_RES\_ERR\_INV\_QOBJ\_SUBI" (1401)  
 Invalid value in qosubi.

"MSK\_RES\_ERR\_INV\_QOBJ\_SUBJ" (1402)  
 Invalid value in qosubj.

"MSK\_RES\_ERR\_INV\_QOBJ\_VAL" (1403)  
 Invalid value in qoval.

"MSK\_RES\_ERR\_INV\_QCON\_SUBK" (1404)  
 Invalid value in qcsubk.

"MSK\_RES\_ERR\_INV\_QCON\_SUBI" (1405)  
 Invalid value in qcsubi.

"MSK\_RES\_ERR\_INV\_QCON\_SUBJ" (1406)  
 Invalid value in qcsubj.

"MSK\_RES\_ERR\_INV\_QCON\_VAL" (1407)  
 Invalid value in qcval.

"MSK\_RES\_ERR\_QCON\_SUBI\_TOO\_SMALL" (1408)  
 Invalid value in qcsubi.

"MSK\_RES\_ERR\_QCON\_SUBI\_TOO\_LARGE" (1409)  
 Invalid value in qcsubi.

"MSK\_RES\_ERR\_QOBJ\_UPPER\_TRIANGLE" (1415)  
 An element in the upper triangle of  $Q^o$  is specified. Only elements in the lower triangle should be specified.

"MSK\_RES\_ERR\_QCON\_UPPER\_TRIANGLE" (1417)  
 An element in the upper triangle of a  $Q^k$  is specified. Only elements in the lower triangle should be specified.

"MSK\_RES\_ERR\_FIXED\_BOUND\_VALUES" (1420)  
 A fixed constraint/variable has been specified using the bound keys but the numerical value of the lower and upper bound is different.

"MSK\_RES\_ERR\_TOO\_SMALL\_A\_TRUNCATION\_VALUE" (1421)  
 A too small value for the A truncation value is specified.

"MSK\_RES\_ERR\_INVALID\_OBJECTIVE\_SENSE" (1445)  
 An invalid objective sense is specified.

"MSK\_RES\_ERR\_UNDEFINED\_OBJECTIVE\_SENSE" (1446)  
 The objective sense has not been specified before the optimization.

"MSK\_RES\_ERR\_Y\_IS\_UNDEFINED" (1449)  
 The solution item  $y$  is undefined.

"MSK\_RES\_ERR\_NAN\_IN\_DOUBLE\_DATA" (1450)  
 An invalid floating point value was used in some double data.

"MSK\_RES\_ERR\_NAN\_IN\_BLC" (1461)  
 $l^c$  contains an invalid floating point value, i.e. a NaN.

"MSK\_RES\_ERR\_NAN\_IN\_BUC" (1462)  
 $u^c$  contains an invalid floating point value, i.e. a NaN.

"MSK\_RES\_ERR\_NAN\_IN\_C" (1470)  
 $c$  contains an invalid floating point value, i.e. a NaN.

"MSK\_RES\_ERR\_NAN\_IN\_BLX" (1471)  
 $l^x$  contains an invalid floating point value, i.e. a NaN.

"MSK\_RES\_ERR\_NAN\_IN\_BUX" (1472)  
 $u^x$  contains an invalid floating point value, i.e. a NaN.

"MSK\_RES\_ERR\_INVALID\_AIJ" (1473)  
 $a_{i,j}$  contains an invalid floating point value, i.e. a NaN or an infinite value.

"MSK\_RES\_ERR\_INVALID\_CJ" (1474)  
 $c_j$  contains an invalid floating point value, i.e. a NaN or an infinite value.

"MSK\_RES\_ERR\_SYM\_MAT\_INVALID" (1480)  
 A symmetric matrix contains an invalid floating point value, i.e. a NaN or an infinite value.

"MSK\_RES\_ERR\_SYM\_MAT\_HUGE" (1482)  
 A symmetric matrix contains a huge value in absolute size. The parameter `MSK_DPAR_DATA_SYM_MAT_TOL_HUGE` controls when an  $e_{i,j}$  is considered huge.

"MSK\_RES\_ERR\_INV\_PROBLEM" (1500)  
Invalid problem type. Probably a nonconvex problem has been specified.

"MSK\_RES\_ERR\_MIXED\_CONIC\_AND\_NL" (1501)  
The problem contains nonlinear terms conic constraints. The requested operation cannot be applied to this type of problem.

"MSK\_RES\_ERR\_GLOBAL\_INV\_CONIC\_PROBLEM" (1503)  
The global optimizer can only be applied to problems without semidefinite variables.

"MSK\_RES\_ERR\_INV\_OPTIMIZER" (1550)  
An invalid optimizer has been chosen for the problem.

"MSK\_RES\_ERR\_MIO\_NO\_OPTIMIZER" (1551)  
No optimizer is available for the current class of integer optimization problems.

"MSK\_RES\_ERR\_NO\_OPTIMIZER\_VAR\_TYPE" (1552)  
No optimizer is available for this class of optimization problems.

"MSK\_RES\_ERR\_FINAL\_SOLUTION" (1560)  
An error occurred during the solution finalization.

"MSK\_RES\_ERR\_FIRST" (1570)  
Invalid `first`.

"MSK\_RES\_ERR\_LAST" (1571)  
Invalid index `last`. A given index was out of expected range.

"MSK\_RES\_ERR\_SLICE\_SIZE" (1572)  
Invalid slice size specified.

"MSK\_RES\_ERR\_NEGATIVE\_SURPLUS" (1573)  
Negative surplus.

"MSK\_RES\_ERR\_NEGATIVE\_APPEND" (1578)  
Cannot append a negative number.

"MSK\_RES\_ERR\_POSTSOLVE" (1580)  
An error occurred during the postsolve. Please contact **MOSEK** support.

"MSK\_RES\_ERR\_OVERFLOW" (1590)  
A computation produced an overflow i.e. a very large number.

"MSK\_RES\_ERR\_NO\_BASIS\_SOL" (1600)  
No basic solution is defined.

"MSK\_RES\_ERR\_BASIS\_FACTOR" (1610)  
The factorization of the basis is invalid.

"MSK\_RES\_ERR\_BASIS\_SINGULAR" (1615)  
The basis is singular and hence cannot be factored.

"MSK\_RES\_ERR\_FACTOR" (1650)  
An error occurred while factorizing a matrix.

"MSK\_RES\_ERR\_FEASREPAIR\_CANNOT\_RELAX" (1700)  
An optimization problem cannot be relaxed.

"MSK\_RES\_ERR\_FEASREPAIR\_SOLVING\_RELAXED" (1701)  
The relaxed problem could not be solved to optimality. Please consult the log file for further details.

"MSK\_RES\_ERR\_FEASREPAIR\_INCONSISTENT\_BOUND" (1702)  
The upper bound is less than the lower bound for a variable or a constraint. Please correct this before running the feasibility repair.

"MSK\_RES\_ERR\_REPAIR\_INVALID\_PROBLEM" (1710)  
The feasibility repair does not support the specified problem type.

"MSK\_RES\_ERR\_REPAIR\_OPTIMIZATION\_FAILED" (1711)  
Computation the optimal relaxation failed. The cause may have been numerical problems.

"MSK\_RES\_ERR\_NAME\_MAX\_LEN" (1750)  
A name is longer than the buffer that is supposed to hold it.

"MSK\_RES\_ERR\_NAME\_IS\_NULL" (1760)  
The name buffer is a `NULL` pointer.

"MSK\_RES\_ERR\_INVALID\_COMPRESSION" (1800)  
Invalid compression type.

"MSK\_RES\_ERR\_INVALID\_IOMODE" (1801)  
Invalid io mode.

"MSK\_RES\_ERR\_NO\_PRIMAL\_INFEAS\_CER" (2000)  
A certificate of primal infeasibility is not available.

"MSK\_RES\_ERR\_NO\_DUAL\_INFEAS\_CER" (2001)  
 A certificate of infeasibility is not available.

"MSK\_RES\_ERR\_NO\_SOLUTION\_IN\_CALLBACK" (2500)  
 The required solution is not available.

"MSK\_RES\_ERR\_INV\_MARKI" (2501)  
 Invalid value in marki.

"MSK\_RES\_ERR\_INV\_MARKJ" (2502)  
 Invalid value in markj.

"MSK\_RES\_ERR\_INV\_NUMI" (2503)  
 Invalid numi.

"MSK\_RES\_ERR\_INV\_NUMJ" (2504)  
 Invalid numj.

"MSK\_RES\_ERR\_TASK\_INCOMPATIBLE" (2560)  
 The Task file is incompatible with this platform. This results from reading a file on a 32 bit platform generated on a 64 bit platform.

"MSK\_RES\_ERR\_TASK\_INVALID" (2561)  
 The Task file is invalid.

"MSK\_RES\_ERR\_TASK\_WRITE" (2562)  
 Failed to write the task file.

"MSK\_RES\_ERR\_LU\_MAX\_NUM\_TRIES" (2800)  
 Could not compute the LU factors of the matrix within the maximum number of allowed tries.

"MSK\_RES\_ERR\_INVALID\_UTF8" (2900)  
 An invalid UTF8 string is encountered.

"MSK\_RES\_ERR\_INVALID\_WCHAR" (2901)  
 An invalid wchar string is encountered.

"MSK\_RES\_ERR\_NO\_DUAL\_FOR\_ITG\_SOL" (2950)  
 No dual information is available for the integer solution.

"MSK\_RES\_ERR\_NO\_SNX\_FOR\_BAS\_SOL" (2953)  
 $s_n^x$  is not available for the basis solution.

"MSK\_RES\_ERR\_INTERNAL" (3000)  
 An internal error occurred. Please report this problem.

"MSK\_RES\_ERR\_API\_ARRAY\_TOO\_SMALL" (3001)  
 An input array was too short.

"MSK\_RES\_ERR\_API\_CB\_CONNECT" (3002)  
 Failed to connect a callback object.

"MSK\_RES\_ERR\_API\_FATAL\_ERROR" (3005)  
 An internal error occurred in the API. Please report this problem.

"MSK\_RES\_ERR\_API\_INTERNAL" (3999)  
 An internal fatal error occurred in an interface function.

"MSK\_RES\_ERR\_SEN\_FORMAT" (3050)  
 Syntax error in sensitivity analysis file.

"MSK\_RES\_ERR\_SEN\_UNDEF\_NAME" (3051)  
 An undefined name was encountered in the sensitivity analysis file.

"MSK\_RES\_ERR\_SEN\_INDEX\_RANGE" (3052)  
 Index out of range in the sensitivity analysis file.

"MSK\_RES\_ERR\_SEN\_BOUND\_INVALID\_UP" (3053)  
 Analysis of upper bound requested for an index, where no upper bound exists.

"MSK\_RES\_ERR\_SEN\_BOUND\_INVALID\_LO" (3054)  
 Analysis of lower bound requested for an index, where no lower bound exists.

"MSK\_RES\_ERR\_SEN\_INDEX\_INVALID" (3055)  
 Invalid range given in the sensitivity file.

"MSK\_RES\_ERR\_SEN\_INVALID\_REGEX" (3056)  
 Syntax error in regexp or regexp longer than 1024.

"MSK\_RES\_ERR\_SEN\_SOLUTION\_STATUS" (3057)  
 No optimal solution found to the original problem given for sensitivity analysis.

"MSK\_RES\_ERR\_SEN\_NUMERICAL" (3058)  
 Numerical difficulties encountered performing the sensitivity analysis.

"MSK\_RES\_ERR\_SEN\_UNHANDLED\_PROBLEM\_TYPE" (3080)  
Sensitivity analysis cannot be performed for the specified problem. Sensitivity analysis is only possible for linear problems.

"MSK\_RES\_ERR\_UNB\_STEP\_SIZE" (3100)  
A step size in an optimizer was unexpectedly unbounded. For instance, if the step-size becomes unbounded in phase 1 of the simplex algorithm then an error occurs. Normally this will happen only if the problem is badly formulated. Please contact **MOSEK** support if this error occurs.

"MSK\_RES\_ERR\_IDENTICAL\_TASKS" (3101)  
Some tasks related to this function call were identical. Unique tasks were expected.

"MSK\_RES\_ERR\_AD\_INVALID\_CODELIST" (3102)  
The code list data was invalid.

"MSK\_RES\_ERR\_INTERNAL\_TEST\_FAILED" (3500)  
An internal unit test function failed.

"MSK\_RES\_ERR\_XML\_INVALID\_PROBLEM\_TYPE" (3600)  
The problem type is not supported by the XML format.

"MSK\_RES\_ERR\_INVALID\_AMPL\_STUB" (3700)  
Invalid AMPL stub.

"MSK\_RES\_ERR\_INT64\_TO\_INT32\_CAST" (3800)  
A 64 bit integer could not be cast to a 32 bit integer.

"MSK\_RES\_ERR\_SIZE\_LICENSE\_NUMCORES" (3900)  
The computer contains more cpu cores than the license allows for.

"MSK\_RES\_ERR\_INFEAS\_UNDEFINED" (3910)  
The requested value is not defined for this solution type.

"MSK\_RES\_ERR\_NO\_BARX\_FOR\_SOLUTION" (3915)  
There is no  $\bar{X}$  available for the solution specified. In particular note there are no  $\bar{X}$  defined for the basic and integer solutions.

"MSK\_RES\_ERR\_NO\_BARS\_FOR\_SOLUTION" (3916)  
There is no  $\bar{s}$  available for the solution specified. In particular note there are no  $\bar{s}$  defined for the basic and integer solutions.

"MSK\_RES\_ERR\_BAR\_VAR\_DIM" (3920)  
The dimension of a symmetric matrix variable has to be greater than 0.

"MSK\_RES\_ERR\_SYM\_MAT\_INVALID\_ROW\_INDEX" (3940)  
A row index specified for sparse symmetric matrix is invalid.

"MSK\_RES\_ERR\_SYM\_MAT\_INVALID\_COL\_INDEX" (3941)  
A column index specified for sparse symmetric matrix is invalid.

"MSK\_RES\_ERR\_SYM\_MAT\_NOT\_LOWER\_TRINGULAR" (3942)  
Only the lower triangular part of sparse symmetric matrix should be specified.

"MSK\_RES\_ERR\_SYM\_MAT\_INVALID\_VALUE" (3943)  
The numerical value specified in a sparse symmetric matrix is not a floating point value.

"MSK\_RES\_ERR\_SYM\_MAT\_DUPLICATE" (3944)  
A value in a symmetric matrix has been specified more than once.

"MSK\_RES\_ERR\_INVALID\_SYM\_MAT\_DIM" (3950)  
A sparse symmetric matrix of invalid dimension is specified.

"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_SYM\_MAT" (4000)  
The file format does not support a problem with symmetric matrix variables.

"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_CFIX" (4001)  
The file format does not support a problem with nonzero fixed term in c.

"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_RANGED\_CONSTRAINTS" (4002)  
The file format does not support a problem with ranged constraints.

"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_FREE\_CONSTRAINTS" (4003)  
The file format does not support a problem with free constraints.

"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_CONES" (4005)  
The file format does not support a problem with conic constraints.

"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_NONLINEAR" (4010)  
The file format does not support a problem with nonlinear terms.

"MSK\_RES\_ERR\_DUPLICATE\_CONSTRAINT\_NAMES" (4500)  
Two constraint names are identical.

"MSK\_RES\_ERR\_DUPLICATE\_VARIABLE\_NAMES" (4501)  
Two variable names are identical.

"MSK\_RES\_ERR\_DUPLICATE\_BARVARIABLE\_NAMES" (4502)  
Two barvariable names are identical.

"MSK\_RES\_ERR\_DUPLICATE\_CONE\_NAMES" (4503)  
Two cone names are identical.

"MSK\_RES\_ERR\_NON\_UNIQUE\_ARRAY" (5000)  
An array does not contain unique elements.

"MSK\_RES\_ERR\_ARGUMENT\_IS\_TOO\_LARGE" (5005)  
The value of a function argument is too large.

"MSK\_RES\_ERR\_MIO\_INTERNAL" (5010)  
A fatal error occurred in the mixed integer optimizer. Please contact **MOSEK** support.

"MSK\_RES\_ERR\_INVALID\_PROBLEM\_TYPE" (6000)  
An invalid problem type.

"MSK\_RES\_ERR\_UNHANDLED\_SOLUTION\_STATUS" (6010)  
Unhandled solution status.

"MSK\_RES\_ERR\_UPPER\_TRIANGLE" (6020)  
An element in the upper triangle of a lower triangular matrix is specified.

"MSK\_RES\_ERR\_LAU\_SINGULAR\_MATRIX" (7000)  
A matrix is singular.

"MSK\_RES\_ERR\_LAU\_NOT\_POSITIVE\_DEFINITE" (7001)  
A matrix is not positive definite.

"MSK\_RES\_ERR\_LAU\_INVALID\_LOWER\_TRIANGULAR\_MATRIX" (7002)  
An invalid lower triangular matrix.

"MSK\_RES\_ERR\_LAU\_UNKNOWN" (7005)  
An unknown error.

"MSK\_RES\_ERR\_LAU\_ARG\_M" (7010)  
Invalid argument m.

"MSK\_RES\_ERR\_LAU\_ARG\_N" (7011)  
Invalid argument n.

"MSK\_RES\_ERR\_LAU\_ARG\_K" (7012)  
Invalid argument k.

"MSK\_RES\_ERR\_LAU\_ARG\_TRANSA" (7015)  
Invalid argument transa.

"MSK\_RES\_ERR\_LAU\_ARG\_TRANSB" (7016)  
Invalid argument transb.

"MSK\_RES\_ERR\_LAU\_ARG\_UPLO" (7017)  
Invalid argument uplo.

"MSK\_RES\_ERR\_LAU\_ARG\_TRANS" (7018)  
Invalid argument trans.

"MSK\_RES\_ERR\_LAU\_INVALID\_SPARSE\_SYMMETRIC\_MATRIX" (7019)  
An invalid sparse symmetric matrix is specified. Note only the lower triangular part with no duplicates is specified.

"MSK\_RES\_ERR\_CBF\_PARSE" (7100)  
An error occurred while parsing an CBF file.

"MSK\_RES\_ERR\_CBF\_OBJ\_SENSE" (7101)  
An invalid objective sense is specified.

"MSK\_RES\_ERR\_CBF\_NO\_VARIABLES" (7102)  
No variables are specified.

"MSK\_RES\_ERR\_CBF\_TOO\_MANY\_CONSTRAINTS" (7103)  
Too many constraints specified.

"MSK\_RES\_ERR\_CBF\_TOO\_MANY\_VARIABLES" (7104)  
Too many variables specified.

"MSK\_RES\_ERR\_CBF\_NO\_VERSION\_SPECIFIED" (7105)  
No version specified.

"MSK\_RES\_ERR\_CBF\_SYNTAX" (7106)  
Invalid syntax.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_OBJ" (7107)  
Duplicate OBJ keyword.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_CON" (7108)  
Duplicate CON keyword.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_VAR" (7109)  
Duplicate VAR keyword.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_INT" (7110)  
Duplicate INT keyword.

"MSK\_RES\_ERR\_CBF\_INVALID\_VAR\_TYPE" (7111)  
Invalid variable type.

"MSK\_RES\_ERR\_CBF\_INVALID\_CON\_TYPE" (7112)  
Invalid constraint type.

"MSK\_RES\_ERR\_CBF\_INVALID\_DOMAIN\_DIMENSION" (7113)  
Invalid domain dimension.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_OBJCOORD" (7114)  
Duplicate index in OBJCOORD.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_BCOORD" (7115)  
Duplicate index in BCOORD.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_ACOORD" (7116)  
Duplicate index in ACOORD.

"MSK\_RES\_ERR\_CBF\_TOO\_FEW\_VARIABLES" (7117)  
Too few variables defined.

"MSK\_RES\_ERR\_CBF\_TOO\_FEW\_CONSTRAINTS" (7118)  
Too few constraints defined.

"MSK\_RES\_ERR\_CBF\_TOO\_FEW\_INTS" (7119)  
Too few ints are specified.

"MSK\_RES\_ERR\_CBF\_TOO\_MANY\_INTS" (7120)  
Too many ints are specified.

"MSK\_RES\_ERR\_CBF\_INVALID\_INT\_INDEX" (7121)  
Invalid INT index.

"MSK\_RES\_ERR\_CBF\_UNSUPPORTED" (7122)  
Unsupported feature is present.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_PSDVAR" (7123)  
Duplicate PSDVAR keyword.

"MSK\_RES\_ERR\_CBF\_INVALID\_PSDVAR\_DIMENSION" (7124)  
Invalid PSDVAR dimension.

"MSK\_RES\_ERR\_CBF\_TOO\_FEW\_PSDVAR" (7125)  
Too few variables defined.

"MSK\_RES\_ERR\_CBF\_INVALID\_EXP\_DIMENSION" (7126)  
Invalid dimension of a exponential cone.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_POW\_CONES" (7130)  
Multiple POWCONES specified.

"MSK\_RES\_ERR\_CBF\_DUPLICATE\_POW\_STAR\_CONES" (7131)  
Multiple POW\*CONES specified.

"MSK\_RES\_ERR\_CBF\_INVALID\_POWER" (7132)  
Invalid power specified.

"MSK\_RES\_ERR\_CBF\_POWER\_CONE\_IS\_TOO\_LONG" (7133)  
Power cone is too long.

"MSK\_RES\_ERR\_CBF\_INVALID\_POWER\_CONE\_INDEX" (7134)  
Invalid power cone index.

"MSK\_RES\_ERR\_CBF\_INVALID\_POWER\_STAR\_CONE\_INDEX" (7135)  
Invalid power star cone index.

"MSK\_RES\_ERR\_CBF\_UNHANDLED\_POWER\_CONE\_TYPE" (7136)  
An unhandled power cone type.

"MSK\_RES\_ERR\_CBF\_UNHANDLED\_POWER\_STAR\_CONE\_TYPE" (7137)  
An unhandled power star cone type.

"MSK\_RES\_ERR\_CBF\_POWER\_CONE\_MISMATCH" (7138)  
The power cone does not match with it definition.

"MSK\_RES\_ERR\_CBF\_POWER\_STAR\_CONE\_MISMATCH" (7139)  
The power star cone does not match with its definition.

"MSK\_RES\_ERR\_CBF\_INVALID\_NUMBER\_OF\_CONES" (7740)  
Invalid number of cones.

"MSK\_RES\_ERR\_CBF\_INVALID\_DIMENSION\_OF\_CONES" (7741)  
Invalid dimension of cones.

"MSK\_RES\_ERR\_MIO\_INVALID\_ROOT\_OPTIMIZER" (7700)  
An invalid root optimizer was selected for the problem type.

"MSK\_RES\_ERR\_MIO\_INVALID\_NODE\_OPTIMIZER" (7701)  
An invalid node optimizer was selected for the problem type.

"MSK\_RES\_ERR\_TOCONIC\_CONSTR\_Q\_NOT\_PSD" (7800)  
The matrix defining the quadratic part of constraint is not positive semidefinite.

"MSK\_RES\_ERR\_TOCONIC\_CONSTRAINT\_FX" (7801)  
The quadratic constraint is an equality, thus not convex.

"MSK\_RES\_ERR\_TOCONIC\_CONSTRAINT\_RA" (7802)  
The quadratic constraint has finite lower and upper bound, and therefore it is not convex.

"MSK\_RES\_ERR\_TOCONIC\_CONSTR\_NOT\_CONIC" (7803)  
The constraint is not conic representable.

"MSK\_RES\_ERR\_TOCONIC\_OBJECTIVE\_NOT\_PSD" (7804)  
The matrix defining the quadratic part of the objective function is not positive semidefinite.

"MSK\_RES\_ERR\_SERVER\_CONNECT" (8000)  
Failed to connect to remote solver server. The server string or the port string were invalid, or the server did not accept connection.

"MSK\_RES\_ERR\_SERVER\_PROTOCOL" (8001)  
Unexpected message or data from solver server.

"MSK\_RES\_ERR\_SERVER\_STATUS" (8002)  
Server returned non-ok HTTP status code

"MSK\_RES\_ERR\_SERVER\_TOKEN" (8003)  
The job ID specified is incorrect or invalid

"MSK\_RES\_ERR\_SERVER\_PROBLEM\_SIZE" (8008)  
The size of the problem exceeds the dimensions permitted by the instance of the OptServer where it was run.

## 15.7 Enumerations

### basindtype

Basis identification

"MSK\_BI\_NEVER"

Never do basis identification.

"MSK\_BI\_ALWAYS"

Basis identification is always performed even if the interior-point optimizer terminates abnormally.

"MSK\_BI\_NO\_ERROR"

Basis identification is performed if the interior-point optimizer terminates without an error.

"MSK\_BI\_IF\_FEASIBLE"

Basis identification is not performed if the interior-point optimizer terminates with a problem status saying that the problem is primal or dual infeasible.

"MSK\_BI\_RESERVED"

Not currently in use.

### boundkey

Bound keys

"MSK\_BK\_LO"

The constraint or variable has a finite lower bound and an infinite upper bound.

"MSK\_BK\_UP"

The constraint or variable has an infinite lower bound and a finite upper bound.

"MSK\_BK\_FX"  
The constraint or variable is fixed.

"MSK\_BK\_FR"  
The constraint or variable is free.

"MSK\_BK\_RA"  
The constraint or variable is ranged.

**mark**  
Mark

"MSK\_MARK\_LO"  
The lower bound is selected for sensitivity analysis.

"MSK\_MARK\_UP"  
The upper bound is selected for sensitivity analysis.

**simdegen**  
Degeneracy strategies

"MSK\_SIM\_DEGEN\_NONE"  
The simplex optimizer should use no degeneration strategy.

"MSK\_SIM\_DEGEN\_FREE"  
The simplex optimizer chooses the degeneration strategy.

"MSK\_SIM\_DEGEN\_AGGRESSIVE"  
The simplex optimizer should use an aggressive degeneration strategy.

"MSK\_SIM\_DEGEN\_MODERATE"  
The simplex optimizer should use a moderate degeneration strategy.

"MSK\_SIM\_DEGEN\_MINIMUM"  
The simplex optimizer should use a minimum degeneration strategy.

**transpose**  
Transposed matrix.

"MSK\_TRANSPOSE\_NO"  
No transpose is applied.

"MSK\_TRANSPOSE\_YES"  
A transpose is applied.

**uplo**  
Triangular part of a symmetric matrix.

"MSK\_UPLO\_LO"  
Lower part.

"MSK\_UPLO\_UP"  
Upper part.

**simreform**  
Problem reformulation.

"MSK\_SIM\_REFORMULATION\_ON"  
Allow the simplex optimizer to reformulate the problem.

"MSK\_SIM\_REFORMULATION\_OFF"  
Disallow the simplex optimizer to reformulate the problem.

"MSK\_SIM\_REFORMULATION\_FREE"  
The simplex optimizer can choose freely.

"MSK\_SIM\_REFORMULATION\_AGGRESSIVE"  
The simplex optimizer should use an aggressive reformulation strategy.

**simdupvec**  
Exploit duplicate columns.

"MSK\_SIM\_EXPLOIT\_DUPVEC\_ON"  
Allow the simplex optimizer to exploit duplicated columns.

"MSK\_SIM\_EXPLOIT\_DUPVEC\_OFF"  
Disallow the simplex optimizer to exploit duplicated columns.

"MSK\_SIM\_EXPLOIT\_DUPVEC\_FREE"  
The simplex optimizer can choose freely.

**simhotstart**  
Hot-start type employed by the simplex optimizer

"MSK\_SIM\_HOTSTART\_NONE"  
The simplex optimizer performs a coldstart.

"MSK\_SIM\_HOTSTART\_FREE"  
The simplex optimizer chooses the hot-start type.

"MSK\_SIM\_HOTSTART\_STATUS\_KEYS"  
Only the status keys of the constraints and variables are used to choose the type of hot-start.

**intpnthotstart**  
Hot-start type employed by the interior-point optimizers.

"MSK\_INTPNT\_HOTSTART\_NONE"  
The interior-point optimizer performs a coldstart.

"MSK\_INTPNT\_HOTSTART\_PRIMAL"  
The interior-point optimizer exploits the primal solution only.

"MSK\_INTPNT\_HOTSTART\_DUAL"  
The interior-point optimizer exploits the dual solution only.

"MSK\_INTPNT\_HOTSTART\_PRIMAL\_DUAL"  
The interior-point optimizer exploits both the primal and dual solution.

**purify**  
Solution purification employed optimizer.

"MSK\_PURIFY\_NONE"  
The optimizer performs no solution purification.

"MSK\_PURIFY\_PRIMAL"  
The optimizer purifies the primal solution.

"MSK\_PURIFY\_DUAL"  
The optimizer purifies the dual solution.

"MSK\_PURIFY\_PRIMAL\_DUAL"  
The optimizer purifies both the primal and dual solution.

"MSK\_PURIFY\_AUTO"  
TBD

**callbackcode**  
Progress callback codes

"MSK\_CALLBACK\_BEGIN\_BI"  
The basis identification procedure has been started.

"MSK\_CALLBACK\_BEGIN\_CONIC"  
The callback function is called when the conic optimizer is started.

"MSK\_CALLBACK\_BEGIN\_DUAL\_BI"  
The callback function is called from within the basis identification procedure when the dual phase is started.

"MSK\_CALLBACK\_BEGIN\_DUAL\_SENSITIVITY"  
Dual sensitivity analysis is started.

"MSK\_CALLBACK\_BEGIN\_DUAL\_SETUP\_BI"  
The callback function is called when the dual BI phase is started.

"MSK\_CALLBACK\_BEGIN\_DUAL\_SIMPLEX"  
The callback function is called when the dual simplex optimizer started.

"MSK\_CALLBACK\_BEGIN\_DUAL\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure when the dual simplex clean-up phase is started.

"MSK\_CALLBACK\_BEGIN\_FULL\_CONVEXITY\_CHECK"  
Begin full convexity check.

"MSK\_CALLBACK\_BEGIN\_INFEAS\_ANA"  
The callback function is called when the infeasibility analyzer is started.

"MSK\_CALLBACK\_BEGIN\_INTPNT"  
The callback function is called when the interior-point optimizer is started.

"MSK\_CALLBACK\_BEGIN\_LICENSE\_WAIT"  
Begin waiting for license.

"MSK\_CALLBACK\_BEGIN\_MIO"  
The callback function is called when the mixed-integer optimizer is started.

"MSK\_CALLBACK\_BEGIN\_OPTIMIZER"  
The callback function is called when the optimizer is started.

"MSK\_CALLBACK\_BEGIN\_PRESOLVE"  
The callback function is called when the presolve is started.

"MSK\_CALLBACK\_BEGIN\_PRIMAL\_BI"  
The callback function is called from within the basis identification procedure when the primal phase is started.

"MSK\_CALLBACK\_BEGIN\_PRIMAL\_REPAIR"  
Begin primal feasibility repair.

"MSK\_CALLBACK\_BEGIN\_PRIMAL\_SENSITIVITY"  
Primal sensitivity analysis is started.

"MSK\_CALLBACK\_BEGIN\_PRIMAL\_SETUP\_BI"  
The callback function is called when the primal BI setup is started.

"MSK\_CALLBACK\_BEGIN\_PRIMAL\_SIMPLEX"  
The callback function is called when the primal simplex optimizer is started.

"MSK\_CALLBACK\_BEGIN\_PRIMAL\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure when the primal simplex clean-up phase is started.

"MSK\_CALLBACK\_BEGIN\_QCQO\_REFORMULATE"  
Begin QCQO reformulation.

"MSK\_CALLBACK\_BEGIN\_READ"  
**MOSEK** has started reading a problem file.

"MSK\_CALLBACK\_BEGIN\_ROOT\_CUTGEN"  
The callback function is called when root cut generation is started.

"MSK\_CALLBACK\_BEGIN\_SIMPLEX"  
The callback function is called when the simplex optimizer is started.

"MSK\_CALLBACK\_BEGIN\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure when the simplex clean-up phase is started.

"MSK\_CALLBACK\_BEGIN\_TO\_CONIC"  
Begin conic reformulation.

"MSK\_CALLBACK\_BEGIN\_WRITE"  
**MOSEK** has started writing a problem file.

"MSK\_CALLBACK\_CONIC"  
The callback function is called from within the conic optimizer after the information database has been updated.

"MSK\_CALLBACK\_DUAL\_SIMPLEX"  
The callback function is called from within the dual simplex optimizer.

"MSK\_CALLBACK\_END\_BI"  
The callback function is called when the basis identification procedure is terminated.

"MSK\_CALLBACK\_END\_CONIC"  
The callback function is called when the conic optimizer is terminated.

"MSK\_CALLBACK\_END\_DUAL\_BI"  
The callback function is called from within the basis identification procedure when the dual phase is terminated.

"MSK\_CALLBACK\_END\_DUAL\_SENSITIVITY"  
Dual sensitivity analysis is terminated.

"MSK\_CALLBACK\_END\_DUAL\_SETUP\_BI"  
The callback function is called when the dual BI phase is terminated.

"MSK\_CALLBACK\_END\_DUAL\_SIMPLEX"  
The callback function is called when the dual simplex optimizer is terminated.

"MSK\_CALLBACK\_END\_DUAL\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure when the dual clean-up phase is terminated.

"MSK\_CALLBACK\_END\_FULL\_CONVEXITY\_CHECK"  
End full convexity check.

"MSK\_CALLBACK\_END\_INFEAS\_ANA"  
The callback function is called when the infeasibility analyzer is terminated.

"MSK\_CALLBACK\_END\_INTPNT"  
The callback function is called when the interior-point optimizer is terminated.

"MSK\_CALLBACK\_END\_LICENSE\_WAIT"  
End waiting for license.

"MSK\_CALLBACK\_END\_MIO"  
The callback function is called when the mixed-integer optimizer is terminated.

"MSK\_CALLBACK\_END\_OPTIMIZER"  
The callback function is called when the optimizer is terminated.

"MSK\_CALLBACK\_END\_PRESOLVE"  
The callback function is called when the presolve is completed.

"MSK\_CALLBACK\_END\_PRIMAL\_BI"  
The callback function is called from within the basis identification procedure when the primal phase is terminated.

"MSK\_CALLBACK\_END\_PRIMAL\_REPAIR"  
End primal feasibility repair.

"MSK\_CALLBACK\_END\_PRIMAL\_SENSITIVITY"  
Primal sensitivity analysis is terminated.

"MSK\_CALLBACK\_END\_PRIMAL\_SETUP\_BI"  
The callback function is called when the primal BI setup is terminated.

"MSK\_CALLBACK\_END\_PRIMAL\_SIMPLEX"  
The callback function is called when the primal simplex optimizer is terminated.

"MSK\_CALLBACK\_END\_PRIMAL\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure when the primal clean-up phase is terminated.

"MSK\_CALLBACK\_END\_QCQO\_REFORMULATE"  
End QCQO reformulation.

"MSK\_CALLBACK\_END\_READ"  
**MOSEK** has finished reading a problem file.

"MSK\_CALLBACK\_END\_ROOT\_CUTGEN"  
The callback function is called when root cut generation is terminated.

"MSK\_CALLBACK\_END\_SIMPLEX"  
The callback function is called when the simplex optimizer is terminated.

"MSK\_CALLBACK\_END\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure when the simplex clean-up phase is terminated.

"MSK\_CALLBACK\_END\_TO\_CONIC"  
End conic reformulation.

"MSK\_CALLBACK\_END\_WRITE"  
**MOSEK** has finished writing a problem file.

"MSK\_CALLBACK\_IM\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point.

"MSK\_CALLBACK\_IM\_CONIC"  
The callback function is called at an intermediate stage within the conic optimizer where the information database has not been updated.

"MSK\_CALLBACK\_IM\_DUAL\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

"MSK\_CALLBACK\_IM\_DUAL\_SENSIVITY"  
The callback function is called at an intermediate stage of the dual sensitivity analysis.

"MSK\_CALLBACK\_IM\_DUAL\_SIMPLEX"  
The callback function is called at an intermediate point in the dual simplex optimizer.

"MSK\_CALLBACK\_IM\_FULL\_CONVEXITY\_CHECK"  
The callback function is called at an intermediate stage of the full convexity check.

"MSK\_CALLBACK\_IM\_INTPNT"  
The callback function is called at an intermediate stage within the interior-point optimizer where the information database has not been updated.

"MSK\_CALLBACK\_IM\_LICENSE\_WAIT"  
**MOSEK** is waiting for a license.

"MSK\_CALLBACK\_IM\_LU"  
The callback function is called from within the LU factorization procedure at an intermediate point.

"MSK\_CALLBACK\_IM\_MIO"  
The callback function is called at an intermediate point in the mixed-integer optimizer.

"MSK\_CALLBACK\_IM\_MIO\_DUAL\_SIMPLEX"  
The callback function is called at an intermediate point in the mixed-integer optimizer while running the dual simplex optimizer.

"MSK\_CALLBACK\_IM\_MIO\_INTPNT"  
The callback function is called at an intermediate point in the mixed-integer optimizer while running the interior-point optimizer.

"MSK\_CALLBACK\_IM\_MIO\_PRIMAL\_SIMPLEX"  
The callback function is called at an intermediate point in the mixed-integer optimizer while running the primal simplex optimizer.

"MSK\_CALLBACK\_IM\_ORDER"  
The callback function is called from within the matrix ordering procedure at an intermediate point.

"MSK\_CALLBACK\_IM\_PRESOLVE"  
The callback function is called from within the presolve procedure at an intermediate stage.

"MSK\_CALLBACK\_IM\_PRIMAL\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

"MSK\_CALLBACK\_IM\_PRIMAL\_SENSIVITY"  
The callback function is called at an intermediate stage of the primal sensitivity analysis.

"MSK\_CALLBACK\_IM\_PRIMAL\_SIMPLEX"  
The callback function is called at an intermediate point in the primal simplex optimizer.

"MSK\_CALLBACK\_IM\_QO\_REFORMULATE"  
The callback function is called at an intermediate stage of the conic quadratic reformulation.

"MSK\_CALLBACK\_IM\_READ"  
Intermediate stage in reading.

"MSK\_CALLBACK\_IM\_ROOT\_CUTGEN"  
The callback is called from within root cut generation at an intermediate stage.

"MSK\_CALLBACK\_IM\_SIMPLEX"  
The callback function is called from within the simplex optimizer at an intermediate point.

"MSK\_CALLBACK\_IM\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point in the simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK\_IPAR\_LOG\_SIM\_FREQ* parameter.

"MSK\_CALLBACK\_INTPNT"  
The callback function is called from within the interior-point optimizer after the information database has been updated.

"MSK\_CALLBACK\_NEW\_INT\_MIO"  
The callback function is called after a new integer solution has been located by the mixed-integer optimizer.

"MSK\_CALLBACK\_PRIMAL\_SIMPLEX"  
The callback function is called from within the primal simplex optimizer.

"MSK\_CALLBACK\_READ\_OPF"  
The callback function is called from the OPF reader.

"MSK\_CALLBACK\_READ\_OPF\_SECTION"  
A chunk of  $Q$  non-zeros has been read from a problem file.

"MSK\_CALLBACK\_SOLVING\_REMOTE"  
The callback function is called while the task is being solved on a remote server.

"MSK\_CALLBACK\_UPDATE\_DUAL\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

"MSK\_CALLBACK\_UPDATE\_DUAL\_SIMPLEX"  
The callback function is called in the dual simplex optimizer.

"MSK\_CALLBACK\_UPDATE\_DUAL\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point in the dual simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK\_IPAR\_LOG\_SIM\_FREQ* parameter.

"MSK\_CALLBACK\_UPDATE\_PRESOLVE"  
The callback function is called from within the presolve procedure.

"MSK\_CALLBACK\_UPDATE\_PRIMAL\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

"MSK\_CALLBACK\_UPDATE\_PRIMAL\_SIMPLEX"  
The callback function is called in the primal simplex optimizer.

"MSK\_CALLBACK\_UPDATE\_PRIMAL\_SIMPLEX\_BI"  
The callback function is called from within the basis identification procedure at an intermediate point in the primal simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK\_IPAR\_LOG\_SIM\_FREQ* parameter.

"MSK\_CALLBACK\_WRITE\_OPF"  
The callback function is called from the OPF writer.

checkconvexitytype  
Types of convexity checks.

"MSK\_CHECK\_CONVEXITY\_NONE"  
No convexity check.

"MSK\_CHECK\_CONVEXITY\_SIMPLE"  
Perform simple and fast convexity check.

"MSK\_CHECK\_CONVEXITY\_FULL"  
 Perform a full convexity check.

**compresstype**  
 Compression types

"MSK\_COMPRESS\_NONE"  
 No compression is used.

"MSK\_COMPRESS\_FREE"  
 The type of compression used is chosen automatically.

"MSK\_COMPRESS\_GZIP"  
 The type of compression used is gzip compatible.

"MSK\_COMPRESS\_ZSTD"  
 The type of compression used is zstd compatible.

**conetype**  
 Cone types

"MSK\_CT\_QUAD"  
 The cone is a quadratic cone.

"MSK\_CT\_RQUAD"  
 The cone is a rotated quadratic cone.

"MSK\_CT\_PEXP"  
 A primal exponential cone.

"MSK\_CT\_DEXP"  
 A dual exponential cone.

"MSK\_CT\_PPOW"  
 A primal power cone.

"MSK\_CT\_DPOW"  
 A dual power cone.

"MSK\_CT\_ZERO"  
 The zero cone.

**nametype**  
 Name types

"MSK\_NAME\_TYPE\_GEN"  
 General names. However, no duplicate and blank names are allowed.

"MSK\_NAME\_TYPE\_MPS"  
 MPS type names.

"MSK\_NAME\_TYPE\_LP"  
 LP type names.

**scopr**  
 SCopt operator types

"MSK\_OPR\_ENT"  
 Entropy

"MSK\_OPR\_EXP"  
 Exponential

"MSK\_OPR\_LOG"  
 Logarithm

"MSK\_OPR\_POW"  
 Power

"MSK\_OPR\_SQRT"  
 Square root

**symmattype**  
 Cone types

"MSK\_SYMMAT\_TYPE\_SPARSE"  
 Sparse symmetric matrix.





"MSK\_DINF\_MIO\_ROOT\_PREOLVE\_TIME"  
Time spent presolving the problem at the root node.

"MSK\_DINF\_MIO\_TIME"  
Time spent in the mixed-integer optimizer.

"MSK\_DINF\_MIO\_USER\_OBJ\_CUT"  
If the objective cut is used, then this information item has the value of the cut.

"MSK\_DINF\_OPTIMIZER\_TIME"  
Total time spent in the optimizer since it was invoked.

"MSK\_DINF\_PREOLVE\_ELI\_TIME"  
Total time spent in the eliminator since the presolve was invoked.

"MSK\_DINF\_PREOLVE\_LINDEP\_TIME"  
Total time spent in the linear dependency checker since the presolve was invoked.

"MSK\_DINF\_PREOLVE\_TIME"  
Total time (in seconds) spent in the presolve since it was invoked.

"MSK\_DINF\_PRIMAL\_REPAIR\_PENALTY\_OBJ"  
The optimal objective value of the penalty function.

"MSK\_DINF\_QCQO\_REFORMULATE\_MAX\_PERTURBATION"  
Maximum absolute diagonal perturbation occurring during the QCQO reformulation.

"MSK\_DINF\_QCQO\_REFORMULATE\_TIME"  
Time spent with conic quadratic reformulation.

"MSK\_DINF\_QCQO\_REFORMULATE\_WORST\_CHOLESKY\_COLUMN\_SCALING"  
Worst Cholesky column scaling.

"MSK\_DINF\_QCQO\_REFORMULATE\_WORST\_CHOLESKY\_DIAG\_SCALING"  
Worst Cholesky diagonal scaling.

"MSK\_DINF\_RD\_TIME"  
Time spent reading the data file.

"MSK\_DINF\_SIM\_DUAL\_TIME"  
Time spent in the dual simplex optimizer since invoking it.

"MSK\_DINF\_SIM\_FEAS"  
Feasibility measure reported by the simplex optimizer.

"MSK\_DINF\_SIM\_OBJ"  
Objective value reported by the simplex optimizer.

"MSK\_DINF\_SIM\_PRIMAL\_TIME"  
Time spent in the primal simplex optimizer since invoking it.

"MSK\_DINF\_SIM\_TIME"  
Time spent in the simplex optimizer since invoking it.

"MSK\_DINF\_SOL\_BAS\_DUAL\_OBJ"  
Dual objective value of the basic solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_BAS\_DVIOLCON"  
Maximal dual bound violation for  $x^c$  in the basic solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_BAS\_DVIOLVAR"  
Maximal dual bound violation for  $x^x$  in the basic solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_BAS\_NRM\_BARX"  
Infinity norm of  $\overline{X}$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_NRM\_SLC"  
Infinity norm of  $s_l^c$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_NRM\_SLX"  
Infinity norm of  $s_l^x$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_NRM\_SUC"  
Infinity norm of  $s_u^c$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_NRM\_SUX"  
Infinity norm of  $s_u^X$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_NRM\_XC"  
Infinity norm of  $x^c$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_NRM\_XX"  
Infinity norm of  $x^x$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_NRM\_Y"  
Infinity norm of  $y$  in the basic solution.

"MSK\_DINF\_SOL\_BAS\_PRIMAL\_OBJ"  
Primal objective value of the basic solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_BAS\_PVIOLCON"  
Maximal primal bound violation for  $x^c$  in the basic solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_BAS\_PVIOLVAR"  
Maximal primal bound violation for  $x^x$  in the basic solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITG\_NRM\_BARX"  
Infinity norm of  $\bar{X}$  in the integer solution.

"MSK\_DINF\_SOL\_ITG\_NRM\_XC"  
Infinity norm of  $x^c$  in the integer solution.

"MSK\_DINF\_SOL\_ITG\_NRM\_XX"  
Infinity norm of  $x^x$  in the integer solution.

"MSK\_DINF\_SOL\_ITG\_PRIMAL\_OBJ"  
Primal objective value of the integer solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITG\_PVIOLBARVAR"  
Maximal primal bound violation for  $\bar{X}$  in the integer solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITG\_PVIOLCON"  
Maximal primal bound violation for  $x^c$  in the integer solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITG\_PVIOLCONES"  
Maximal primal violation for primal conic constraints in the integer solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITG\_PVIOLITG"  
Maximal violation for the integer constraints in the integer solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITG\_PVIOLVAR"  
Maximal primal bound violation for  $x^x$  in the integer solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_DUAL\_OBJ"  
Dual objective value of the interior-point solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_DVIOLBARVAR"  
Maximal dual bound violation for  $\bar{X}$  in the interior-point solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_DVIOLCON"  
Maximal dual bound violation for  $x^c$  in the interior-point solution. Updated if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_DVIOLCONES"  
Maximal dual violation for dual conic constraints in the interior-point solution. Updated if  
*MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_DVIOLVAR"  
Maximal dual bound violation for  $x^x$  in the interior-point solution. Updated if  
*MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_NRM\_BARS"  
Infinity norm of  $\bar{S}$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_BARX"  
Infinity norm of  $\bar{X}$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_SLC"  
Infinity norm of  $s_l^c$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_SLX"  
Infinity norm of  $s_l^x$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_SNX"  
Infinity norm of  $s_n^x$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_SUC"  
Infinity norm of  $s_u^c$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_SUX"  
Infinity norm of  $s_u^X$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_XC"  
Infinity norm of  $x^c$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_XX"  
Infinity norm of  $x^x$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_NRM\_Y"  
Infinity norm of  $y$  in the interior-point solution.

"MSK\_DINF\_SOL\_ITR\_PRIMAL\_OBJ"  
Primal objective value of the interior-point solution. Updated if  
*MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_PVIOLBARVAR"  
Maximal primal bound violation for  $\bar{X}$  in the interior-point solution. Updated if  
*MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_PVIOLCON"  
Maximal primal bound violation for  $x^c$  in the interior-point solution. Updated if  
*MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_PVIOLCONES"  
Maximal primal violation for primal conic constraints in the interior-point solution. Updated  
if *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_SOL\_ITR\_PVIOLVAR"  
Maximal primal bound violation for  $x^x$  in the interior-point solution. Updated if  
*MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO* is set .

"MSK\_DINF\_TO\_CONIC\_TIME"  
Time spent in the last to conic reformulation.

**feature**  
License feature

"MSK\_FEATURE\_PTS"  
Base system.

"MSK\_FEATURE\_PTON"  
Conic extension.

**liinfitem**  
Long integer information items.

"MSK\_LIINF\_BI\_CLEAN\_DUAL\_DEG\_ITER"  
Number of dual degenerate clean iterations performed in the basis identification.

"MSK\_LIINF\_BI\_CLEAN\_DUAL\_ITER"  
Number of dual clean iterations performed in the basis identification.

"MSK\_LIINF\_BI\_CLEAN\_PRIMAL\_DEG\_ITER"  
Number of primal degenerate clean iterations performed in the basis identification.

"MSK\_LIINF\_BI\_CLEAN\_PRIMAL\_ITER"  
Number of primal clean iterations performed in the basis identification.

"MSK\_LIINF\_BI\_DUAL\_ITER"  
Number of dual pivots performed in the basis identification.

"MSK\_LIINF\_BI\_PRIMAL\_ITER"  
Number of primal pivots performed in the basis identification.

"MSK\_LIINF\_INTPNT\_FACTOR\_NUM\_NZ"  
Number of non-zeros in factorization.

"MSK\_LIINF\_MIO\_ANZ"  
Number of non-zero entries in the constraint matrix of the problem to be solved by the mixed-integer optimizer.

"MSK\_LIINF\_MIO\_INTPNT\_ITER"  
Number of interior-point iterations performed by the mixed-integer optimizer.

"MSK\_LIINF\_MIO\_PRESTORED\_ANZ"  
Number of non-zero entries in the constraint matrix of the problem after the mixed-integer optimizer's presolve.

"MSK\_LIINF\_MIO\_SIMPLEX\_ITER"  
Number of simplex iterations performed by the mixed-integer optimizer.

"MSK\_LIINF\_RD\_NUMANZ"  
Number of non-zeros in A that is read.

"MSK\_LIINF\_RD\_NUMQNZ"  
Number of Q non-zeros.

iinfitem  
Integer information items.

"MSK\_IINF\_ANA\_PRO\_NUM\_CON"  
Number of constraints in the problem.

"MSK\_IINF\_ANA\_PRO\_NUM\_CON\_EQ"  
Number of equality constraints.

"MSK\_IINF\_ANA\_PRO\_NUM\_CON\_FR"  
Number of unbounded constraints.

"MSK\_IINF\_ANA\_PRO\_NUM\_CON\_LO"  
Number of constraints with a lower bound and an infinite upper bound.

"MSK\_IINF\_ANA\_PRO\_NUM\_CON\_RA"  
Number of constraints with finite lower and upper bounds.

"MSK\_IINF\_ANA\_PRO\_NUM\_CON\_UP"  
Number of constraints with an upper bound and an infinite lower bound.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR"  
Number of variables in the problem.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_BIN"  
Number of binary (0-1) variables.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_CONT"  
Number of continuous variables.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_EQ"  
Number of fixed variables.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_FR"  
Number of free variables.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_INT"  
Number of general integer variables.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_LO"  
Number of variables with a lower bound and an infinite upper bound.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_RA"  
Number of variables with finite lower and upper bounds.

"MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_UP"  
Number of variables with an upper bound and an infinite lower bound.

"MSK\_IINF\_INTPNT\_FACTOR\_DIM\_DENSE"  
Dimension of the dense sub system in factorization.

"MSK\_IINF\_INTPNT\_ITER"  
Number of interior-point iterations since invoking the interior-point optimizer.

"MSK\_IINF\_INTPNT\_NUM\_THREADS"  
Number of threads that the interior-point optimizer is using.

"MSK\_IINF\_INTPNT\_SOLVE\_DUAL"  
Non-zero if the interior-point optimizer is solving the dual problem.

"MSK\_IINF\_MIO\_ABSGAP\_SATISFIED"  
Non-zero if absolute gap is within tolerances.

"MSK\_IINF\_MIO\_CLIQUETABLE\_SIZE"  
Size of the clique table.

"MSK\_IINF\_MIO\_CONSTRUCT\_SOLUTION"  
This item informs if **MOSEK** constructed an initial integer feasible solution.

- -1: tried, but failed,
- 0: no partial solution supplied by the user,
- 1: constructed feasible solution.

"MSK\_IINF\_MIO\_NODE\_DEPTH"  
Depth of the last node solved.

"MSK\_IINF\_MIO\_NUM\_ACTIVE\_NODES"  
Number of active branch and bound nodes.

"MSK\_IINF\_MIO\_NUM\_BRANCH"  
Number of branches performed during the optimization.

"MSK\_IINF\_MIO\_NUM\_CLIQUETABLE\_CUTS"  
Number of clique cuts.

"MSK\_IINF\_MIO\_NUM\_CMIR\_CUTS"  
Number of Complemented Mixed Integer Rounding (CMIR) cuts.

"MSK\_IINF\_MIO\_NUM\_GOMORY\_CUTS"  
Number of Gomory cuts.

"MSK\_IINF\_MIO\_NUM\_IMPLIED\_BOUND\_CUTS"  
Number of implied bound cuts.

"MSK\_IINF\_MIO\_NUM\_INT\_SOLUTIONS"  
Number of integer feasible solutions that have been found.

"MSK\_IINF\_MIO\_NUM\_KNAPSACK\_COVER\_CUTS"  
Number of clique cuts.

"MSK\_IINF\_MIO\_NUM\_RELAX"  
Number of relaxations solved during the optimization.

"MSK\_IINF\_MIO\_NUM\_REPEATED\_PRESOLVE"  
Number of times presolve was repeated at root.

"MSK\_IINF\_MIO\_NUMBIN"  
Number of binary variables in the problem to be solved by the mixed-integer optimizer.



"MSK\_IINF\_MIO\_PRESOLVED\_NUMDPOWCONES"  
 Number of dual power cones in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_PRESOLVED\_NUMINT"  
 Number of integer variables in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_PRESOLVED\_NUMINTCONEVAR"  
 Number of integer cone variables in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_PRESOLVED\_NUMEXPCONES"  
 Number of primal exponential cones in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_PRESOLVED\_NUMPPOWCONES"  
 Number of primal power cones in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_PRESOLVED\_NUMQCONES"  
 Number of quadratic cones in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_PRESOLVED\_NUMRQCONES"  
 Number of rotated quadratic cones in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_PRESOLVED\_NUMVAR"  
 Number of variables in the problem after the mixed-integer optimizer's presolve.

"MSK\_IINF\_MIO\_RELGAP\_SATISFIED"  
 Non-zero if relative gap is within tolerances.

"MSK\_IINF\_MIO\_TOTAL\_NUM\_CUTS"  
 Total number of cuts generated by the mixed-integer optimizer.

"MSK\_IINF\_MIO\_USER\_OBJ\_CUT"  
 If it is non-zero, then the objective cut is used.

"MSK\_IINF\_OPT\_NUMCON"  
 Number of constraints in the problem solved when the optimizer is called.

"MSK\_IINF\_OPT\_NUMVAR"  
 Number of variables in the problem solved when the optimizer is called

"MSK\_IINF\_OPTIMIZE\_RESPONSE"  
 The response code returned by optimize.

"MSK\_IINF\_PURIFY\_DUAL\_SUCCESS"  
 Is nonzero if the dual solution is purified.

"MSK\_IINF\_PURIFY\_PRIMAL\_SUCCESS"  
 Is nonzero if the primal solution is purified.

"MSK\_IINF\_RD\_NUMBARVAR"  
 Number of symmetric variables read.

"MSK\_IINF\_RD\_NUMCON"  
 Number of constraints read.

"MSK\_IINF\_RD\_NUMCONE"  
 Number of conic constraints read.

"MSK\_IINF\_RD\_NUMINTVAR"  
 Number of integer-constrained variables read.

"MSK\_IINF\_RD\_NUMQ"  
 Number of nonempty Q matrices read.

"MSK\_IINF\_RD\_NUMVAR"  
 Number of variables read.

"MSK\_IINF\_RD\_PROTOTYPE"  
 Problem type.

"MSK\_IINF\_SIM\_DUAL\_DEG\_ITER"  
 The number of dual degenerate iterations.

"MSK\_IINF\_SIM\_DUAL\_HOTSTART"  
 If 1 then the dual simplex algorithm is solving from an advanced basis.

"MSK\_IINF\_SIM\_DUAL\_HOTSTART\_LU"  
 If 1 then a valid basis factorization of full rank was located and used by the dual simplex algorithm.

"MSK\_IINF\_SIM\_DUAL\_INF\_ITER"  
 The number of iterations taken with dual infeasibility.

"MSK\_IINF\_SIM\_DUAL\_ITER"  
 Number of dual simplex iterations during the last optimization.

"MSK\_IINF\_SIM\_NUMCON"  
 Number of constraints in the problem solved by the simplex optimizer.

"MSK\_IINF\_SIM\_NUMVAR"  
 Number of variables in the problem solved by the simplex optimizer.

"MSK\_IINF\_SIM\_PRIMAL\_DEG\_ITER"  
 The number of primal degenerate iterations.

"MSK\_IINF\_SIM\_PRIMAL\_HOTSTART"  
 If 1 then the primal simplex algorithm is solving from an advanced basis.

"MSK\_IINF\_SIM\_PRIMAL\_HOTSTART\_LU"  
 If 1 then a valid basis factorization of full rank was located and used by the primal simplex algorithm.

"MSK\_IINF\_SIM\_PRIMAL\_INF\_ITER"  
 The number of iterations taken with primal infeasibility.

"MSK\_IINF\_SIM\_PRIMAL\_ITER"  
 Number of primal simplex iterations during the last optimization.

"MSK\_IINF\_SIM\_SOLVE\_DUAL"  
 Is non-zero if dual problem is solved.

"MSK\_IINF\_SOL\_BAS\_PROSTA"  
 Problem status of the basic solution. Updated after each optimization.

"MSK\_IINF\_SOL\_BAS\_SOLSTA"  
 Solution status of the basic solution. Updated after each optimization.

"MSK\_IINF\_SOL\_ITG\_PROSTA"  
 Problem status of the integer solution. Updated after each optimization.

"MSK\_IINF\_SOL\_ITG\_SOLSTA"  
 Solution status of the integer solution. Updated after each optimization.

"MSK\_IINF\_SOL\_ITR\_PROSTA"  
 Problem status of the interior-point solution. Updated after each optimization.

"MSK\_IINF\_SOL\_ITR\_SOLSTA"  
 Solution status of the interior-point solution. Updated after each optimization.

"MSK\_IINF\_STO\_NUM\_A\_REALLOC"  
 Number of times the storage for storing  $A$  has been changed. A large value may indicate that memory fragmentation may occur.

**inftype**  
 Information item types

"MSK\_INF\_DOU\_TYPE"  
 Is a double information type.

"MSK\_INF\_INT\_TYPE"  
 Is an integer.

"MSK\_INF\_LINT\_TYPE"  
 Is a long integer.

**iomode**  
 Input/output modes

"MSK\_IOMODE\_READ"  
 The file is read-only.

"MSK\_IOMODE\_WRITE"  
The file is write-only. If the file exists then it is truncated when it is opened. Otherwise it is created when it is opened.

"MSK\_IOMODE\_READWRITE"  
The file is to read and write.

**branchdir**  
Specifies the branching direction.

"MSK\_BRANCH\_DIR\_FREE"  
The mixed-integer optimizer decides which branch to choose.

"MSK\_BRANCH\_DIR\_UP"  
The mixed-integer optimizer always chooses the up branch first.

"MSK\_BRANCH\_DIR\_DOWN"  
The mixed-integer optimizer always chooses the down branch first.

"MSK\_BRANCH\_DIR\_NEAR"  
Branch in direction nearest to selected fractional variable.

"MSK\_BRANCH\_DIR\_FAR"  
Branch in direction farthest from selected fractional variable.

"MSK\_BRANCH\_DIR\_ROOT\_LP"  
Chose direction based on root lp value of selected variable.

"MSK\_BRANCH\_DIR\_GUIDED"  
Branch in direction of current incumbent.

"MSK\_BRANCH\_DIR\_PSEUDOCOST"  
Branch based on the pseudocost of the variable.

**miocontsoltype**  
Continuous mixed-integer solution type

"MSK\_MIO\_CONT\_SOL\_NONE"  
No interior-point or basic solution are reported when the mixed-integer optimizer is used.

"MSK\_MIO\_CONT\_SOL\_ROOT"  
The reported interior-point and basic solutions are a solution to the root node problem when mixed-integer optimizer is used.

"MSK\_MIO\_CONT\_SOL\_ITG"  
The reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. A solution is only reported in case the problem has a primal feasible solution.

"MSK\_MIO\_CONT\_SOL\_ITG\_REL"  
In case the problem is primal feasible then the reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. If the problem is primal infeasible, then the solution to the root node problem is reported.

**miomode**  
Integer restrictions

"MSK\_MIO\_MODE\_IGNORED"  
The integer constraints are ignored and the problem is solved as a continuous problem.

"MSK\_MIO\_MODE\_SATISFIED"  
Integer restrictions should be satisfied.

**mionodeseltype**  
Mixed-integer node selection types

"MSK\_MIO\_NODE\_SELECTION\_FREE"  
The optimizer decides the node selection strategy.

"MSK\_MIO\_NODE\_SELECTION\_FIRST"  
The optimizer employs a depth first node selection strategy.

"MSK\_MIO\_NODE\_SELECTION\_BEST"  
The optimizer employs a best bound node selection strategy.

"MSK\_MIO\_NODE\_SELECTION\_PSEUDO"  
The optimizer employs selects the node based on a pseudo cost estimate.

**mpsformat**  
MPS file format type

"MSK\_MPS\_FORMAT\_STRICT"  
It is assumed that the input file satisfies the MPS format strictly.

"MSK\_MPS\_FORMAT\_RELAXED"  
It is assumed that the input file satisfies a slightly relaxed version of the MPS format.

"MSK\_MPS\_FORMAT\_FREE"  
It is assumed that the input file satisfies the free MPS format. This implies that spaces are not allowed in names. Otherwise the format is free.

"MSK\_MPS\_FORMAT\_CPLEX"  
The CPLEX compatible version of the MPS format is employed.

**objsense**  
Objective sense types

"MSK\_OBJECTIVE\_SENSE\_MINIMIZE"  
The problem should be minimized.

"MSK\_OBJECTIVE\_SENSE\_MAXIMIZE"  
The problem should be maximized.

**onoffkey**  
On/off

"MSK\_ON"  
Switch the option on.

"MSK\_OFF"  
Switch the option off.

**optimizertype**  
Optimizer types

"MSK\_OPTIMIZER\_CONIC"  
The optimizer for problems having conic constraints.

"MSK\_OPTIMIZER\_DUAL\_SIMPLEX"  
The dual simplex optimizer is used.

"MSK\_OPTIMIZER\_FREE"  
The optimizer is chosen automatically.

"MSK\_OPTIMIZER\_FREE\_SIMPLEX"  
One of the simplex optimizers is used.

"MSK\_OPTIMIZER\_INTPNT"  
The interior-point optimizer is used.

"MSK\_OPTIMIZER\_MIXED\_INT"  
The mixed-integer optimizer.

"MSK\_OPTIMIZER\_PRIMAL\_SIMPLEX"  
The primal simplex optimizer is used.

**orderingtype**  
Ordering strategies

"MSK\_ORDER\_METHOD\_FREE"  
The ordering method is chosen automatically.

"MSK\_ORDER\_METHOD\_APPMINLOC"  
Approximate minimum local fill-in ordering is employed.

"MSK\_ORDER\_METHOD\_EXPERIMENTAL"  
This option should not be used.

"MSK\_ORDER\_METHOD\_TRY\_GRAPHPAR"  
Always try the graph partitioning based ordering.

"MSK\_ORDER\_METHOD\_FORCE\_GRAPHPAR"  
 Always use the graph partitioning based ordering even if it is worse than the approximate minimum local fill ordering.

"MSK\_ORDER\_METHOD\_NONE"  
 No ordering is used.

**presolvemode**  
 Presolve method.

"MSK\_PRESOLVE\_MODE\_OFF"  
 The problem is not presolved before it is optimized.

"MSK\_PRESOLVE\_MODE\_ON"  
 The problem is presolved before it is optimized.

"MSK\_PRESOLVE\_MODE\_FREE"  
 It is decided automatically whether to presolve before the problem is optimized.

**parametertype**  
 Parameter type

"MSK\_PAR\_INVALID\_TYPE"  
 Not a valid parameter.

"MSK\_PAR\_DOUB\_TYPE"  
 Is a double parameter.

"MSK\_PAR\_INT\_TYPE"  
 Is an integer parameter.

"MSK\_PAR\_STR\_TYPE"  
 Is a string parameter.

**problemitem**  
 Problem data items

"MSK\_PI\_VAR"  
 Item is a variable.

"MSK\_PI\_CON"  
 Item is a constraint.

"MSK\_PI\_CONE"  
 Item is a cone.

**problemtypes**  
 Problem types

"MSK\_PROBTYPE\_LO"  
 The problem is a linear optimization problem.

"MSK\_PROBTYPE\_QQ"  
 The problem is a quadratic optimization problem.

"MSK\_PROBTYPE\_QCQO"  
 The problem is a quadratically constrained optimization problem.

"MSK\_PROBTYPE\_CONIC"  
 A conic optimization.

"MSK\_PROBTYPE\_MIXED"  
 General nonlinear constraints and conic constraints. This combination can not be solved by **MOSEK**.

**prosta**  
 Problem status keys

"MSK\_PRO\_STA\_UNKNOWN"  
 Unknown problem status.

"MSK\_PRO\_STA\_PRIM\_AND\_DUAL\_FEAS"  
 The problem is primal and dual feasible.

"MSK\_PRO\_STA\_PRIM\_FEAS"  
 The problem is primal feasible.

"MSK\_PRO\_STA\_DUAL\_FEAS"  
The problem is dual feasible.

"MSK\_PRO\_STA\_PRIM\_INFEAS"  
The problem is primal infeasible.

"MSK\_PRO\_STA\_DUAL\_INFEAS"  
The problem is dual infeasible.

"MSK\_PRO\_STA\_PRIM\_AND\_DUAL\_INFEAS"  
The problem is primal and dual infeasible.

"MSK\_PRO\_STA\_ILL\_POSED"  
The problem is ill-posed. For example, it may be primal and dual feasible but have a positive duality gap.

"MSK\_PRO\_STA\_PRIM\_INFEAS\_OR\_UNBOUNDED"  
The problem is either primal infeasible or unbounded. This may occur for mixed-integer problems.

**xmlwriteroutputtype**  
XML writer output mode

"MSK\_WRITE\_XML\_MODE\_ROW"  
Write in row order.

"MSK\_WRITE\_XML\_MODE\_COL"  
Write in column order.

**rescodetype**  
Response code type

"MSK\_RESPONSE\_OK"  
The response code is OK.

"MSK\_RESPONSE\_WRN"  
The response code is a warning.

"MSK\_RESPONSE\_TRM"  
The response code is an optimizer termination status.

"MSK\_RESPONSE\_ERR"  
The response code is an error.

"MSK\_RESPONSE\_UNK"  
The response code does not belong to any class.

**scalingtype**  
Scaling type

"MSK\_SCALING\_FREE"  
The optimizer chooses the scaling heuristic.

"MSK\_SCALING\_NONE"  
No scaling is performed.

"MSK\_SCALING\_MODERATE"  
A conservative scaling is performed.

"MSK\_SCALING\_AGGRESSIVE"  
A very aggressive scaling is performed.

**scalingmethod**  
Scaling method

"MSK\_SCALING\_METHOD\_POW2"  
Scales only with power of 2 leaving the mantissa untouched.

"MSK\_SCALING\_METHOD\_FREE"  
The optimizer chooses the scaling heuristic.

**sensitivitytype**  
Sensitivity types

"MSK\_SENSITIVITY\_TYPE\_BASIS"  
Basis sensitivity analysis is performed.

**simseltype**  
Simplex selection strategy

"MSK\_SIM\_SELECTION\_FREE"  
The optimizer chooses the pricing strategy.

"MSK\_SIM\_SELECTION\_FULL"  
The optimizer uses full pricing.

"MSK\_SIM\_SELECTION\_ASE"  
The optimizer uses approximate steepest-edge pricing.

"MSK\_SIM\_SELECTION\_DEVEX"  
The optimizer uses devex steepest-edge pricing (or if it is not available an approximate steep-edge selection).

"MSK\_SIM\_SELECTION\_SE"  
The optimizer uses steepest-edge selection (or if it is not available an approximate steep-edge selection).

"MSK\_SIM\_SELECTION\_PARTIAL"  
The optimizer uses a partial selection approach. The approach is usually beneficial if the number of variables is much larger than the number of constraints.

**solitem**  
Solution items

"MSK\_SOL\_ITEM\_XC"  
Solution for the constraints.

"MSK\_SOL\_ITEM\_XX"  
Variable solution.

"MSK\_SOL\_ITEM\_Y"  
Lagrange multipliers for equations.

"MSK\_SOL\_ITEM\_SLC"  
Lagrange multipliers for lower bounds on the constraints.

"MSK\_SOL\_ITEM\_SUC"  
Lagrange multipliers for upper bounds on the constraints.

"MSK\_SOL\_ITEM\_SLX"  
Lagrange multipliers for lower bounds on the variables.

"MSK\_SOL\_ITEM\_SUX"  
Lagrange multipliers for upper bounds on the variables.

"MSK\_SOL\_ITEM\_SNX"  
Lagrange multipliers corresponding to the conic constraints on the variables.

**solsta**  
Solution status keys

"MSK\_SOL\_STA\_UNKNOWN"  
Status of the solution is unknown.

"MSK\_SOL\_STA\_OPTIMAL"  
The solution is optimal.

"MSK\_SOL\_STA\_PRIM\_FEAS"  
The solution is primal feasible.

"MSK\_SOL\_STA\_DUAL\_FEAS"  
The solution is dual feasible.

"MSK\_SOL\_STA\_PRIM\_AND\_DUAL\_FEAS"  
The solution is both primal and dual feasible.

"MSK\_SOL\_STA\_PRIM\_INFEAS\_CER"  
The solution is a certificate of primal infeasibility.

"MSK\_SOL\_STA\_DUAL\_INFEAS\_CER"  
The solution is a certificate of dual infeasibility.

"MSK\_SOL\_STA\_PRIM\_ILLPOSED\_CER"  
The solution is a certificate that the primal problem is illposed.

"MSK\_SOL\_STA\_DUAL\_ILLPOSED\_CER"  
The solution is a certificate that the dual problem is illposed.

"MSK\_SOL\_STA\_INTEGER\_OPTIMAL"  
The primal solution is integer optimal.

**soltype**  
Solution types

"MSK\_SOL\_BAS"  
The basic solution.

"MSK\_SOL\_ITR"  
The interior solution.

"MSK\_SOL\_ITG"  
The integer solution.

**solveform**  
Solve primal or dual form

"MSK\_SOLVE\_FREE"  
The optimizer is free to solve either the primal or the dual problem.

"MSK\_SOLVE\_PRIMAL"  
The optimizer should solve the primal problem.

"MSK\_SOLVE\_DUAL"  
The optimizer should solve the dual problem.

**stakey**  
Status keys

"MSK\_SK\_UNK"  
The status for the constraint or variable is unknown.

"MSK\_SK\_BAS"  
The constraint or variable is in the basis.

"MSK\_SK\_SUPBAS"  
The constraint or variable is super basic.

"MSK\_SK\_LOW"  
The constraint or variable is at its lower bound.

"MSK\_SK\_UPR"  
The constraint or variable is at its upper bound.

"MSK\_SK\_FIX"  
The constraint or variable is fixed.

"MSK\_SK\_INF"  
The constraint or variable is infeasible in the bounds.

**startpointtype**  
Starting point types

"MSK\_STARTING\_POINT\_FREE"  
The starting point is chosen automatically.

"MSK\_STARTING\_POINT\_GUESS"  
The optimizer guesses a starting point.

"MSK\_STARTING\_POINT\_CONSTANT"  
The optimizer constructs a starting point by assigning a constant value to all primal and dual variables. This starting point is normally robust.

"MSK\_STARTING\_POINT\_SATISFY\_BOUNDS"  
The starting point is chosen to satisfy all the simple bounds on nonlinear variables. If this starting point is employed, then more care than usual should be employed when choosing the bounds on the nonlinear variables. In particular very tight bounds should be avoided.

**streamtype**  
Stream types

- "MSK\_STREAM\_LOG"  
Log stream. Contains the aggregated contents of all other streams. This means that a message written to any other stream will also be written to this stream.
- "MSK\_STREAM\_MSG"  
Message stream. Log information relating to performance and progress of the optimization is written to this stream.
- "MSK\_STREAM\_ERR"  
Error stream. Error messages are written to this stream.
- "MSK\_STREAM\_WRN"  
Warning stream. Warning messages are written to this stream.

**value**  
Integer values

- "MSK\_MAX\_STR\_LEN"  
Maximum string length allowed in **MOSEK**.
- "MSK\_LICENSE\_BUFFER\_LENGTH"  
The length of a license key buffer.

**variabletype**  
Variable types

- "MSK\_VAR\_TYPE\_CONT"  
Is a continuous variable.
- "MSK\_VAR\_TYPE\_INT"  
Is an integer variable.

## 15.8 Nonlinear interfaces (obsolete)

---

**Important:** This is a legacy document for users familiar with SCopt, DGopt, EXPopt, mskenopt, mskscopt and mskgpopt from previous versions of **MOSEK**. These interfaces have now been removed. We assume familiarity with documentation included in version 8. All problems expressible with this interface can (and should) be reformulated using the exponential cone and power cones.

New users should formulate problems involving powers, logarithms and exponentials directly in conic form.

---

### Conversion tutorial

We recommend converting all nonlinear problems using SCopt, DGopt, EXPopt, mskenopt, mskscopt and mskgpopt into conic form. Depending on the values of  $f, g, h$  either the epigraph or hypograph of a SCopt function if convex, and a bounding variable can be introduced following the basic rules below. We assume all variables are within safe bounds where the SCopt operators are defined and convex. We also assume  $f > 0$ .

A more comprehensive modeling guide for these types of problems can be found in the **MOSEK Modeling Cookbook**.











```
general
x1 x2
binary
x3 x4
```

Again, all variables listed in the binary or general sections must occur in either the objective or a constraint.

### Terminating Section

Finally, an LP formatted file must be terminated with the keyword

```
end
```

## 16.1.2 LP File Examples

### Linear example lo1.lp

```
\ File: lo1.lp
maximize
obj: 3 x1 + x2 + 5 x3 + x4
subject to
c1: 3 x1 + x2 + 2 x3 = 30
c2: 2 x1 + x2 + 3 x3 + x4 >= 15
c3: 2 x2 + 3 x4 <= 25
bounds
0 <= x1 <= +infinity
0 <= x2 <= 10
0 <= x3 <= +infinity
0 <= x4 <= +infinity
end
```

### Mixed integer example milo1.lp

```
maximize
obj: x1 + 6.4e-01 x2
subject to
c1: 5e+01 x1 + 3.1e+01 x2 <= 2.5e+02
c2: 3e+00 x1 - 2e+00 x2 >= -4e+00
bounds
0 <= x1 <= +infinity
0 <= x2 <= +infinity
general
x1 x2
end
```







### Linear example lo1.mps

A concrete example of a MPS file is presented below:

```
* File: lo1.mps
NAME          lo1
OBJSENSE
    MAX
ROWS
    N  obj
    E  c1
    G  c2
    L  c3
COLUMNS
    x1      obj      3
    x1      c1       3
    x1      c2       2
    x2      obj      1
    x2      c1       1
    x2      c2       1
    x2      c3       2
    x3      obj      5
    x3      c1       2
    x3      c2       3
    x4      obj      1
    x4      c2       1
    x4      c3       3
RHS
    rhs     c1      30
    rhs     c2      15
    rhs     c3      25
RANGES
BOUNDS
    UP bound    x2      10
ENDATA
```

Subsequently each individual section in the MPS format is discussed.

#### NAME (optional)

In this section a name ([name]) is assigned to the problem.

#### OBJSENSE (optional)

This is an optional section that can be used to specify the sense of the objective function. The **OBJSENSE** section contains one line at most which can be one of the following:

```
MIN
MINIMIZE
MAX
MAXIMIZE
```

It should be obvious what the implication is of each of these four lines.

































```

[variables disallow_new_variables]
  x1 x2 x3 x4
[/variables]

[objective maximize 'obj']
  3 x1 + x2 + 5 x3 + x4
[/objective]

[constraints]
  [con 'c1'] 3 x1 +   x2 + 2 x3           = 30 [/con]
  [con 'c2'] 2 x1 +   x2 + 3 x3 +   x4 >= 15 [/con]
  [con 'c3']      2 x2           + 3 x4 <= 25 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
  [b] 0 <= x2 <= 10 [/b]
[/bounds]

```

### Quadratic Example qo1.opf

An example of a quadratic optimization problem is

$$\begin{aligned}
 &\text{minimize} && x_1^2 + 0.1x_2^2 + x_3^2 - x_1x_3 - x_2 \\
 &\text{subject to} && 1 \leq x_1 + x_2 + x_3, \\
 &&& x \geq 0.
 \end{aligned}$$

This can be formulated in `opf` as shown below.

Listing 16.2: Example of an OPF file for a quadratic problem.

```

[comment]
  The qo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 3 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
  [hint NUMQNZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3
[/variables]

[objective minimize 'obj']
  # The quadratic terms are often written with a factor of 1/2 as here,
  # but this is not required.

  - x2 + 0.5 ( 2.0 x1 ^ 2 - 2.0 x3 * x1 + 0.2 x2 ^ 2 + 2.0 x3 ^ 2 )
[/objective]

[constraints]
  [con 'c1'] 1.0 <= x1 + x2 + x3 [/con]
[/constraints]

```



### Mixed Integer Example milo1.opf

Consider the mixed integer problem:

$$\begin{array}{llll} \text{maximize} & x_0 + 0.64x_1 & & \\ \text{subject to} & 50x_0 + 31x_1 & \leq & 250, \\ & 3x_0 - 2x_1 & \geq & -4, \\ & x_0, x_1 \geq 0 & & \text{and integer} \end{array}$$

This can be implemented in OPF with the file in [Listing 16.4](#).

Listing 16.4: Example of an OPF file for a mixed-integer linear problem.

```
[comment]
  The milo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 2 [/hint]
  [hint NUMCON] 2 [/hint]
  [hint NUMANZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2
[/variables]

[objective maximize 'obj']
  x1 + 6.4e-1 x2
[/objective]

[constraints]
  [con 'c1'] 5e+1 x1 + 3.1e+1 x2 <= 2.5e+2 [/con]
  [con 'c2'] -4 <= 3 x1 - 2 x2 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]

[integer]
  x1 x2
[/integer]
```









- The affine expressions of the scalar constraints are defined, for  $i \in \mathcal{I}$ , as

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

in terms of the symmetric matrices,  $F_{ij}$ , and scalars,  $a_{ij}$  and  $b_i$ .

- The affine expressions of the PSD constraints are defined, for  $i \in \mathcal{I}^{PSD}$ , as

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i,$$

in terms of the symmetric matrices,  $H_{ij}$  and  $D_i$ .

### List of cones

The format uses an explicit syntax for symmetric positive semidefinite cones as shown above. For scalar variables and constraints, constructed in vectors, the supported conic domains and their minimum sizes are given as follows.

Table 16.3: Cones available in the CBF format

Name	CBF keyword	Cone family
Free domain	F	linear
Positive orthant	L+	linear
Negative orthant	L-	linear
Fixpoint zero	L=	linear
Quadratic cone	Q	second-order
Rotated quadratic cone	QR	second-order

### 16.4.4 File Format Keywords

#### VER

*Description:* The version of the Conic Benchmark Format used to write the file.

HEADER: None

BODY: One line formatted as:

INT

This is the version number.

Must appear exactly once in a file, as the first keyword.

#### OBJSENSE

*Description:* Define the objective sense.

HEADER: None

BODY: One line formatted as:

STR

having MIN indicates minimize, and MAX indicates maximize. Capital letters are required.

Must appear exactly once in a file.

## PSDVAR

*Description:* Construct the PSD variables.

**HEADER:** One line formatted as:

INT
-----

This is the number of PSD variables in the problem.

**BODY:** A list of lines formatted as:

INT
-----

This indicates the number of rows (equal to the number of columns) in the matrix-valued PSD variable. The number of lines should match the number stated in the header.

## VAR

*Description:* Construct the scalar variables.

**HEADER:** One line formatted as:

INT INT
---------

This is the number of scalar variables, followed by the number of conic domains they are restricted to.

**BODY:** A list of lines formatted as:

STR INT
---------

This indicates the cone name (see [Table 16.3](#)), and the number of scalar variables restricted to this cone. These numbers should add up to the number of scalar variables stated first in the header. The number of lines should match the second number stated in the header.

## INT

*Description:* Declare integer requirements on a selected subset of scalar variables.

**HEADER:** one line formatted as:

INT
-----

This is the number of integer scalar variables in the problem.

**BODY:** a list of lines formatted as:

INT
-----

This indicates the scalar variable index  $j \in \mathcal{J}$ . The number of lines should match the number stated in the header.

Can only be used after the keyword **VAR**.

## PSDCON

*Description:* Construct the PSD constraints.

**HEADER:** One line formatted as:

INT
-----

This is the number of PSD constraints in the problem.

**BODY:** A list of lines formatted as:

INT
-----

This indicates the number of rows (equal to the number of columns) in the matrix-valued affine expression of the PSD constraint. The number of lines should match the number stated in the header.

Can only be used after these keywords: **PSDVAR**, **VAR**.

## CON

*Description:* Construct the scalar constraints.

**HEADER:** One line formatted as:

INT INT
---------

This is the number of scalar constraints, followed by the number of conic domains they restrict to.

**BODY:** A list of lines formatted as:

STR INT
---------

This indicates the cone name (see Table 16.3), and the number of affine expressions restricted to this cone. These numbers should add up to the number of scalar constraints stated first in the header. The number of lines should match the second number stated in the header.

Can only be used after these keywords: PSDVAR, VAR

## OBJCOORD

*Description:* Input sparse coordinates (quadruplets) to define the symmetric matrices  $F_j^{obj}$ , as used in the objective.

**HEADER:** One line formatted as:

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as:

INT INT INT REAL
------------------

This indicates the PSD variable index  $j \in \mathcal{J}^{PSD}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## OBJACoord

*Description:* Input sparse coordinates (pairs) to define the scalars,  $a_j^{obj}$ , as used in the objective.

**HEADER:** One line formatted as:

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as:

INT REAL
----------

This indicates the scalar variable index  $j \in \mathcal{J}$  and the coefficient value. The number of lines should match the number stated in the header.

## OBJBCoord

*Description:* Input the scalar,  $b^{obj}$ , as used in the objective.

**HEADER:** None.

**BODY:** One line formatted as:

REAL
------

This indicates the coefficient value.

## FCOORD

*Description:* Input sparse coordinates (quintuplets) to define the symmetric matrices,  $F_{ij}$ , as used in the scalar constraints.

**HEADER:** One line formatted as:

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as:

INT INT INT INT REAL
----------------------

This indicates the scalar constraint index  $i \in \mathcal{I}$ , the PSD variable index  $j \in \mathcal{J}^{PSD}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## ACOORD

*Description:* Input sparse coordinates (triplets) to define the scalars,  $a_{ij}$ , as used in the scalar constraints.

**HEADER:** One line formatted as:

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as:

INT INT REAL
--------------

This indicates the scalar constraint index  $i \in \mathcal{I}$ , the scalar variable index  $j \in \mathcal{J}$  and the coefficient value. The number of lines should match the number stated in the header.

## BCOORD

*Description:* Input sparse coordinates (pairs) to define the scalars,  $b_i$ , as used in the scalar constraints.

**HEADER:** One line formatted as:

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as:

INT REAL
----------

This indicates the scalar constraint index  $i \in \mathcal{I}$  and the coefficient value. The number of lines should match the number stated in the header.

## HCOORD

*Description:* Input sparse coordinates (quintuplets) to define the symmetric matrices,  $H_{ij}$ , as used in the PSD constraints.

**HEADER:** One line formatted as:

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as

INT INT INT INT REAL
----------------------

This indicates the PSD constraint index  $i \in \mathcal{I}^{PSD}$ , the scalar variable index  $j \in \mathcal{J}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## DCOORD

*Description:* Input sparse coordinates (quadruplets) to define the symmetric matrices,  $D_i$ , as used in the PSD constraints.

**HEADER:** One line formatted as

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as:

INT INT INT REAL
------------------

This indicates the PSD constraint index  $i \in \mathcal{I}^{PSD}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## CHANGE

Start of a new instance specification based on changes to the previous. Can be interpreted as the end of file when the hotstart-sequence is unsupported or undesired.

**BODY:** None

**Header:** None

## 16.4.5 CBF Format Examples

### Minimal Working Example

The conic optimization problem (16.11), has three variables in a quadratic cone - first one is integer - and an affine expression in domain 0 (equality constraint).

$$\begin{aligned} & \text{minimize} && 5.1 x_0 \\ & \text{subject to} && 6.2 x_1 + 7.3 x_2 - 8.4 \in \{0\} \\ & && x \in \mathcal{Q}^3, x_0 \in \mathbb{Z}. \end{aligned} \tag{16.11}$$

Its formulation in the Conic Benchmark Format begins with the version of the CBF format used, to safeguard against later revisions.

VER
1

Next follows the problem structure, consisting of the objective sense, the number and domain of variables, the indices of integer variables, and the number and domain of scalar-valued affine expressions (i.e., the equality constraint).

OBJSENSE
MIN
VAR
3 1
Q 3
INT
1
0
CON
1 1
L= 1

Finally follows the problem data, consisting of the coefficients of the objective, the coefficients of the constraints, and the constant terms of the constraints. All data is specified on a sparse coordinate form.

```
OBJCOORD
```

```
1
0 5.1
```

```
ACCOORD
```

```
2
0 1 6.2
0 2 7.3
```

```
BCCOORD
```

```
1
0 -8.4
```

This concludes the example.

### Mixing Linear, Second-order and Semidefinite Cones

The conic optimization problem (16.12), has a semidefinite cone, a quadratic cone over unordered subindices, and two equality constraints.

$$\begin{aligned} & \text{minimize} && \left\langle \begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}, X_1 \right\rangle + x_1 \\ & \text{subject to} && \left\langle \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 &= 1.0, \\ & && \left\langle \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, X_1 \right\rangle + x_0 + x_2 &= 0.5, \\ & && x_1 \geq \sqrt{x_0^2 + x_2^2}, \\ & && X_1 \succeq \mathbf{0}. \end{aligned} \tag{16.12}$$

The equality constraints are easily rewritten to the conic form,  $(g_0, g_1) \in \{0\}^2$ , by moving constants such that the right-hand-side becomes zero. The quadratic cone does not fit under the `VAR` keyword in this variable permutation. Instead, it takes a scalar constraint  $(g_2, g_3, g_4) = (x_1, x_0, x_2) \in \mathcal{Q}^3$ , with scalar variables constructed as  $(x_0, x_1, x_2) \in \mathbb{R}^3$ . Its formulation in the CBF format is reported in the following list

```
# File written using this version of the Conic Benchmark Format:
#   | Version 1.
VER
1

# The sense of the objective is:
#   | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#   | Three times three.
PSDVAR
1
3

# Three scalar variables in this one conic domain:
#   | Three are free.
VAR
3 1
```

(continues on next page)

```

F 3

# Five scalar constraints with affine expressions in two conic domains:
#   | Two are fixed to zero.
#   | Three are in conic quadratic domain.
CON
5 2
L= 2
Q 3

# Five coordinates in  $F^{\{obj\}}_j$  coefficients:
#   |  $F^{\{obj\}}[0][0,0] = 2.0$ 
#   |  $F^{\{obj\}}[0][1,0] = 1.0$ 
#   | and more...
OBJFCOORD
5
0 0 0 2.0
0 1 0 1.0
0 1 1 2.0
0 2 1 1.0
0 2 2 2.0

# One coordinate in  $a^{\{obj\}}_j$  coefficients:
#   |  $a^{\{obj\}}[1] = 1.0$ 
OBJACOORD
1
1 1.0

# Nine coordinates in  $F_{ij}$  coefficients:
#   |  $F[0,0][0,0] = 1.0$ 
#   |  $F[0,0][1,1] = 1.0$ 
#   | and more...
FCOORD
9
0 0 0 0 1.0
0 0 1 1 1.0
0 0 2 2 1.0
1 0 0 0 1.0
1 0 1 0 1.0
1 0 2 0 1.0
1 0 1 1 1.0
1 0 2 1 1.0
1 0 2 2 1.0

# Six coordinates in  $a_{ij}$  coefficients:
#   |  $a[0,1] = 1.0$ 
#   |  $a[1,0] = 1.0$ 
#   | and more...
ACOORD
6
0 1 1.0
1 0 1.0
1 2 1.0
2 1 1.0
3 0 1.0
4 2 1.0

```

(continues on next page)

(continued from previous page)

```
# Two coordinates in b_i coefficients:
#      | b[0] = -1.0
#      | b[1] = -0.5
BCOORD
2
0 -1.0
1 -0.5
```

### Mixing Semidefinite Variables and Linear Matrix Inequalities

The standard forms in semidefinite optimization are usually based either on semidefinite variables or linear matrix inequalities. In the CBF format, both forms are supported and can even be mixed as shown in.

$$\begin{aligned} \text{minimize} \quad & \left\langle \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 + x_2 + 1 \\ \text{subject to} \quad & \left\langle \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, X_1 \right\rangle - x_1 - x_2 \geq 0.0, \\ & x_1 \begin{bmatrix} 0 & 1 \\ 1 & 3 \end{bmatrix} + x_2 \begin{bmatrix} 3 & 1 \\ 1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \preceq \mathbf{0}, \\ & X_1 \succeq \mathbf{0}. \end{aligned} \tag{16.13}$$

Its formulation in the CBF format is written in what follows

```
# File written using this version of the Conic Benchmark Format:
#      | Version 1.
VER
1

# The sense of the objective is:
#      | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#      | Two times two.
PSDVAR
1
2

# Two scalar variables in this one conic domain:
#      | Two are free.
VAR
2 1
F 2

# One PSD constraint of this size:
#      | Two times two.
PSDCON
1
2

# One scalar constraint with an affine expression in this one conic domain:
#      | One is greater than or equal to zero.
CON
1 1
```

(continues on next page)

```

L+ 1

# Two coordinates in  $F^{\{obj\}}_j$  coefficients:
#   |  $F^{\{obj\}}[0][0,0] = 1.0$ 
#   |  $F^{\{obj\}}[0][1,1] = 1.0$ 
OBJFCOORD
2
0 0 0 1.0
0 1 1 1.0

# Two coordinates in  $a^{\{obj\}}_j$  coefficients:
#   |  $a^{\{obj\}}[0] = 1.0$ 
#   |  $a^{\{obj\}}[1] = 1.0$ 
OBJACOORD
2
0 1.0
1 1.0

# One coordinate in  $b^{\{obj\}}$  coefficient:
#   |  $b^{\{obj\}} = 1.0$ 
OBJBCOORD
1.0

# One coordinate in  $F_{ij}$  coefficients:
#   |  $F[0,0][1,0] = 1.0$ 
FCOORD
1
0 0 1 0 1.0

# Two coordinates in  $a_{ij}$  coefficients:
#   |  $a[0,0] = -1.0$ 
#   |  $a[0,1] = -1.0$ 
ACCOORD
2
0 0 -1.0
0 1 -1.0

# Four coordinates in  $H_{ij}$  coefficients:
#   |  $H[0,0][1,0] = 1.0$ 
#   |  $H[0,0][1,1] = 3.0$ 
#   | and more...
HCOORD
4
0 0 1 0 1.0
0 0 1 1 3.0
0 1 0 0 3.0
0 1 1 0 1.0

# Two coordinates in  $D_i$  coefficients:
#   |  $D[0][0,0] = -1.0$ 
#   |  $D[0][1,1] = -1.0$ 
DCOORD
2
0 0 0 -1.0
0 1 1 -1.0

```

## Optimization Over a Sequence of Objectives

The linear optimization problem (16.14), is defined for a sequence of objectives such that hotstarting from one to the next might be advantages.

$$\begin{aligned} & \text{maximize}_k && g_k^{obj} \\ & \text{subject to} && 50x_0 + 31 \leq 250, \\ & && 3x_0 - 2x_1 \geq -4, \\ & && x \in \mathbb{R}_+^2, \end{aligned} \tag{16.14}$$

given,

1.  $g_0^{obj} = x_0 + 0.64x_1$ .
2.  $g_1^{obj} = 1.11x_0 + 0.76x_1$ .
3.  $g_2^{obj} = 1.11x_0 + 0.85x_1$ .

Its formulation in the CBF format is reported in Listing 16.5.

Listing 16.5: Problem (16.14) in CBF format.

```
# File written using this version of the Conic Benchmark Format:
#   | Version 1.
VER
1

# The sense of the objective is:
#   | Maximize.
OBJSENSE
MAX

# Two scalar variables in this one conic domain:
#   | Two are nonnegative.
VAR
2 1
L+ 2

# Two scalar constraints with affine expressions in these two conic domains:
#   | One is in the nonpositive domain.
#   | One is in the nonnegative domain.
CON
2 2
L- 1
L+ 1

# Two coordinates in a^{obj}_j coefficients:
#   | a^{obj}[0] = 1.0
#   | a^{obj}[1] = 0.64
OBJACoord
2
0 1.0
1 0.64

# Four coordinates in a_ij coefficients:
#   | a[0,0] = 50.0
#   | a[1,0] = 3.0
#   | and more...
ACoord
4
```

(continues on next page)

```

0 0 50.0
1 0 3.0
0 1 31.0
1 1 -2.0

# Two coordinates in b_i coefficients:
#     | b[0] = -250.0
#     | b[1] = 4.0
BCOORD
2
0 -250.0
1 4.0

# New problem instance defined in terms of changes.
CHANGE

# Two coordinate changes in a^{obj}_j coefficients. Now it is:
#     | a^{obj}[0] = 1.11
#     | a^{obj}[1] = 0.76
OBJACORD
2
0 1.11
1 0.76

# New problem instance defined in terms of changes.
CHANGE

# One coordinate change in a^{obj}_j coefficients. Now it is:
#     | a^{obj}[0] = 1.11
#     | a^{obj}[1] = 0.85
OBJACORD
1
1 0.85

```

## 16.5 The PTF Format

The PTF format is a new human-readable, natural text format. Its features and structure are similar to the *OPF* format, with the difference that the PTF format **does** support semidefinite terms.

### 16.5.1 The overall format

The format is indentation based, where each section is started by a head line and followed by a section body with deeper indentation than the head line. For example:

```

Header line
  Body line 1
  Body line 1
  Body line 1

```

Section can also be nested:

```

Header line A
  Body line in A
  Header line A.1
    Body line in A.1

```

(continues on next page)

```

    Body line in A.1
Body line in A

```

The indentation of blank lines is ignored, so a subsection can contain a blank line with no indentation. The character # defines a line comment and anything between the # character and the end of the line is ignored.

In a PTF file, the first section must be a **Task** section. The order of the remaining section is arbitrary, and sections may occur multiple times or not at all.

**MOSEK** will ignore any top-level section it does not recognize.

## Names

In the description of the format we use following definitions for name strings:

```

NAME: PLAIN_NAME | QUOTED_NAME
PLAIN_NAME: [a-zA-Z_] [a-zA-Z0-9_-.!|]
QUOTED_NAME: '"' ( [^'\\r\n] | "\\" ( [\\rn] | "x" [0-9a-fA-F] [0-9a-fA-F] ) ) * '"'

```

## Expressions

An expression is a sum of terms. A term is either a linear term (a coefficient and a variable name, where the coefficient can be left out if it is 1.0), or a matrix inner product.

An expression:

```

EXPR: EMPTY | [+]? TERM ( [+]? TERM ) *
TERM: LINEAR_TERM | MATRIX_TERM

```

A linear term

```

LINEAR_TERM: FLOAT? NAME

```

A matrix term

```

MATRIX_TERM: "<" FLOAT? NAME ( [+]? FLOAT? NAME ) * ";" NAME ">"

```

Here the right-hand name is the name of a (semidefinite) matrix variable, and the left-hand side is a sum of symmetric matrixes. The actual matrixes are defined in a separate section.

Expressions can span multiple lines by giving subsequent lines a deeper indentation.

For example following two section are equivalent:

```

# Everything on one line:
x1 + x2 + x3 + x4

# Split into multiple lines:
x1
+ x2
+ x3
+ x4

```

### 16.5.2 Task section

The first section of the file must be a **Task**. The text in this section is not used and may contain comments, or meta-information from the writer or about the content.

Format:

```
Task NAME
  Anything goes here...
```

NAME is a the task name.

### 16.5.3 Objective section

The **Objective** section defines the objective name, sense and function. The format:

```
"Objective" NAME?
  ( "Minimize" | "Maximize" ) EXPR
```

For example:

```
Objective 'obj'
  Minimize x1 + 0.2 x2 + < M1 ; X1 >
```

### 16.5.4 Constraints section

The constraints section defines a series of constraints. A constraint defines a term  $A \cdot x + b \in K$ . For linear constraints A is just one row, while for conic constraints it can be multiple rows. If a constraint spans multiple rows these can either be written inline separated by semi-colons, or each expression in a separate sub-section.

Simple linear constraints:

```
"Constraints"
NAME? "[" [-+] (FLOAT | "Inf") (";" [-+] (FLOAT | "Inf"))? "]" EXPR
```

If the brackets contain two values, they are used as upper and lower bounds. If they contain one value the constraint is an equality.

For example:

```
Constraints
'c1' [0;10] x1 + x2 + x3
[0] x1 + x2 + x3
```

Constraint blocks put the expression either in a subsection or inline. The cone type (domain) is written in the brackets, and **MOSEK** currently supports following types:

- SOC(N) Second order cone of dimension N
- RSOC(N) Rotated second order cone of dimension N
- PSD(N) Symmetric positive semidefinite cone of dimension N. This contains  $N*(N+1)/2$  elements.
- PEXP Primal exponential cone of dimension 3
- DEXP Dual exponential cone of dimension 3
- PPOW(N,P) Primal power cone of dimension N with parameter P
- DPOW(N,P) Dual power cone of dimension N with parameter P
- ZERO(N) The zero-cone of dimension N.

```
"Constraints"
NAME? "[" DOMAIN "]" EXPR_LIST
```

For example:

```
Constraints
'K1' [SOC(3)] x1 + x2 ; x2 + x3 ; x3 + x1
'K2' [RSOC(3)]
    x1 + x2
    x2 + x3
    x3 + x1
```

### 16.5.5 Variables section

Any variable used in an expression must be defined in a variable section. The variable section defines each variable domain.

```
"Variables"
NAME "[" [-+] (FLOAT | "Inf") (";" [-+] (FLOAT | "Inf"))? "]"
NAME "[" DOMAIN "]" NAMES

For example, a linear variable
```

```
Variables
x1 [0;Inf]
```

As with constraints, members of a conic domain can be listed either inline or in a subsection:

```
Variables
k1 [SOC(3)] x1 ; x2 ; x3
k2 [RSOC(3)]
    x1
    x2
    x3
```

### 16.5.6 Integer section

This section contains a list of variables that are integral. For example:

```
Integer
x1 x2 x3
```

### 16.5.7 SymmetricMatrixes section

This section defines the symmetric matrixes used for matrix coefficients in matrix inner product terms. The section lists named matrixes, each with a size and a number of non-zeros. Only non-zeros in the lower triangular part should be defined.

```
"SymmetricMatrixes"
NAME "SYMMAT" "(" INT ")" ( "(" INT "," INT "," FLOAT ")" ) *
...
```

For example:

```
SymmetricMatrixes
M1 SYMMAT(3) (0,0,1.0) (1,1,2.0) (2,1,0.5)
M2 SYMMAT(3)
    (0,0,1.0)
    (1,1,2.0)
    (2,1,0.5)
```

### 16.5.8 Solutions section

Each subsection defines a solution. A solution defines for each constraint and for each variable exactly one primal value and either one (for conic domains) or two (for linear domains) dual values. The values follow the same logic as in the **MOSEK C API**. A primal and a dual solution status defines the meaning of the values primal and dual (solution, certificate, unknown, etc.)

The format is this:

```
"Solutions"
  "Solution" WHICH SOL
    "ProblemStatus" PROSTA PROSTA?
  "SolutionStatus" SOLSTA SOLSTA?
  "Objective" FLOAT FLOAT
  "Variables"
    # Linear variable status: level, slx, sux
    NAME "[" STATUS "]" FLOAT (FLOAT FLOAT)?
    # Conic variable status: level, snx
    NAME
      "[" STATUS "]" FLOAT FLOAT?
    ...
  "Constraints"
    # Linear variable status: level, slx, sux
    NAME "[" STATUS "]" FLOAT (FLOAT FLOAT)?
    # Conic variable status: level, snx
    NAME
      "[" STATUS "]" FLOAT FLOAT?
    ...
```

Following values for WHICH SOL are supported:

- **interior** Interior solution, the result of an interior-point solver.
- **basic** Basic solution, as produced by a simplex solver.
- **integer** Integer solution, the solution to a mixed-integer problem. This does not define a dual solution.

Following values for PROSTA are supported:

- **unknown** The problem status is unknown
- **feasible** The problem has been proven feasible
- **infeasible** The problem has been proven infeasible
- **illposed** The problem has been proved to be ill posed
- **infeasible\_or\_unbounded** The problem is infeasible or unbounded

Following values for SOLSTA are supported:

- **unknown** The solution status is unknown
- **feasible** The solution is feasible
- **optimal** The solution is optimal
- **infeas\_cert** The solution is a certificate of infeasibility
- **illposed\_cert** The solution is a certificate of illposedness

Following values for STATUS are supported:

- **unknown** The value is unknown
- **super\_basic** The value is super basic

- `at_lower` The value is basic and at its lower bound
- `at_upper` The value is basic and at its upper bound
- `fixed` The value is basic fixed
- `infinite` The value is at infinity

## 16.6 The Task Format

The Task format is **MOSEK**'s native binary format. It contains a complete image of a **MOSEK** task, i.e.

- Problem data: Linear, conic, semidefinite and quadratic data
- Problem item names: Variable names, constraints names, cone names etc.
- Parameter settings
- Solutions

There are a few things to be aware of:

- Status of a solution read from a file will *always* be unknown.
- Parameter settings in a task file *always override* any parameters set on the command line or in a parameter file.

The format is based on the *TAR* (USTar) file format. This means that the individual pieces of data in a `.task` file can be examined by unpacking it as a *TAR* file. Please note that the inverse may not work: Creating a file using *TAR* will most probably not create a valid **MOSEK** Task file since the order of the entries is important.

## 16.7 The JSON Format

**MOSEK** provides the possibility to read/write problems in valid JSON format.

JSON (JavaScript Object Notation) is a lightweight data-interchange format. It is easy for humans to read and write. It is easy for machines to parse and generate. It is based on a subset of the JavaScript Programming Language, Standard ECMA-262 3rd Edition - December 1999. JSON is a text format that is completely language independent but uses conventions that are familiar to programmers of the C-family of languages, including C, C++, C#, Java, JavaScript, Perl, Python, and many others. These properties make JSON an ideal data-interchange language.

The official JSON website <http://www.json.org> provides plenty of information along with the format definition.

**MOSEK** defines two JSON-like formats:

- `jtask`
- `jsol`

Despite being text-based human-readable formats, *jtask* and *jsol* files will include no indentation and no new-lines, in order to keep the files as compact as possible. We therefore strongly advise to use JSON viewer tools to inspect *jtask* and *jsol* files.

### 16.7.1 *jtask* format

It stores a problem instance. The *jtask* format contains the same information as a *task format*. Even though a *jtask* file is human-readable, we do not recommend users to create it by hand, but to rely on MOSEK.

### 16.7.2 *jsol* format

It stores a problem solution. The *jsol* format contains all solutions and information items.

### 16.7.3 A *jtask* example

In Listing 16.6 we present a file in the *jtask* format that corresponds to the sample problem from 1o1.1p. The listing has been formatted for readability.

Listing 16.6: A formatted *jtask* file for the 1o1.1p example.

```
{
  "$schema": "http://mosek.com/json/schema#",
  "Task/INFO": {
    "taskname": "1o1",
    "numvar": 4,
    "numcon": 3,
    "numcone": 0,
    "numbarvar": 0,
    "numanz": 9,
    "numsymmat": 0,
    "mosekver": [
      8,
      0,
      0,
      9
    ]
  },
  "Task/data": {
    "var": {
      "name": [
        "x1",
        "x2",
        "x3",
        "x4"
      ],
      "bk": [
        "lo",
        "ra",
        "lo",
        "lo"
      ],
      "b1": [
        0.0,
        0.0,
        0.0,
        0.0
      ],
      "bu": [
        1e+30,
        1e+1,
        1e+30,

```

(continues on next page)

```

        1e+30
    ],
    "type": [
        "cont",
        "cont",
        "cont",
        "cont"
    ]
},
"con": {
    "name": [
        "c1",
        "c2",
        "c3"
    ],
    "bk": [
        "fx",
        "lo",
        "up"
    ],
    "bl": [
        3e+1,
        1.5e+1,
        -1e+30
    ],
    "bu": [
        3e+1,
        1e+30,
        2.5e+1
    ]
},
"objective": {
    "sense": "max",
    "name": "obj",
    "c": {
        "subj": [
            0,
            1,
            2,
            3
        ],
        "val": [
            3e+0,
            1e+0,
            5e+0,
            1e+0
        ]
    },
    "cfix": 0.0
},
"A": {
    "subi": [
        0,
        0,
        0,
        1,

```

```

        1,
        1,
        1,
        2,
        2
    ],
    "subj": [
        0,
        1,
        2,
        0,
        1,
        2,
        3,
        1,
        3
    ],
    "val": [
        3e+0,
        1e+0,
        2e+0,
        2e+0,
        1e+0,
        3e+0,
        1e+0,
        2e+0,
        3e+0
    ]
}
},
"Task/parameters": {
    "iparam": {
        "ANA_SOL_BASIS": "ON",
        "ANA_SOL_PRINT_VIOLATED": "OFF",
        "AUTO_SORT_A_BEFORE_OPT": "OFF",
        "AUTO_UPDATE_SOL_INFO": "OFF",
        "BASIS_SOLVE_USE_PLUS_ONE": "OFF",
        "BI_CLEAN_OPTIMIZER": "OPTIMIZER_FREE",
        "BI_IGNORE_MAX_ITER": "OFF",
        "BI_IGNORE_NUM_ERROR": "OFF",
        "BI_MAX_ITERATIONS": 1000000,
        "CACHE_LICENSE": "ON",
        "CHECK_CONVEXITY": "CHECK_CONVEXITY_FULL",
        "COMPRESS_STATFILE": "ON",
        "CONCURRENT_NUM_OPTIMIZERS": 2,
        "CONCURRENT_PRIORITY_DUAL_SIMPLEX": 2,
        "CONCURRENT_PRIORITY_FREE_SIMPLEX": 3,
        "CONCURRENT_PRIORITY_INTPNT": 4,
        "CONCURRENT_PRIORITY_PRIMAL_SIMPLEX": 1,
        "FEASREPAIR_OPTIMIZE": "FEASREPAIR_OPTIMIZE_NONE",
        "INFEAS_GENERIC_NAMES": "OFF",
        "INFEAS_PREFER_PRIMAL": "ON",
        "INFEAS_REPORT_AUTO": "OFF",
        "INFEAS_REPORT_LEVEL": 1,
        "INTPNT_BASIS": "BI_ALWAYS",
        "INTPNT_DIFF_STEP": "ON",

```

```

"INTPNT_FACTOR_DEBUG_LVL":0,
"INTPNT_FACTOR_METHOD":0,
"INTPNT_HOTSTART":"INTPNT_HOTSTART_NONE",
"INTPNT_MAX_ITERATIONS":400,
"INTPNT_MAX_NUM_COR":-1,
"INTPNT_MAX_NUM_REFINEMENT_STEPS":-1,
"INTPNT_OFF_COL_TRH":40,
"INTPNT_ORDER_METHOD":"ORDER_METHOD_FREE",
"INTPNT_REGULARIZATION_USE":"ON",
"INTPNT_SCALING":"SCALING_FREE",
"INTPNT_SOLVE_FORM":"SOLVE_FREE",
"INTPNT_STARTING_POINT":"STARTING_POINT_FREE",
"LIC_TRH_EXPIRY_WRN":7,
"LICENSE_DEBUG":"OFF",
"LICENSE_PAUSE_TIME":0,
"LICENSE_SUPPRESS_EXPIRE_WRNS":"OFF",
"LICENSE_WAIT":"OFF",
"LOG":10,
"LOG_ANA_PRO":1,
"LOG_BI":4,
"LOG_BI_FREQ":2500,
"LOG_CHECK_CONVEXITY":0,
"LOG_CONCURRENT":1,
"LOG_CUT_SECOND_OPT":1,
"LOG_EXPAND":0,
"LOG_FACTOR":1,
"LOG_FEAS_REPAIR":1,
"LOG_FILE":1,
"LOG_HEAD":1,
"LOG_INFEAS_ANA":1,
"LOG_INTPNT":4,
"LOG_MIO":4,
"LOG_MIO_FREQ":1000,
"LOG_OPTIMIZER":1,
"LOG_ORDER":1,
"LOG_PRESOLVE":1,
"LOG_RESPONSE":0,
"LOG_SENSITIVITY":1,
"LOG_SENSITIVITY_OPT":0,
"LOG_SIM":4,
"LOG_SIM_FREQ":1000,
"LOG_SIM_MINOR":1,
"LOG_STORAGE":1,
"MAX_NUM_WARNINGS":10,
"MIO_BRANCH_DIR":"BRANCH_DIR_FREE",
"MIO_CONSTRUCT_SOL":"OFF",
"MIO_CUT_CLIQUE":"ON",
"MIO_CUT_CMIR":"ON",
"MIO_CUT_GMI":"ON",
"MIO_CUT_KNAPSACK_COVER":"OFF",
"MIO_HEURISTIC_LEVEL":-1,
"MIO_MAX_NUM_BRANCHES":-1,
"MIO_MAX_NUM_RELAXS":-1,
"MIO_MAX_NUM_SOLUTIONS":-1,
"MIO_MODE":"MIO_MODE_SATISFIED",
"MIO_MT_USER_CB":"ON",

```

```

"MIO_NODE_OPTIMIZER": "OPTIMIZER_FREE",
"MIO_NODE_SELECTION": "MIO_NODE_SELECTION_FREE",
"MIO_PERSPECTIVE_REFORMULATE": "ON",
"MIO_PROBING_LEVEL": -1,
"MIO_RINS_MAX_NODES": -1,
"MIO_ROOT_OPTIMIZER": "OPTIMIZER_FREE",
"MIO_ROOT_REPEAT_PRESOLVE_LEVEL": -1,
"MT_SPINCOUNT": 0,
"NUM_THREADS": 0,
"OPF_MAX_TERMS_PER_LINE": 5,
"OPF_WRITE_HEADER": "ON",
"OPF_WRITE_HINTS": "ON",
"OPF_WRITE_PARAMETERS": "OFF",
"OPF_WRITE_PROBLEM": "ON",
"OPF_WRITE_SOL_BAS": "ON",
"OPF_WRITE_SOL_ITG": "ON",
"OPF_WRITE_SOL_ITR": "ON",
"OPF_WRITE_SOLUTIONS": "OFF",
"OPTIMIZER": "OPTIMIZER_FREE",
"PARAM_READ_CASE_NAME": "ON",
"PARAM_READ_IGN_ERROR": "OFF",
"PRESOLVE_ELIMINATOR_MAX_FILL": -1,
"PRESOLVE_ELIMINATOR_MAX_NUM_TRIES": -1,
"PRESOLVE_LEVEL": -1,
"PRESOLVE_LINDEP_ABS_WORK_TRH": 100,
"PRESOLVE_LINDEP_REL_WORK_TRH": 100,
"PRESOLVE_LINDEP_USE": "ON",
"PRESOLVE_MAX_NUM_REDUCTIONS": -1,
"PRESOLVE_USE": "PRESOLVE_MODE_FREE",
"PRIMAL_REPAIR_OPTIMIZER": "OPTIMIZER_FREE",
"QO_SEPARABLE_REFORMULATION": "OFF",
"READ_DATA_COMPRESSED": "COMPRESS_FREE",
"READ_DATA_FORMAT": "DATA_FORMAT_EXTENSION",
"READ_DEBUG": "OFF",
"READ_KEEP_FREE_CON": "OFF",
"READ_LP_DROP_NEW_VARS_IN_BOU": "OFF",
"READ_LP_QUOTED_NAMES": "ON",
"READ_MPS_FORMAT": "MPS_FORMAT_FREE",
"READ_MPS_WIDTH": 1024,
"READ_TASK_IGNORE_PARAM": "OFF",
"SENSITIVITY_ALL": "OFF",
"SENSITIVITY_OPTIMIZER": "OPTIMIZER_FREE_SIMPLEX",
"SENSITIVITY_TYPE": "SENSITIVITY_TYPE_BASIS",
"SIM_BASIS_FACTOR_USE": "ON",
"SIM_DEGEN": "SIM_DEGEN_FREE",
"SIM_DUAL_CRASH": 90,
"SIM_DUAL_PHASEONE_METHOD": 0,
"SIM_DUAL_RESTRICT_SELECTION": 50,
"SIM_DUAL_SELECTION": "SIM_SELECTION_FREE",
"SIM_EXPLOIT_DUPVEC": "SIM_EXPLOIT_DUPVEC_OFF",
"SIM_HOTSTART": "SIM_HOTSTART_FREE",
"SIM_HOTSTART_LU": "ON",
"SIM_INTEGER": 0,
"SIM_MAX_ITERATIONS": 10000000,
"SIM_MAX_NUM_SETBACKS": 250,
"SIM_NON_SINGULAR": "ON",

```

```

"SIM_PRIMAL_CRASH":90,
"SIM_PRIMAL_PHASEONE_METHOD":0,
"SIM_PRIMAL_RESTRICT_SELECTION":50,
"SIM_PRIMAL_SELECTION":"SIM_SELECTION_FREE",
"SIM_REFACTOR_FREQ":0,
"SIM_REFORMULATION":"SIM_REFORMULATION_OFF",
"SIM_SAVE_LU":"OFF",
"SIM_SCALING":"SCALING_FREE",
"SIM_SCALING_METHOD":"SCALING_METHOD_POW2",
"SIM_SOLVE_FORM":"SOLVE_FREE",
"SIM_STABILITY_PRIORITY":50,
"SIM_SWITCH_OPTIMIZER":"OFF",
"SOL_FILTER_KEEP_BASIC":"OFF",
"SOL_FILTER_KEEP_RANGED":"OFF",
"SOL_READ_NAME_WIDTH":-1,
"SOL_READ_WIDTH":1024,
"SOLUTION_CALLBACK":"OFF",
"TIMING_LEVEL":1,
"WRITE_BAS_CONSTRAINTS":"ON",
"WRITE_BAS_HEAD":"ON",
"WRITE_BAS_VARIABLES":"ON",
"WRITE_DATA_COMPRESSED":0,
"WRITE_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
"WRITE_DATA_PARAM":"OFF",
"WRITE_FREE_CON":"OFF",
"WRITE_GENERIC_NAMES":"OFF",
"WRITE_GENERIC_NAMES_IO":1,
"WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS":"OFF",
"WRITE_IGNORE_INCOMPATIBLE_ITEMS":"OFF",
"WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS":"OFF",
"WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS":"OFF",
"WRITE_INT_CONSTRAINTS":"ON",
"WRITE_INT_HEAD":"ON",
"WRITE_INT_VARIABLES":"ON",
"WRITE_LP_FULL_OBJ":"ON",
"WRITE_LP_LINE_WIDTH":80,
"WRITE_LP_QUOTED_NAMES":"ON",
"WRITE_LP_STRICT_FORMAT":"OFF",
"WRITE_LP_TERMS_PER_LINE":10,
"WRITE_MPS_FORMAT":"MPS_FORMAT_FREE",
"WRITE_MPS_INT":"ON",
"WRITE_PRECISION":15,
"WRITE_SOL_BARVARIABLES":"ON",
"WRITE_SOL_CONSTRAINTS":"ON",
"WRITE_SOL_HEAD":"ON",
"WRITE_SOL_IGNORE_INVALID_NAMES":"OFF",
"WRITE_SOL_VARIABLES":"ON",
"WRITE_TASK_INC_SOL":"ON",
"WRITE_XML_MODE":"WRITE_XML_MODE_ROW"
},
"dparam":{
  "ANA_SOL_INFEAS_TOL":1e-6,
  "BASIS_REL_TOL_S":1e-12,
  "BASIS_TOL_S":1e-6,
  "BASIS_TOL_X":1e-6,
  "CHECK_CONVEXITY_REL_TOL":1e-10,

```

```

"DATA_TOL_AIJ":1e-12,
"DATA_TOL_AIJ_HUGE":1e+20,
"DATA_TOL_AIJ_LARGE":1e+10,
"DATA_TOL_BOUND_INF":1e+16,
"DATA_TOL_BOUND_WRN":1e+8,
"DATA_TOL_C_HUGE":1e+16,
"DATA_TOL_CJ_LARGE":1e+8,
"DATA_TOL_QIJ":1e-16,
"DATA_TOL_X":1e-8,
"FEASREPAIR_TOL":1e-10,
"INTPNT_CO_TOL_DFEAS":1e-8,
"INTPNT_CO_TOL_INFEAS":1e-10,
"INTPNT_CO_TOL_MU_RED":1e-8,
"INTPNT_CO_TOL_NEAR_REL":1e+3,
"INTPNT_CO_TOL_PFEAS":1e-8,
"INTPNT_CO_TOL_REL_GAP":1e-7,
"INTPNT_NL_MERIT_BAL":1e-4,
"INTPNT_NL_TOL_DFEAS":1e-8,
"INTPNT_NL_TOL_MU_RED":1e-12,
"INTPNT_NL_TOL_NEAR_REL":1e+3,
"INTPNT_NL_TOL_PFEAS":1e-8,
"INTPNT_NL_TOL_REL_GAP":1e-6,
"INTPNT_NL_TOL_REL_STEP":9.95e-1,
"INTPNT_QO_TOL_DFEAS":1e-8,
"INTPNT_QO_TOL_INFEAS":1e-10,
"INTPNT_QO_TOL_MU_RED":1e-8,
"INTPNT_QO_TOL_NEAR_REL":1e+3,
"INTPNT_QO_TOL_PFEAS":1e-8,
"INTPNT_QO_TOL_REL_GAP":1e-8,
"INTPNT_TOL_DFEAS":1e-8,
"INTPNT_TOL_DSAFE":1e+0,
"INTPNT_TOL_INFEAS":1e-10,
"INTPNT_TOL_MU_RED":1e-16,
"INTPNT_TOL_PATH":1e-8,
"INTPNT_TOL_PFEAS":1e-8,
"INTPNT_TOL_PSAFE":1e+0,
"INTPNT_TOL_REL_GAP":1e-8,
"INTPNT_TOL_REL_STEP":9.999e-1,
"INTPNT_TOL_STEP_SIZE":1e-6,
"LOWER_OBJ_CUT":-1e+30,
"LOWER_OBJ_CUT_FINITE_TRH":-5e+29,
"MIO_DISABLE_TERM_TIME":-1e+0,
"MIO_MAX_TIME":-1e+0,
"MIO_MAX_TIME_APRX_OPT":6e+1,
"MIO_NEAR_TOL_ABS_GAP":0.0,
"MIO_NEAR_TOL_REL_GAP":1e-3,
"MIO_REL_GAP_CONST":1e-10,
"MIO_TOL_ABS_GAP":0.0,
"MIO_TOL_ABS_RELAX_INT":1e-5,
"MIO_TOL_FEAS":1e-6,
"MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT":0.0,
"MIO_TOL_REL_GAP":1e-4,
"MIO_TOL_X":1e-6,
"OPTIMIZER_MAX_TIME":-1e+0,
"PRESOLVE_TOL_ABS_LINDEP":1e-6,
"PRESOLVE_TOL_AIJ":1e-12,

```

```

        "PRESOLVE_TOL_REL_LINDEP":1e-10,
        "PRESOLVE_TOL_S":1e-8,
        "PRESOLVE_TOL_X":1e-8,
        "QCQO_REFORMULATE_REL_DROP_TOL":1e-15,
        "SEMIDEFINITE_TOL_APPROX":1e-10,
        "SIM_LU_TOL_REL_PIV":1e-2,
        "SIMPLEX_ABS_TOL_PIV":1e-7,
        "UPPER_OBJ_CUT":1e+30,
        "UPPER_OBJ_CUT_FINITE_TRH":5e+29
    },
    "sparam":{
        "BAS_SOL_FILE_NAME": "",
        "DATA_FILE_NAME": "examples/tools/data/lo1.mps",
        "DEBUG_FILE_NAME": "",
        "INT_SOL_FILE_NAME": "",
        "ITR_SOL_FILE_NAME": "",
        "MIO_DEBUG_STRING": "",
        "PARAM_COMMENT_SIGN": "%%",
        "PARAM_READ_FILE_NAME": "",
        "PARAM_WRITE_FILE_NAME": "",
        "READ_MPS_BOU_NAME": "",
        "READ_MPS_OBJ_NAME": "",
        "READ_MPS_RAN_NAME": "",
        "READ_MPS_RHS_NAME": "",
        "SENSITIVITY_FILE_NAME": "",
        "SENSITIVITY_RES_FILE_NAME": "",
        "SOL_FILTER_XC_LOW": "",
        "SOL_FILTER_XC_UPR": "",
        "SOL_FILTER_XX_LOW": "",
        "SOL_FILTER_XX_UPR": "",
        "STAT_FILE_NAME": "",
        "STAT_KEY": "",
        "STAT_NAME": "",
        "WRITE_LP_GEN_VAR_NAME": "XMSKGEN"
    }
}
}
}

```

## 16.8 The Solution File Format

MOSEK provides several solution files depending on the problem type and the optimizer used:

- *basis solution file* (extension `.bas`) if the problem is optimized using the simplex optimizer or basis identification is performed,
- *interior solution file* (extension `.sol`) if a problem is optimized using the interior-point optimizer and no basis identification is required,
- *integer solution file* (extension `.int`) if the problem contains integer constrained variables.

All solution files have the format:

NAME	: <problem name>
PROBLEM STATUS	: <status of the problem>
SOLUTION STATUS	: <status of the solution>
OBJECTIVE NAME	: <name of the objective function>
PRIMAL OBJECTIVE	: <primal objective value corresponding to the solution>

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DUAL OBJECTIVE : <dual objective value corresponding to the solution>						
CONSTRAINTS						
INDEX	NAME	AT	ACTIVITY	LOWER LIMIT	UPPER LIMIT	DUAL LOWER
?	<name>	??	<a value>	<a value>	<a value>	<a value>
VARIABLES						
INDEX	NAME	AT	ACTIVITY	LOWER LIMIT	UPPER LIMIT	DUAL LOWER
?	<name>	??	<a value>	<a value>	<a value>	<a value>
↪ CONIC DUAL						
?	<name>	??	<a value>	<a value>	<a value>	<a value>
↪ <a value>						

In the example the fields ? and <> will be filled with problem and solution specific information. As can be observed a solution report consists of three sections, i.e.

- **HEADER** In this section, first the name of the problem is listed and afterwards the problem and solution status are shown. Next the primal and dual objective values are displayed.
- **CONSTRAINTS** For each constraint  $i$  of the form

$$l_i^c \leq \sum_{j=1}^n a_{ij}x_j \leq u_i^c, \quad (16.15)$$

the following information is listed:

- **INDEX**: A sequential index assigned to the constraint by **MOSEK**
- **NAME**: The name of the constraint assigned by the user.
- **AT**: The status of the constraint. In Table 16.4 the possible values of the status keys and their interpretation are shown.

Table 16.4: Status keys.

Status key	Interpretation
UN	Unknown status
BS	Is basic
SB	Is superbasic
LL	Is at the lower limit (bound)
UL	Is at the upper limit (bound)
EQ	Lower limit is identical to upper limit
**	Is infeasible i.e. the lower limit is greater than the upper limit.

- **ACTIVITY**: the quantity  $\sum_{j=1}^n a_{ij}x_j^*$ , where  $x^*$  is the value of the primal solution.
  - **LOWER LIMIT**: the quantity  $l_i^c$  (see (16.15).)
  - **UPPER LIMIT**: the quantity  $u_i^c$  (see (16.15).)
  - **DUAL LOWER**: the dual multiplier corresponding to the lower limit on the constraint.
  - **DUAL UPPER**: the dual multiplier corresponding to the upper limit on the constraint.
- **VARIABLES** The last section of the solution report lists information about the variables. This information has a similar interpretation as for the constraints. However, the column with the header **CONIC DUAL** is included for problems having one or more conic constraints. This column shows the dual variables corresponding to the conic constraints.

**Example: 1o1.sol**

In Listing 16.7 we show the solution file for the 1o1.opf problem.

Listing 16.7: An example of .sol file.

```

NAME      :
PROBLEM STATUS : PRIMAL_AND_DUAL_FEASIBLE
SOLUTION STATUS : OPTIMAL
OBJECTIVE NAME : obj
PRIMAL OBJECTIVE : 8.3333333e+01
DUAL OBJECTIVE : 8.3333332e+01

CONSTRAINTS
INDEX      NAME      AT ACTIVITY      LOWER LIMIT      UPPER LIMIT
↪      DUAL LOWER      DUAL UPPER
0      c1      EQ 3.0000000000000e+01      3.00000000e+01      3.
↪00000000e+01      -0.0000000000000e+00      -2.4999999741653e+00
1      c2      SB 5.3333333049187e+01      1.50000000e+01      NONE
↪      2.09159033069640e-10      -0.0000000000000e+00
2      c3      UL 2.49999999842049e+01      NONE      2.
↪50000000e+01      -0.0000000000000e+00      -3.33333332895108e-01

VARIABLES
INDEX      NAME      AT ACTIVITY      LOWER LIMIT      UPPER LIMIT
↪      DUAL LOWER      DUAL UPPER
0      x1      LL 1.67020427038537e-09      0.00000000e+00      NONE
↪      -4.49999999528054e+00      -0.0000000000000e+00
1      x2      LL 2.93510446211883e-09      0.00000000e+00      1.
↪00000000e+01      -2.16666666494915e+00      6.20868657679896e-10
2      x3      SB 1.49999999899424e+01      0.00000000e+00      NONE
↪      -8.79123177245553e-10      -0.0000000000000e+00
3      x4      SB 8.33333332273115e+00      0.00000000e+00      NONE
↪      -1.69795978848200e-09      -0.0000000000000e+00

```

# Chapter 17

## List of examples

List of examples shipped in the distribution of Optimization Toolbox for MATLAB:

Table 17.1: List of distributed examples

File	Description
advs.m	Advanced simplex hot-start examples
affco1.m	A simple problem using affine conic constraints
affco2.m	A simple problem using affine conic constraints
callback.m	An example of data/progress callback
callback_handler.m	Log handler definition for callback.m
ceo1.m	A simple conic exponential problem
cqo1.m	A simple conic quadratic problem
feasreparex1.m	A simple example of how to repair an infeasible problem
gp1.m	A simple geometric program (GP) in conic form
lo1.m	A simple linear problem using msklpopt
lo2.m	A simple linear problem using mosekopt
lo3.m	A simple linear problem using linprog
mico1.m	A simple mixed-integer conic problem
mi1o1.m	A simple mixed-integer linear problem
mi1o1itsol.m	A simple mixed-integer linear problem with an initial guess
normex.m	Demonstrates least squares and other norm minimization problems
opt_server_sync.m	Uses <b>MOSEK</b> OptServer to solve an optimization problem synchronously
parameters.m	Shows how to set optimizer parameters and read information items
portfolio_1_basic.m	Portfolio optimization - basic Markowitz model
portfolio_2_frontier.m	Portfolio optimization - efficient frontier
portfolio_3_impact.m	Portfolio optimization - market impact costs
portfolio_4_transaction.m	Portfolio optimization - transaction costs
portfolio_5_cardinality.m	Portfolio optimization - cardinality constraints
pow1.m	A simple power cone problem
qcqo1.m	A simple quadratically constrained quadratic problem
qo1.m	A simple quadratic problem
qo2.m	A simple quadratic problem
reoptimization.m	Demonstrate how to modify and re-optimize a linear problem

continues on next page

Table 17.1 – continued from previous page

File	Description
<code>response.m</code>	Demonstrates proper response handling
<code>rlo1.m</code>	Robust linear optimization example, part 1
<code>rlo2.m</code>	Robust linear optimization example, part 2
<code>sdo1.m</code>	A simple semidefinite problem with one matrix variable and a quadratic cone
<code>sdo2.m</code>	A simple semidefinite problem with two matrix variables
<code>sensitivity.m</code>	Sensitivity analysis performed on a small linear problem
<code>sensitivity2.m</code>	Sensitivity analysis performed on a small linear problem
<code>simple.m</code>	A simple I/O example: read problem from a file, solve and write solutions
<code>solutionquality.m</code>	Demonstrates how to examine the quality of a solution

Additional examples can be found on the **MOSEK** website and in other **MOSEK** publications.

# Chapter 18

## Interface changes

The section shows interface-specific changes to the **MOSEK** Optimization Toolbox for MATLAB in version 9.3 compared to version 8. See the [release notes](#) for general changes and new features of the **MOSEK** Optimization Suite.

### 18.1 Backwards compatibility

- **Parameters.** Users who set parameters to tune the performance and numerical properties of the solver (termination criteria, tolerances, solving primal or dual, presolve etc.) are recommended to reevaluate such tuning. It may be that other, or default, parameter settings will be more beneficial in the current version. The hints in [Sec. 8](#) may be useful for some cases.
- Remove all Near solution statuses i.e. `MSK_SOL_STA_NEAR_OPTIMAL`, `MSK_SOL_STA_NEAR_PRIM_INFEAS_CER`, etc. See [Sec. 13.3.3](#).
- All functions related to the general nonlinear optimizer and `Scopt` have been removed. See [Sec. 15.8](#).

### 18.2 New API

Introduced a possibility to specify *affine conic constraints* i.e. conic constraints of the form  $Fx + g \in K$  directly. See [Sec. 6.7](#) and [Sec. 12.5](#) for details.

### 18.3 Parameters

#### Added

- `MSK_IPAR_INTPNT_ORDER_GP_NUM_SEEDS`
- `MSK_IPAR_INTPNT_PURIFY`
- `MSK_IPAR_LOG_INCLUDE_SUMMARY`
- `MSK_IPAR_LOG_LOCAL_INFO`
- `MSK_IPAR_MIO_CONIC_OUTER_APPROXIMATION`
- `MSK_IPAR_MIO_FEASPUMP_LEVEL`
- `MSK_IPAR_MIO_MAX_NUM_ROOT_CUT_ROUNDS`
- `MSK_IPAR_MIO_PROPAGATE_OBJECTIVE_CONSTRAINT`
- `MSK_IPAR_MIO_SEED`
- `MSK_IPAR_OPF_WRITE_LINE_LENGTH`

- *MSK\_IPAR\_PRESOLVE\_MAX\_NUM\_PASS*
- *MSK\_IPAR\_PTF\_WRITE\_TRANSFORM*
- *MSK\_IPAR\_SIM\_SEED*
- *MSK\_IPAR\_WRITE\_COMPRESSION*

#### Removed

- *MSK\_DPAR\_DATA\_TOL\_AIJ*
- *MSK\_DPAR\_INTPNT\_NL\_MERIT\_BAL*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_STEP*
- *MSK\_DPAR\_MIO\_DISABLE\_TERM\_TIME*
- *MSK\_DPAR\_MIO\_NEAR\_TOL\_ABS\_GAP*
- *MSK\_DPAR\_MIO\_NEAR\_TOL\_REL\_GAP*
- *MSK\_IPAR\_MIO\_CONSTRUCT\_SOL*
- *MSK\_IPAR\_MIO\_MT\_USER\_CB*
- *MSK\_IPAR\_OPF\_MAX\_TERMS\_PER\_LINE*
- *MSK\_IPAR\_READ\_DATA\_COMPRESSED*
- *MSK\_IPAR\_READ\_DATA\_FORMAT*
- *MSK\_IPAR\_WRITE\_DATA\_COMPRESSED*
- *MSK\_IPAR\_WRITE\_DATA\_FORMAT*

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#### Added

- *"MSK\_COMPRESS\_ZSTD"*
- *"MSK\_CT\_DEXP"*
- *"MSK\_CT\_DPOW"*
- *"MSK\_CT\_PEXP"*
- *"MSK\_CT\_PPOW"*
- *"MSK\_CT\_ZERO"*
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- *"MSK\_IINF\_MIO\_NUMCONEVAR"*
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- *"MSK\_IINF\_MIO\_NUMDEXPCONES"*
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- *"MSK\_IINF\_MIO\_NUMINTCONEVAR"*
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- *"MSK\_IINF\_MIO\_PRE SOLVED\_NUMDEXPCONES"*
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- *"MSK\_IINF\_MIO\_PRE SOLVED\_NUMINTCONEVAR"*
- *"MSK\_IINF\_MIO\_PRE SOLVED\_NUMPEXPONES"*
- *"MSK\_IINF\_MIO\_PRE SOLVED\_NUMPPOWCONES"*
- *"MSK\_IINF\_MIO\_PRE SOLVED\_NUMQCONES"*
- *"MSK\_IINF\_MIO\_PRE SOLVED\_NUMRQCONES"*
- *"MSK\_IINF\_PURIFY\_DUAL\_SUCCESS"*
- *"MSK\_IINF\_PURIFY\_PRIMAL\_SUCCESS"*
- *"MSK\_LIINF\_MIO\_ANZ"*

#### Removed

- MSK\_DATAFORMAT\_XML
- MSK\_DINFITEM\_MIO\_HEURISTIC\_TIME
- MSK\_DINFITEM\_MIO\_OPTIMIZER\_TIME
- MSK\_IINFITEM\_MIO\_CONSTRUCT\_NUM\_ROUNDINGS
- MSK\_IINFITEM\_MIO\_INITIAL\_SOLUTION

- MSK\_IINFITEM\_MIO\_NEAR\_ABSGAP\_SATISFIED
- MSK\_IINFITEM\_MIO\_NEAR\_RELGAP\_SATISFIED
- MSK\_LIINFITEM\_MIO\_SIM\_MAXITER\_SETBACKS
- MSK\_MIONODESELTYPE\_HYBRID
- MSK\_MIONODESELTYPE\_WORST
- MSK\_PROBLEMTYPE\_GECO
- MSK\_PROSTA\_NEAR\_DUAL\_FEAS
- MSK\_PROSTA\_NEAR\_PRIM\_AND\_DUAL\_FEAS
- MSK\_PROSTA\_NEAR\_PRIM\_FEAS
- MSK\_SENSITIVITYTYPE\_OPTIMAL\_PARTITION
- MSK\_SOLSTA\_NEAR\_DUAL\_FEAS
- MSK\_SOLSTA\_NEAR\_DUAL\_INFEAS\_CER
- MSK\_SOLSTA\_NEAR\_INTEGER\_OPTIMAL
- MSK\_SOLSTA\_NEAR\_OPTIMAL
- MSK\_SOLSTA\_NEAR\_PRIM\_AND\_DUAL\_FEAS
- MSK\_SOLSTA\_NEAR\_PRIM\_FEAS
- MSK\_SOLSTA\_NEAR\_PRIM\_INFEAS\_CER

## 18.5 Response Codes

### Added

- *"MSK\_RES\_ERR\_APPENDING\_TOO\_BIG\_CONE"*
- *"MSK\_RES\_ERR\_CBF\_DUPLICATE\_POW\_CONES"*
- *"MSK\_RES\_ERR\_CBF\_DUPLICATE\_POW\_STAR\_CONES"*
- *"MSK\_RES\_ERR\_CBF\_INVALID\_DIMENSION\_OF\_CONES"*
- *"MSK\_RES\_ERR\_CBF\_INVALID\_EXP\_DIMENSION"*
- *"MSK\_RES\_ERR\_CBF\_INVALID\_NUMBER\_OF\_CONES"*
- *"MSK\_RES\_ERR\_CBF\_INVALID\_POWER"*
- *"MSK\_RES\_ERR\_CBF\_INVALID\_POWER\_CONE\_INDEX"*
- *"MSK\_RES\_ERR\_CBF\_INVALID\_POWER\_STAR\_CONE\_INDEX"*
- *"MSK\_RES\_ERR\_CBF\_POWER\_CONE\_IS\_TOO\_LONG"*
- *"MSK\_RES\_ERR\_CBF\_POWER\_CONE\_MISMATCH"*
- *"MSK\_RES\_ERR\_CBF\_POWER\_STAR\_CONE\_MISMATCH"*
- *"MSK\_RES\_ERR\_CBF\_UNHANDLED\_POWER\_CONE\_TYPE"*
- *"MSK\_RES\_ERR\_CBF\_UNHANDLED\_POWER\_STAR\_CONE\_TYPE"*
- *"MSK\_RES\_ERR\_CONE\_PARAMETER"*

- *"MSK\_RES\_ERR\_FORMAT\_STRING"*
- *"MSK\_RES\_ERR\_INVALID\_CJ"*
- *"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_CFIX"*
- *"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_FREE\_CONSTRAINTS"*
- *"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_NONLINEAR"*
- *"MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_RANGED\_CONSTRAINTS"*
- *"MSK\_RES\_ERR\_NUM\_ARGUMENTS"*
- *"MSK\_RES\_ERR\_PTF\_FORMAT"*
- *"MSK\_RES\_ERR\_SERVER\_PROBLEM\_SIZE"*
- *"MSK\_RES\_ERR\_SHAPE\_IS\_TOO\_LARGE"*
- *"MSK\_RES\_ERR\_SLICE\_SIZE"*
- *"MSK\_RES\_ERR\_TOO\_SMALL\_A\_TRUNCATION\_VALUE"*
- *"MSK\_RES\_WRN\_EXP\_CONES\_WITH\_VARIABLES\_FIXED\_AT\_ZERO"*
- *"MSK\_RES\_WRN\_POW\_CONES\_WITH\_ROOT\_FIXED\_AT\_ZERO"*

#### Removed

- MSK\_RES\_ERR\_CANNOT\_CLONE\_NL
- MSK\_RES\_ERR\_CANNOT\_HANDLE\_NL
- MSK\_RES\_ERR\_INVALID\_ACCMODE
- MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_GENERAL\_NL
- MSK\_RES\_ERR\_NONLINEAR\_FUNCTIONS\_NOT\_ALLOWED
- MSK\_RES\_ERR\_NR\_ARGUMENTS
- MSK\_RES\_ERR\_OPEN\_DL
- MSK\_RES\_ERR\_USER\_FUNC\_RET
- MSK\_RES\_ERR\_USER\_FUNC\_RET\_DATA
- MSK\_RES\_ERR\_USER\_NLO\_EVAL
- MSK\_RES\_ERR\_USER\_NLO\_EVAL\_HESSUBI
- MSK\_RES\_ERR\_USER\_NLO\_EVAL\_HESSUBJ
- MSK\_RES\_ERR\_USER\_NLO\_FUNC
- MSK\_RES\_TRM\_MIO\_NEAR\_ABS\_GAP
- MSK\_RES\_TRM\_MIO\_NEAR\_REL\_GAP
- MSK\_RES\_WRN\_CONSTRUCT\_INVALID\_SOL\_ITG
- MSK\_RES\_WRN\_CONSTRUCT\_NO\_SOL\_ITG
- MSK\_RES\_WRN\_CONSTRUCT\_SOLUTION\_INFEAS
- MSK\_RES\_WRN\_NO\_NONLINEAR\_FUNCTION\_WRITE

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