



MOSEK Command Line Tools

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MOSEK ApS

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INTRODUCTION

The **MOSEK** Optimization Suite 8.1.0.70 is a powerful software package capable of solving large-scale optimization problems of the following kind:

- linear,
- conic quadratic (also known as second-order cone),
- convex quadratic,
- semidefinite,
- and general convex.

Integer constrained variables are supported for all problem classes except for semidefinite and general convex problems. In order to obtain an overview of features in the **MOSEK** Optimization Suite consult the [product introduction](#) guide.

The most widespread class of optimization problems is *linear optimization problems*, where all relations are linear. The tremendous success of both applications and theory of linear optimization can be ascribed to the following factors:

- The required data are simple, i.e. just matrices and vectors.
- Convexity is guaranteed since the problem is convex by construction.
- Linear functions are trivially differentiable.
- There exist very efficient algorithms and software for solving linear problems.
- Duality properties for linear optimization are nice and simple.

Even if the linear optimization model is only an approximation to the true problem at hand, the advantages of linear optimization may outweigh the disadvantages. In some cases, however, the problem formulation is inherently nonlinear and a linear approximation is either intractable or inadequate. *Conic optimization* has proved to be a very expressive and powerful way to introduce nonlinearities, while preserving all the nice properties of linear optimization listed above.

The fundamental expression in linear optimization is a linear expression of the form

$$Ax - b \in \mathcal{K}$$

where $\mathcal{K} = \{y : y \geq 0\}$, i.e.,

$$\begin{aligned} Ax - b &= y, \\ y &\in \mathcal{K}. \end{aligned}$$

In conic optimization a wider class of convex sets \mathcal{K} is allowed, for example in 3 dimensions \mathcal{K} may correspond to an ice cream cone. The conic optimizer in **MOSEK** supports three structurally different types of cones \mathcal{K} , which allows a surprisingly large number of nonlinear relations to be modelled (as described in the [MOSEK modeling cookbook](#)), while preserving the nice algorithmic and theoretical properties of linear optimization.

1.1 Why the Command Line Tools?

The **MOSEK** capabilities can be accessed from the command line without the need to use any programming language. The user can input optimization problems using files in a variety of *formats*, or via the AMPL language shell.

The Command Line Tools provides access to:

- Linear Optimization (LO)
- Conic Quadratic (Second-Order Cone) Optimization (CQO, SOCO)
- Convex Quadratic and Quadratically Constrained Optimization (QCQO)
- Semidefinite Optimization (SDO)
- General Convex Optimization problems (via AMPL).

as well as to additional utilities for:

- problem analysis,
- sensitivity analysis,
- infeasibility diagnostics.

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You can get in touch with **MOSEK** using popular social media as well:

Blogger	http://blog.mosek.com/
Google Group	https://groups.google.com/forum/#!forum/mosek
Twitter	https://twitter.com/mosektw
Google+	https://plus.google.com/+Mosek/posts
Linkedin	https://www.linkedin.com/company/mosek-aps

In particular **Twitter** is used for news, updates and release announcements.

LICENSE AGREEMENT

Before using the **MOSEK** software, please read the license agreement available in the distribution at <MSKHOME>/mosek/8/mosek-eula.pdf or on the **MOSEK** website <https://mosek.com/products/license-agreement>.

MOSEK uses some third-party open-source libraries. Their license details follows.

zlib

MOSEK includes the *zlib* library obtained from the [zlib website](#). The license agreement for *zlib* is shown in [Listing 3.1](#).

Listing 3.1: *zlib* license.

```
zlib.h -- interface of the 'zlib' general purpose compression library
version 1.2.7, May 2nd, 2012

Copyright (C) 1995-2012 Jean-loup Gailly and Mark Adler

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2. Altered source versions must be plainly marked as such, and must not be
   misrepresented as being the original software.
3. This notice may not be removed or altered from any source distribution.

Jean-loup Gailly          Mark Adler
jloup@gzip.org            madler@alumni.caltech.edu
```

fplib

MOSEK includes the floating point formatting library developed by David M. Gay obtained from the [netlib website](#). The license agreement for *fplib* is shown in [Listing 3.2](#).

Listing 3.2: *fplib* license.

```
/*
*****
*
*/
```

```
* The author of this software is David M. Gay.
*
* Copyright (c) 1991, 2000, 2001 by Lucent Technologies.
*
* Permission to use, copy, modify, and distribute this software for any
* purpose without fee is hereby granted, provided that this entire notice
* is included in all copies of any software which is or includes a copy
* or modification of this software and in all copies of the supporting
* documentation for such software.
*
* THIS SOFTWARE IS BEING PROVIDED "AS IS", WITHOUT ANY EXPRESS OR IMPLIED
* WARRANTY. IN PARTICULAR, NEITHER THE AUTHOR NOR LUCENT MAKES ANY
* REPRESENTATION OR WARRANTY OF ANY KIND CONCERNING THE MERCHANTABILITY
* OF THIS SOFTWARE OR ITS FITNESS FOR ANY PARTICULAR PURPOSE.
*
*****/
```

INSTALLATION

In this section we discuss how to install and setup the **MOSEK** Command Line Tools.

Important: Before running this **MOSEK** interface please make sure that you:

- Installed **MOSEK** correctly. Some operating systems require extra steps. See the [Installation guide](#) for instructions and common troubleshooting tips.
 - Set up a license. See the [Licensing guide](#) for instructions.
-

Locating Files

The files in Command Line Tools are organized as reported in [Table 4.1](#).

Table 4.1: Relevant files for the Command Line Tools.

Relative Path	Description	Label
<MSKHOME>/mosek/8/tools/platform/<PLATFORM>/bin	Binaries	<BINDIR>
<MSKHOME>/mosek/8/tools/platform/<PLATFORM>/bin/mosek	Mosek executable	
<MSKHOME>/mosek/8/tools/examples/data	Examples	<EXDIR>

where

- <MSKHOME> is the folder in which the **MOSEK** package has been installed,
- <PLATFORM> is the actual platform among those supported by **MOSEK**, i.e. win32x86, win64x86, linux64x86 or osx64x86.

Setting up paths

The executable file is ready for use. It may be convenient to add the directory <BINDIR> to the environment variable `PATH`, and then **MOSEK** can simply be used by typing

```
mosek
```

in the command line.

4.1 Testing the installation

To test that Command Line Tools has been installed correctly go to the examples directory <EXDIR> and run **MOSEK** on any of the input files, for example `lo1.mps`:

```
mosek lo1.mps
```

Is should produce output similar to:

```
MOSEK Version 8.0.0.53 (Build date: 2017-1-12 22:21:45)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file 'lo1.mps'
Reading started.

[....]

Optimizer started.
Interior-point optimizer started.

[....]

Interior-point solution summary
  Problem status   : PRIMAL_AND_DUAL_FEASIBLE
  Solution status  : OPTIMAL
  Primal.  obj: 8.3333333280e+01    nrm: 5e+01    Viol.  con: 1e-08    var: 0e+00
  Dual.    obj: 8.3333333242e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Basic solution summary
  Problem status   : PRIMAL_AND_DUAL_FEASIBLE
  Solution status  : OPTIMAL
  Primal.  obj: 8.3333333333e+01    nrm: 5e+01    Viol.  con: 7e-15    var: 0e+00
  Dual.    obj: 8.3333333245e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

[....]

Open file 'lo1.sol'
Start writing.
done writing. Time: 0.00

Open file 'lo1.bas'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]
```

THE COMMAND LINE TOOL

5.1 Introduction

The **MOSEK** command line tool is used to solve optimization problems from the operating system command line. It is invoked as follows

```
mosek [options] [filename]
```

where both [options] and [filename] are optional arguments:

- [options] consists of command line arguments that modify the behavior of **MOSEK**. They are listed in [Sec. 5.5](#). In particular, options can be used to set optimizer parameters.
- [filename] is a file describing the optimization problem. The **MOSEK** command line accepts files in any of the *supported file formats* or in the AMPL `.nl` format.

If no arguments are given, **MOSEK** will display a splash screen and exit.

```
user@host:~$ mosek/8/tools/platform/linux64x86/bin/mosek

MOSEK Version 8.0.0.32(BETA) (Build date: 2016-7-12 10:29:26)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

*** No input file specified. No optimization is performed.

Return code - 0 [MSK_RES_OK]
```

5.2 Files

The **MOSEK** command line tool communicates with the user via files and prints some execution logs and solution summary to the terminal.

Input files

Optimization problems are read from files. See [Sec. 14](#) for details.

File format conversion

To convert between two file formats supported by **MOSEK** use the option `-x` together with `-out` to specify the target file name. The target file type must support the problem type of the source file, otherwise the conversion will be partial. For instance in case a MPS file must be converted in a more readable OPF format, the following line can be used

```
mosek -x -out lo1.opf lo1.mps
```

With the `-x` option the solver will not actually solve the problem.

Output files

Solutions are written to files:

- `.bas` - basic solution,
- `.sol` - interior point solution,
- `.itg` - integer solution (the only available solution for mixed-integer problems).

For linear problems both the basic and interior point solution may be present. Infeasibility certificates are stored in the same files. See [Sec. 14.8](#) for details.

5.3 Example

To solve a problem stored in file, say `lo1.mps`, write:

```
mosek lo1.mps
```

The solver will

- read `lo1.mps` from disk,
- solve the problem and display the solution log and
- store the relevant solution files if any solution exists; file content explained in [Sec. 14.8](#).

```
MOSEK Version 8.0.0.34(BETA) (Build date: 2016-8-24 00:51:13)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86
```

```
Open file '/home/andrea/mosek/8/tools/examples/data/lo1.mps'
Reading started.
Using 'obj' as objective vector
Read 13 number of A nonzeros in 0.00 seconds.
Using 'rhs' as rhs vector
Using 'bound' as bound vector
Reading terminated. Time: 0.00
```

Read summary

```
  Type           : LO (linear optimization problem)
Objective sense  : max
Scalar variables : 4
Matrix variables : 0
Constraints      : 3
Cones           : 0
Time            : 0.0
```

Problem

```
  Name           : lo1
Objective sense  : max
Type            : LO (linear optimization problem)
Constraints      : 3
Cones           : 0
Scalar variables : 4
Matrix variables : 0
Integer variables : 0
```

```

Optimizer started.
Interior-point optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Freed constraints in eliminator : 0
Eliminator terminated.
Eliminator - tries          : 1          time          : 0.00
Lin. dep. - tries          : 1          time          : 0.00
Lin. dep. - number         : 0
Presolve terminated. Time: 0.00
Optimizer - threads        : 2
Optimizer - solved problem : the primal
Optimizer - Constraints     : 3
Optimizer - Cones          : 0
Optimizer - Scalar variables : 6          conic          : 0
Optimizer - Semi-definite variables: 0      scalarized       : 0
Factor - setup time        : 0.00        dense det. time  : 0.00
Factor - ML order time     : 0.00        GP order time   : 0.00
Factor - nonzeros before factor : 6      after factor    : 6
Factor - dense dim.       : 0          flops           : 1.06e+02
ITE PFEAS  DFEAS  GFEAS  PRSTATUS  POBJ          DOBJ          MU      TIME
0  8.0e+00  3.2e+00  3.5e+00  1.00e+00  1.0000000000e+01  0.0000000000e+00  1.0e+00  0.01
1  4.2e+00  2.5e+00  4.7e-01  0.00e+00  3.093970927e+01  2.766058702e+01  2.6e+00  0.01
2  4.2e-01  2.5e-01  4.6e-02  -1.82e-02  6.511676243e+01  6.308843559e+01  2.6e-01  0.01
3  3.6e-02  2.1e-02  3.9e-03  5.84e-01  8.096141239e+01  8.061962333e+01  2.2e-02  0.01
4  1.5e-05  9.1e-06  1.7e-06  9.43e-01  8.333280389e+01  8.333241803e+01  9.2e-06  0.01
5  1.5e-09  9.1e-10  1.7e-10  1.00e+00  8.333333328e+01  8.333333324e+01  9.2e-10  0.01
Basis identification started.
Primal basis identification phase started.
ITER      TIME
0          0.00
Primal basis identification phase terminated. Time: 0.00
Dual basis identification phase started.
ITER      TIME
0          0.00
Dual basis identification phase terminated. Time: 0.00
Basis identification terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.01.

Optimizer terminated. Time: 0.02

Interior-point solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: 8.3333333280e+01    nrm: 5e+01    Viol.  con: 1e-08    var: 0e+00
Dual.    obj: 8.3333333242e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Basic solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: 8.3333333333e+01    nrm: 5e+01    Viol.  con: 7e-15    var: 0e+00
Dual.    obj: 8.3333333245e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Optimizer summary
Optimizer - time: 0.02
Interior-point - iterations : 5    time: 0.01
Basis identification - time: 0.00
Primal - iterations : 0    time: 0.00
Dual - iterations : 0    time: 0.00
Clean primal - iterations : 0    time: 0.00

```

```
Clean dual      - iterations : 0      time: 0.00
Simplex         -                  time: 0.00
Primal simplex  - iterations : 0      time: 0.00
Dual simplex    - iterations : 0      time: 0.00
Mixed integer   - relaxations: 0      time: 0.00

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.sol'
Start writing.
done writing. Time: 0.00

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.bas'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]
```

5.4 Solver Parameters

MOSEK comes with a large number of parameters that allows the user to tune the behavior of the optimizer. The typical settings which can be changed with solver parameters include:

- choice of the optimizer for linear problems,
- choice of primal/dual solver,
- turning presolve on/off,
- turning heuristics in the mixed-integer optimizer on/off,
- level of multi-threading,
- feasibility tolerances,
- solver termination criteria,
- behaviour of the license manager,

and more. All parameters have default settings which will be suitable for most typical users. Each parameter is identified by a unique string name and it can accept either integers or symbolic names, floating point values or symbolic strings. Please refer to [Sec. 13.2](#) for the complete list of available solver parameters.

5.4.1 Setting from command line

Setting solver parameters is possible using the command line option `-d`. If multiple parameters must be specified, option `-d` must be repeated for each one. For example, the next command will switch off presolve, set a feasibility tolerance and solve the problem from `lo1.opf`:

```
mosek -d MSK_IPAR_PREOLVE_USE MSK_OFF -d MSK_DPAR_INTPNT_TOL_PFEAS 1.0e-8 lo1.opf
```

5.4.2 Using the Parameter File

Solver parameters can also be set using a parameter file, for example:

```
BEGIN MOSEK
% This is a comment.
% The subsequent line tells MOSEK that an optimal
% basis should be computed by the interior-point optimizer.
MSK_IPAR_PREOLVE_USE      MSK_OFF
```



```
MSK_DPAR_INTPNT_TOL_PFEAS    1.0e-9
END MOSEK
```

The syntax of the parameter file must obey a few simple rules:

- The file must begin with **BEGIN MOSEK** and end with **END MOSEK**.
- Empty lines and lines starting from a % sign are ignored.
- Each line contains a valid **MOSEK** parameter name followed by its value.

The parameter file can have any name. Assuming it has been called `mosek.par`, it can be used using the `-p` option as follows:

```
mosek -p mosek.par afiro.mps
```

Command-line parameters override those from the parameter file in case of repetition. For instance

```
mosek -p mosek.par -d MSK_DPAR_INTPNT_TOL_PFEAS 1.0e-8 afiro.mps
```

will set `MSK_DPAR_INTPNT_TOL_PFEAS` to 10^{-8} using the value provided on the command line.

5.5 Command Line Arguments

The following list shows the available command-line arguments for **MOSEK**:

- `-anapro`
Analyze the problem data.
- `-anasoli <name>`
Analyze the initial solution name e.g. `-anasoli bas`.
- `-anasolo <name>`
Analyze the final solution name e.g. `-anasolo itg`.
- `-a`
MOSEK is started in AMPL mode.
- `-basi <name>`
Input basic solution file name.
- `-baso <name>`
Output basic solution file name.
- `-d <name> <value>`
Define the value `value` for the **MOSEK** parameter `name`.
- `-dbgmem <name>`
Name of memory debug file.
- `-f`
Complete license information is printed.
- `-h, -?`
Help.
- `-inti <name>`
Input integer solution file name.
- `-into <name>`
Output integer solution file name.
- `-itri <name>`
Input interior point solution file name.

-itro <name>
Output interior point solution file name.

-info <name>
Infeasible subproblem output file name.

-infrepo <name>
Feasibility reparation output file.

-l, -L <dir>
dir is the directory where the **MOSEK** license file **mosek.lic** is located.

-max
The problem is maximized.

-min
The problem is minimized.

-n
Ignore errors in subsequent parameter settings.

-out <name>
Write the task to a data file named **name**. See [Sec. 14](#).

-p <name>, **-pari** <name>
Name of the input parameter file.

-paro <name>
Name of the output parameter file.

-r
If the option is present, the program returns -1 if an error occurred, otherwise 0 .

-removeitg
Removes all integer constraints after reading the problem.

-rout <name>
If the option is present, the program writes the return code to file **name**.

-q <name>
Name of an optional log file.

-sen <file>
Perform sensitivity analysis based on file.

-silent
As little information as possible is send to the terminal.

-toconic
Translate to conic form after reading.

-v
MOSEK version is printed and no optimization is performed.

-w
If this options is on, then **MOSEK** will wait for a license.

-x
Do not run the optimizer. Useful for converting between file formats.

-=
List all possible solver parameters with default value, lower bound and upper bound (if applicable).

THE MOSEK-BUNDLED AMPL SHELL

AMPL is a modeling language for specifying linear and nonlinear optimization models in a natural way. AMPL also makes it easy to solve the problem and e.g. display the solution or part of it. We will not discuss the specifics of the AMPL language here but instead refer the reader to [FGK03], <http://ampl.com/BOOK/download.html> and the AMPL website <http://www.ampl.com>.

AMPL cannot solve optimization problems by itself but requires a link to an optimizer. The **MOSEK** distribution includes:

- An AMPL link which makes it possible to use **MOSEK** as an optimizer within AMPL. The link can be used from any AMPL shell.
- The full, official AMPL shell repackaged under the name **mampl**. This is sold as a separate product, and it can be hooked to other optimizers as well.

Note:

- To use **MOSEK** from AMPL you need to set up the system path to the **MOSEK** command line tool.
 - It is possible to specify problems in AMPL that cannot be solved by **MOSEK**. The optimization problem must be a smooth convex optimization problem as discussed in Sec. 7.
-

For the remainder of this section we refer to the **MOSEK**-bundled **mampl** as the AMPL interpreter of choice. However, the tutorial applies also to any other standard AMPL shell available to the user.

6.1 Locating the AMPL shell

Assuming **MSKHOME** is the folder in which **MOSEK** has been installed, the AMPL shell is the executable file

`{MSKHOME}/mosek/8/tools/platform/{PLATFORM}/bin/mampl`

for Linux and OSX users (**PLATFORM** must be among `linux64x86`, `osx64x86`), and under

`{MSKHOME}\mosek\8\tools\platform\{PLATFORM}\bin\mampl`

for Windows users (**PLATFORM** must be among `win32x86`, `win64x86`).

6.2 An example

In many instances, you can successfully apply **MOSEK** simply by specifying the model and data, setting the solver option to **MOSEK**, and typing **solve**.

Consider a simple linear optimization problem formulated as an AMPL model in Listing 6.1.

Listing 6.1: An example of an optimization problem in AMPL language.

```

set NUTR ordered;
set FOOD ordered;

param cost {FOOD} >= 0;
param f_min {FOOD} >= 0, default 0;
param f_max {j in FOOD} >= f_min[j], default Infinity;

param n_min {NUTR} >= 0, default 0;
param n_max {i in NUTR} >= n_min[i], default Infinity;

param amt {NUTR,FOOD} >= 0;

# -----

var Buy {j in FOOD} >= f_min[j], <= f_max[j];

# -----

minimize Total_Cost: sum {j in FOOD} cost[j] * Buy[j];

minimize Nutr_Amt {i in NUTR}: sum {j in FOOD} amt[i,j] * Buy[j];

# -----

subject to Diet {i in NUTR}:
    n_min[i] <= sum {j in FOOD} amt[i,j] * Buy[j] <= n_max[i];

```

We can specify the input data using an input file again following the AMPL syntax, as in [Listing 6.2](#).

Listing 6.2: An example of data for an optimization problem using AMPL language.

```

param:  FOOD:      cost  f_min  f_max :=
    "Quarter Pounder w/ Cheese"  1.84  .    .
    "McLean Deluxe w/ Cheese"    2.19  .    .
    "Big Mac"                     1.84  .    .
    "Filet-O-Fish"                1.44  .    .
    "McGrilled Chicken"           2.29  .    .
    "Fries, small"                .77   .    .
    "Sausage McMuffin"            1.29  .    .
    "1% Lowfat Milk"              .60   .    .
    "Orange Juice"               .72   .    . ;

param:  NUTR:      n_min  n_max :=
    Cal      2000  .
    Carbo    350   375
    Protein   55   .
    VitA     100   .
    VitC     100   .
    Calc     100   .
    Iron     100   . ;

param amt (tr):

```

	Cal	Carbo	Protein	VitA	VitC	Calc	Iron
"Quarter Pounder w/ Cheese"	510	34	28	15	6	30	20
"McLean Deluxe w/ Cheese"	370	35	24	15	10	20	20
"Big Mac"	500	42	25	6	2	25	20
"Filet-O-Fish"	370	38	14	2	0	15	10
"McGrilled Chicken"	400	42	31	8	15	15	8
"Fries, small"	220	26	3	0	15	0	2
"Sausage McMuffin"	345	27	15	4	0	20	15
"1% Lowfat Milk"	110	12	9	10	4	30	0

"Orange Juice"	80	20	1	2	120	2	2 ;
----------------	----	----	---	---	-----	---	-----

Invoke the AMPL shell:

```
mampl
```

and type in the commands:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: solve;
```

The resulting output is:

```
MOSEK finished.
Problem status   - PRIMAL_AND_DUAL_FEASIBLE
Solution status  - OPTIMAL
Primal objective - 14.8557377
Dual objective   - 14.8557377

Objective = Total_Cost
```

6.3 Retrieving solutions

6.3.1 Status codes

The AMPL parameter `solve_result_num` is used to indicate the outcome of the optimization process. It is used as follows

```
ampl: display solve_result_num
```

Please refer to table [Table 6.1](#) for possible values of this parameter.

Table 6.1: Interpretation of `solve_result_num`.

Value	Message
0	the solution is optimal.
100	suboptimal primal solution.
101	superoptimal (dual feasible) solution.
150	the solution is near optimal.
200	primal infeasible problem.
300	dual infeasible problem.
400	too many iterations.
500	solution status is unknown.
501	ill-posed problem, solution status is unknown.
> 501	Mapped MOSEK response code. See note below.

MOSEK response codes are mapped to AMPL return codes greater than 501. In order to get the actual response code the base value 501 must be subtracted. For example: the AMPL return code 502 corresponds to **MOSEK** response code 1.

6.3.2 Which solution is returned

MOSEK can produce three types of solutions: basic, interior point and integer. The solution returned to AMPL is determined according to the following rules:

- For problems containing integer variables only the integer solution is available and it is returned.
- For nonlinear problems only the interior point solution is available and it is returned.
- For linear problems, if both basic and interior point solution are available, then the basic solution is returned. Otherwise the only available solution is returned.

6.4 Optimizer options

6.4.1 The MOSEK parameter database

The **MOSEK** optimizer can be controller using solver parameters, as described in [Sec. 5.4](#). These parameters can be modified within AMPL as shown in the example below:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex \
ampl? msk_ipar_sim_max_iterations = 100000';
ampl: solve;
```

In the example above a string called `mosek_options` is created which contains the parameter settings. Each parameter setting has the format

```
parameter_name = value
```

where `parameter_name` is a valid **MOSEK** parameter name. See [Sec. 13.2](#) for a description of all valid **MOSEK** parameters.

An alternative way of specifying the parameters is

```
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex'
ampl? 'msk_ipar_sim_max_iterations = 100000';
```

New parameters can also be appended to an existing option string as shown below.

```
ampl: option mosek_options $mosek_options
ampl? ' msk_ipar_sim_print_freq = 0 msk_ipar_sim_max_iterations = 1000';
```

The expression `$mosek_options` expands to the current value of the option. Line two in the example appends an additional value `msk_ipar_sim_max_iterations` to the option string.

6.4.2 Options

MOSEK recognizes the following AMPL options.

outlev

Controls the amount of printed output. 0 means no printed output and a higher value means progressively more output. An example of setting `outlev` is as follows:

```
ampl: option mosek_options 'outlev=2';
```

wantsol

Controls the solution information generated when run in standalone mode (called without the argument `-AMPL`). It should be constructed as the sum of

1	to write a <code>.sol</code> file
2	to print the primal variable values
4	to print the dual variable values
8	to suppress printing the solution message

We refer the reader to the AMPL manual [\[FGK03\]](#) for more details.

6.4.3 Passing variable names to MOSEK

AMPL assigns meaningful names to all the constraints and variables. Since **MOSEK** uses item names in error and log messages, it may be useful to pass the AMPL names to **MOSEK**. This can be achieved with the command:

```
ampl: option auxfiles rc;
ampl: solve;
```

6.5 Hot-start

Frequently, a sequence of optimization problems is solved where each problem differs only slightly from the previous problem. In that case it may be advantageous to use the previous optimal solution to warm-start the optimizer. Such a facility is available in **MOSEK** only when the simplex optimizer is used.

The warm-start facility exploits the AMPL variable suffix `sstatus` to communicate the optimal basis back to AMPL, and AMPL uses this facility to communicate an initial basis to **MOSEK**. The following example demonstrates this feature.

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex outlev=2';
ampl: solve;
ampl: display Buy.sstatus;
ampl: solve;
```

The resulting output is:

```
Accepted: msk_ipar_optimizer          = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev                      = 2

Computer  - Platform                  : Linux/64-X86
Computer  - CPU type                  : Intel-P4
MOSEK     - task name                  :
MOSEK     - objective sense            : min
MOSEK     - problem type               : L0 (linear optimization problem)
MOSEK     - constraints                : 7                variables          : 9
MOSEK     - integer variables          : 0

Optimizer started.
Simplex optimizer started.
Presolve started.
Linear dependency checker started.
```

```

Linear dependency checker terminated.
Presolve - Stk. size (kb) : 0
Eliminator - tries : 0 time : 0.00
Eliminator - elim's : 0
Lin. dep. - tries : 1 time : 0.00
Lin. dep. - number : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.
Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer - solved problem : the primal
Optimizer - constraints : 7 variables : 9
Optimizer - hotstart : no
ITER DEGITER(%) PFEAS DFEAS POBJ DOBJ TIME
↪ TOTTIME
0 0.00 1.40e+03 NA 1.2586666667e+01 NA 0.00
↪ 0.01
3 0.00 0.00e+00 NA 1.4855737705e+01 NA 0.00
↪ 0.01
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0 [MSK_RES_OK]
MOSEK finished.
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal objective : 14.8557377
Dual objective : 14.8557377

Objective = Total_Cost
Buy.sstatus [*] :=
'Quarter Pounder w/ Cheese' bas
'McLean Deluxe w/ Cheese' low
'Big Mac' low
Filet-O-Fish low
'McGrilled Chicken' low
'Fries, small' bas
'Sausage McMuffin' low
'1% Lowfat Milk' bas
'Orange Juice' low
;
Accepted: msk_ipar_optimizer = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev = 2
Basic solution
Problem status : UNKNOWN
Solution status : UNKNOWN
Primal - objective: 1.4855737705e+01 eq. infeas.: 3.97e+03 max bound infeas.: 2.00e+03
Dual - objective: 0.0000000000e+00 eq. infeas.: 7.14e-01 max bound infeas.: 0.00e+00

Computer - Platform : Linux/64-X86
Computer - CPU type : Intel-P4
MOSEK - task name :
MOSEK - objective sense : min
MOSEK - problem type : LO (linear optimization problem)
MOSEK - constraints : 7 variables : 9
MOSEK - integer variables : 0
Optimizer started.
Simplex optimizer started.
Presolve started.
Presolve - Stk. size (kb) : 0
Eliminator - tries : 0 time : 0.00
Eliminator - elim's : 0
Lin. dep. - tries : 0 time : 0.00

```



```

Lin. dep. - number          : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.
Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer - solved problem   : the primal
Optimizer - constraints      : 7          variables          : 9
Optimizer - hotstart        : yes
Optimizer - Num. basic      : 7          Basis rank          : 7
Optimizer - Valid bas. fac. : no
ITER    DEGITER(%)  PFEAS    DFEAS    POBJ          DOBJ          TIME
↪      TOTTIME
0       0.00        0.00e+00  NA        1.4855737705e+01  NA            0.00
↪      0.01
0       0.00        0.00e+00  NA        1.4855737705e+01  NA            0.00
↪      0.01
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0 [MSK_RES_OK]
MOSEK finished.
Problem status   : PRIMAL_AND_DUAL_FEASIBLE
Solution status  : OPTIMAL
Primal objective : 14.8557377
Dual objective   : 14.8557377

Objective = Total_Cost

```

Please note that the second solve takes fewer iterations since the previous optimal basis is reused.

6.6 Infeasibility report

For linear optimization problems without any integer constrained variables **MOSEK** can generate an infeasibility report automatically. The report provides important information about the infeasibility.

The generation of the infeasibility report is turned on using the parameter setting

```

option auxfiles rc;
option mosek_options 'msk_ipar_infeas_report_auto=msk_on';

```

For further details about infeasibility report see [Sec. 11](#).

6.7 Sensitivity analysis

MOSEK can calculate sensitivity information for the objective and constraints. To enable sensitivity information set the option:

```
sensitivity = 1
```

Results are returned in variable/constraint suffixes as follows:

- **.down** Smallest value of objective coefficient/right hand side before the optimal basis changes.
- **.up** Largest value of objective coefficient/right hand side before the optimal basis changes.
- **.current** Current value of objective coefficient/right hand side.

For ranged constraints sensitivity information is returned only for the lower bound.

The example below returns sensitivity information on the `diet` model.

```

ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options 'sensitivity=1';

ampl: solve;
#display sensitivity information and current solution.
ampl: display _var.down,_var.current,_var.up,_var;
#display sensitivity information and optimal dual values.
ampl: display _con.down,_con.current,_con.up,_con;

```

The resulting output is:

```

Return code - 0 [MSK_RES_OK]
MOSEK finished.
Problem status      : PRIMAL_AND_DUAL_FEASIBLE
Solution status     : OPTIMAL
Primal objective    : 14.8557377
Dual objective      : 14.8557377

suffix up OUT;
suffix down OUT;
suffix current OUT;
Objective = Total_Cost
:  _var.down _var.current      _var.up      _var      :=
1  1.37385   1.84             1.86075    4.38525
2  1.8677    2.19             Infinity    0
3  1.82085   1.84             Infinity    0
4  1.35466   1.44             Infinity    0
5  1.57633   2.29             Infinity    0
6  0.094     0.77             0.794851    6.14754
7  1.22759   1.29             Infinity    0
8  0.57559   0.6              0.910769    3.42213
9  0.657279  0.72             Infinity    0
;
ampl: display _con.down,_con.current,_con.up,_con;
:  _con.down _con.current      _con.up      _con      :=
1  -Infinity 2000             3965.37    0
2  297.6     350             375          0.0277049
3  -Infinity 55              172.029    0
4  63.0531   100             195.388    0.0267541
5  -Infinity 100             132.213    0
6  -Infinity 100             234.221    0
7  17.6923   100             142.821    0.0248361
;

```

6.8 Using the command line version of the AMPL interface

AMPL can generate a data file containing the optimization problem and all relevant information which can then be read and solved by the **MOSEK** command line tool.

When the problem has been loaded into AMPL, the commands

```

ampl: option auxfiles rc;
ampl: write bprob;

```

will make AMPL write the appropriate data files, i.e.

```
prob.nl  
prob.col  
prob.row
```

Then the problem can be solved using the command line version of **MOSEK** as follows

```
mosek prob.nl outlev=10 -a
```

The option *-a* indicates that **MOSEK** is invoked in AMPL mode. When **MOSEK** is invoked in AMPL mode the standard **MOSEK** command line options should appear *after* the *-a* option except for the file name which should be the first argument. As the above example demonstrates **MOSEK** accepts command line options following the AMPL convention. To see which command line arguments **MOSEK** accepts in AMPL mode write:

```
mosek -- -a
```

For linear, quadratic and quadratically constrained problems a text file representation of the problem can be obtained by performing one of the following conversions:

```
mosek prob.nl -a -x -out prob.mps  
mosek prob.nl -a -x -out prob.opf  
mosek prob.nl -a -x -out prob.lp
```


PROBLEM FORMULATION AND SOLUTIONS

In this chapter we will discuss the following issues:

- The formal, mathematical formulations of the problem types that **MOSEK** can solve and their duals.
- The solution information produced by **MOSEK**.
- The infeasibility certificate produced by **MOSEK** if the problem is infeasible.

7.1 Linear Optimization

A linear optimization problem can be written as

$$\begin{array}{ll} \text{minimize} & c^T x + c^f \\ \text{subject to} & l^c \leq Ax \leq u^c, \\ & l^x \leq x \leq u^x, \end{array} \quad (7.1)$$

where

- m is the number of constraints.
- n is the number of decision variables.
- $x \in \mathbb{R}^n$ is a vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear part of the objective function.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.

A primal solution (x) is *(primal) feasible* if it satisfies all constraints in (7.1). If (7.1) has at least one primal feasible solution, then (7.1) is said to be (primal) feasible.

In case (7.1) does not have a feasible solution, the problem is said to be *(primal) infeasible*.

7.1.1 Duality for Linear Optimization

Corresponding to the primal problem (7.1), there is a dual problem

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ & A^T y + s_l^x - s_u^x = c, \\ \text{subject to} & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{array} \quad (7.2)$$

If a bound in the primal problem is plus or minus infinity, the corresponding dual variable is fixed at 0, and we use the convention that the product of the bound value and the corresponding dual variable is 0. E.g.

$$l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0 \text{ and } l_j^x \cdot (s_l^x)_j = 0.$$

This is equivalent to removing variable $(s_l^x)_j$ from the dual problem. A solution

$$(y, s_l^c, s_u^c, s_l^x, s_u^x)$$

to the dual problem is feasible if it satisfies all the constraints in (7.2). If (7.2) has at least one feasible solution, then (7.2) is *(dual) feasible*, otherwise the problem is *(dual) infeasible*.

A Primal-dual Feasible Solution

A solution

$$(x, y, s_l^c, s_u^c, s_l^x, s_u^x)$$

is denoted a *primal-dual feasible solution*, if (x) is a solution to the primal problem (7.1) and $(y, s_l^c, s_u^c, s_l^x, s_u^x)$ is a solution to the corresponding dual problem (7.2).

The Duality Gap

Let

$$(x^*, y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

be a primal-dual feasible solution, and let

$$(x^c)^* := Ax^*.$$

For a primal-dual feasible solution we define the *duality gap* as the difference between the primal and the dual objective value,

$$\begin{aligned} c^T x^* + c^f - \{ & (l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* + c^f \} \\ &= \sum_{i=0}^{m-1} [(s_l^c)^* ((x_i^c)^* - l_i^c) + (s_u^c)^* (u_i^c - (x_i^c)^*)] \\ &+ \sum_{j=0}^{n-1} [(s_l^x)^* (x_j - l_j^x) + (s_u^x)^* (u_j^x - x_j^*)] \geq 0 \end{aligned} \quad (7.3)$$

where the first relation can be obtained by transposing and multiplying the dual constraints (7.2) by x^* and $(x^c)^*$ respectively, and the second relation comes from the fact that each term in each sum is nonnegative. It follows that the primal objective will always be greater than or equal to the dual objective.

An Optimal Solution

It is well-known that a linear optimization problem has an optimal solution if and only if there exist feasible primal and dual solutions so that the duality gap is zero, or, equivalently, that the *complementarity conditions*

$$\begin{aligned} (s_l^c)^* ((x_i^c)^* - l_i^c) &= 0, & i = 0, \dots, m-1, \\ (s_u^c)^* (u_i^c - (x_i^c)^*) &= 0, & i = 0, \dots, m-1, \\ (s_l^x)^* (x_j - l_j^x) &= 0, & j = 0, \dots, n-1, \\ (s_u^x)^* (u_j^x - x_j^*) &= 0, & j = 0, \dots, n-1, \end{aligned}$$

are satisfied.

If (7.1) has an optimal solution and **MOSEK** solves the problem successfully, both the primal and dual solution are reported, including a status indicating the exact state of the solution.

7.1.2 Infeasibility for Linear Optimization

Primal Infeasible Problems

If the problem (7.1) is infeasible (has no feasible solution), **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the modified dual problem

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ & \text{subject to} && A^T y + s_l^x - s_u^x = 0, \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \end{aligned} \tag{7.4}$$

such that the objective value is strictly positive, i.e. a solution

$$(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

to (7.4) so that

$$(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* > 0.$$

Such a solution implies that (7.4) is unbounded, and that its dual is infeasible. As the constraints to the dual of (7.4) are identical to the constraints of problem (7.1), we thus have that problem (7.1) is also infeasible.

Dual Infeasible Problems

If the problem (7.2) is infeasible (has no feasible solution), **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the modified primal problem

$$\begin{aligned} & \text{minimize} && c^T x \\ & \text{subject to} && \hat{l}^c \leq Ax \leq \hat{u}^c, \\ & && \hat{l}^x \leq x \leq \hat{u}^x, \end{aligned} \tag{7.5}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that

$$c^T x < 0.$$

Such a solution implies that (7.5) is unbounded, and that its dual is infeasible. As the constraints to the dual of (7.5) are identical to the constraints of problem (7.2), we thus have that problem (7.2) is also infeasible.

Primal and Dual Infeasible Case

In case that both the primal problem (7.1) and the dual problem (7.2) are infeasible, **MOSEK** will report only one of the two possible certificates — which one is not defined (**MOSEK** returns the first certificate found).

Minimalization vs. Maximalization

When the objective sense of problem (7.1) is maximization, i.e.

$$\begin{array}{ll} \text{maximize} & c^T x + c^f \\ \text{subject to} & l^c \leq Ax \leq u^c, \\ & l^x \leq x \leq u^x, \end{array}$$

the objective sense of the dual problem changes to minimization, and the domain of all dual variables changes sign in comparison to (7.2). The dual problem thus takes the form

$$\begin{array}{ll} \text{minimize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & A^T y + s_l^x - s_u^x = c, \\ & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \leq 0. \end{array}$$

This means that the duality gap, defined in (7.3) as the primal minus the dual objective value, becomes nonpositive. It follows that the dual objective will always be greater than or equal to the primal objective. The primal infeasibility certificate will be reported by **MOSEK** as a solution to the system

$$\begin{array}{l} A^T y + s_l^x - s_u^x = 0, \\ -y + s_l^c - s_u^c = 0, \\ s_l^c, s_u^c, s_l^x, s_u^x \leq 0, \end{array} \quad (7.6)$$

such that the objective value is strictly negative

$$(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* < 0.$$

Similarly, the certificate of dual infeasibility is an x satisfying the requirements of (7.5) such that $c^T x > 0$.

7.2 Conic Quadratic Optimization

Conic quadratic optimization is an extension of linear optimization (see Sec. 7.1) allowing conic domains to be specified for subsets of the problem variables. A conic quadratic optimization problem can be written as

$$\begin{array}{ll} \text{minimize} & c^T x + c^f \\ \text{subject to} & l^c \leq Ax \leq u^c, \\ & l^x \leq x \leq u^x, \\ & x \in \mathcal{K}, \end{array} \quad (7.7)$$

where set \mathcal{K} is a Cartesian product of convex cones, namely $\mathcal{K} = \mathcal{K}_1 \times \cdots \times \mathcal{K}_p$. Having the domain restriction, $x \in \mathcal{K}$, is thus equivalent to

$$x^t \in \mathcal{K}_t \subseteq \mathbb{R}^{n_t},$$

where $x = (x^1, \dots, x^p)$ is a partition of the problem variables. Please note that the n -dimensional Euclidean space \mathbb{R}^n is a cone itself, so simple linear variables are still allowed.

MOSEK supports only a limited number of cones, specifically:

- The \mathbb{R}^n set.
- The quadratic cone:

$$\mathcal{Q}^n = \left\{ x \in \mathbb{R}^n : x_1 \geq \sqrt{\sum_{j=2}^n x_j^2} \right\}.$$

- The rotated quadratic cone:

$$\mathcal{Q}_r^n = \left\{ x \in \mathbb{R}^n : 2x_1x_2 \geq \sum_{j=3}^n x_j^2, \quad x_1 \geq 0, \quad x_2 \geq 0 \right\}.$$

Although these cones may seem to provide only limited expressive power they can be used to model a wide range of problems as demonstrated in [\[MOSEKApS12\]](#).

7.2.1 Duality for Conic Quadratic Optimization

The dual problem corresponding to the conic quadratic optimization problem (7.7) is given by

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ & \text{subject to} && \\ & && A^T y + s_l^x - s_u^x + s_n^x = c \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & && s_n^x \in \mathcal{K}^*, \end{aligned} \tag{7.8}$$

where the dual cone \mathcal{K}^* is a Cartesian product of the cones

$$\mathcal{K}^* = \mathcal{K}_1^* \times \cdots \times \mathcal{K}_p^*,$$

where each \mathcal{K}_t^* is the dual cone of \mathcal{K}_t . For the cone types **MOSEK** can handle, the relation between the primal and dual cone is given as follows:

- The \mathbb{R}^n set:

$$\mathcal{K}_t = \mathbb{R}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \{s \in \mathbb{R}^{n_t} : s = 0\}.$$

- The quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : s_1 \geq \sqrt{\sum_{j=2}^{n_t} s_j^2} \right\}.$$

- The rotated quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}_r^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}_r^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : 2s_1s_2 \geq \sum_{j=3}^{n_t} s_j^2, \quad s_1 \geq 0, \quad s_2 \geq 0 \right\}.$$

Please note that the dual problem of the dual problem is identical to the original primal problem.

7.2.2 Infeasibility for Conic Quadratic Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see [Sec. 7.1.2](#)).

Primal Infeasible Problems

If the problem (7.7) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ & \text{subject to} && \\ & && A^T y + s_l^x - s_u^x + s_n^x = 0, \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & && s_n^x \in \mathcal{K}^*, \end{aligned}$$

such that the objective value is strictly positive.

Dual infeasible problems

If the problem (7.8) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{minimize} && c^T x \\ & \text{subject to} && \hat{l}^c \leq Ax \leq \hat{u}^c, \\ & && \hat{l}^x \leq x \leq \hat{u}^x, \\ & && x \in \mathcal{K}, \end{aligned}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that the objective value is strictly negative.

7.3 Semidefinite Optimization

Semidefinite optimization is an extension of conic quadratic optimization (see Sec. 7.2) allowing positive semidefinite matrix variables to be used in addition to the usual scalar variables. A semidefinite optimization problem can be written as

$$\begin{aligned} & \text{minimize} && \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \langle \bar{C}_j, \bar{X}_j \rangle + c^f \\ & \text{subject to} && \begin{aligned} l_i^c &\leq && \sum_{j=0}^{n-1} a_{ij} x_j + \sum_{j=0}^{p-1} \langle \bar{A}_{ij}, \bar{X}_j \rangle &\leq & u_i^c, & i = 0, \dots, m-1 \\ l_j^x &\leq && x_j &\leq & u_j^x, & j = 0, \dots, n-1 \\ &&& x \in \mathcal{K}, \bar{X}_j \in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1 \end{aligned} \end{aligned} \quad (7.9)$$

where the problem has p symmetric positive semidefinite variables $\bar{X}_j \in \mathcal{S}_+^{r_j}$ of dimension r_j with symmetric coefficient matrices $\bar{C}_j \in \mathcal{S}^{r_j}$ and $\bar{A}_{ij} \in \mathcal{S}^{r_j}$. We use standard notation for the matrix inner product, i.e., for $U, V \in \mathbb{R}^{m \times n}$ we have

$$\langle U, V \rangle := \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} U_{ij} V_{ij}.$$

With semidefinite optimization we can model a wide range of problems as demonstrated in [MOSEKApS12].

7.3.1 Duality for Semidefinite Optimization

The dual problem corresponding to the semidefinite optimization problem (7.9) is given by

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ & \text{subject to} && \begin{aligned} c - A^T y + s_u^x - s_l^x &= s_n^x, \\ \bar{C}_j - \sum_{i=0}^m y_i \bar{A}_{ij} &= \bar{S}_j, && j = 0, \dots, p-1 \\ s_l^c - s_u^c &= y, \\ s_l^c, s_u^c, s_l^x, s_u^x &\geq 0, \\ s_n^x \in \mathcal{K}^*, \quad \bar{S}_j &\in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1 \end{aligned} \end{aligned} \quad (7.10)$$

where $A \in \mathbb{R}^{m \times n}$, $A_{ij} = a_{ij}$, which is similar to the dual problem for conic quadratic optimization (see Sec. 7.2.1), except for the addition of dual constraints

$$\left(\bar{C}_j - \sum_{i=0}^m y_i \bar{A}_{ij} \right) \in \mathcal{S}_+^{r_j}.$$

Note that the dual of the dual problem is identical to the original primal problem.

7.3.2 Infeasibility for Semidefinite Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of the infeasibility. This works exactly as for linear problems (see Sec. 7.1.2).

Primal Infeasible Problems

If the problem (7.9) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is a certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ & \text{subject to} && A^T y + s_l^x - s_u^x + s_n^x = 0, \\ & && \sum_{i=0}^{m-1} y_i \bar{A}_{ij} + \bar{S}_j = 0, && j = 0, \dots, p-1 \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & && s_n^x \in \mathcal{K}^*, \quad \bar{S}_j \in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1 \end{aligned}$$

such that the objective value is strictly positive.

Dual Infeasible Problems

If the problem (7.10) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{minimize} && \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \langle \bar{C}_j, \bar{X}_j \rangle \\ & \text{subject to} && \hat{l}_i^c \leq \sum_{j=1}^n a_{ij} x_j + \sum_{j=0}^{p-1} \langle \bar{A}_{ij}, \bar{X}_j \rangle \leq \hat{u}_i^c, \quad i = 0, \dots, m-1 \\ & && \hat{l}^x \leq \begin{matrix} x \\ \bar{X}_j \end{matrix} \leq \hat{u}^x, \\ & && x \in \mathcal{K}, \quad \bar{X}_j \in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1 \end{aligned}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that the objective value is strictly negative.

7.4 Quadratic and Quadratically Constrained Optimization

A convex quadratic and quadratically constrained optimization problem has the form

$$\begin{aligned} & \text{minimize} && \frac{1}{2}x^T Q^o x + c^T x + c^f \\ & \text{subject to} && \begin{aligned} l_k^c &\leq \frac{1}{2}x^T Q^k x + \sum_{j=0}^{n-1} a_{kj} x_j &\leq u_k^c, & k = 0, \dots, m-1, \\ l_j^x &\leq x_j &\leq u_j^x, & j = 0, \dots, n-1, \end{aligned} \end{aligned} \quad (7.11)$$

where Q^o and all Q^k are symmetric matrices. Moreover, for convexity, Q^o must be a positive semidefinite matrix and Q^k must satisfy

$$\begin{aligned} -\infty < l_k^c &\Rightarrow Q^k \text{ is negative semidefinite,} \\ u_k^c < \infty &\Rightarrow Q^k \text{ is positive semidefinite,} \\ -\infty < l_k^c \leq u_k^c < \infty &\Rightarrow Q^k = 0. \end{aligned}$$

The convexity requirement is very important and **MOSEK** checks whether it is fulfilled.

7.4.1 A Recommendation

Any convex quadratic optimization problem can be reformulated as a conic quadratic optimization problem, see [MOSEKApS12] and in particular [And13]. In fact **MOSEK** does such conversion internally as a part of the solution process for the following reasons:

- the conic optimizer is numerically more robust than the one for quadratic problems.
- the conic optimizer is usually faster because quadratic cones are simpler than quadratic functions, even though the conic reformulation usually has more constraints and variables than the original quadratic formulation.
- it is easy to dualize the conic formulation if deemed worthwhile potentially leading to (huge) computational savings.

However, instead of relying on the automatic reformulation we recommend to formulate the problem as a conic problem from scratch because:

- it saves the computational overhead of the reformulation including the convexity check. A conic problem is convex by construction and hence no convexity check is needed for conic problems.
- usually the modeller can do a better reformulation than the automatic method because the modeller can exploit the knowledge of the problem at hand.

To summarize we recommend to formulate quadratic problems and in particular quadratically constrained problems directly in conic form.

7.4.2 Duality for Quadratic and Quadratically Constrained Optimization

The dual problem corresponding to the quadratic and quadratically constrained optimization problem (7.11) is given by

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + \frac{1}{2}x^T \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x + c^f \\ & \text{subject to} && \begin{aligned} A^T y + s_l^x - s_u^x + \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x &= c, \\ -y + s_l^c - s_u^c &= 0, \\ s_l^c, s_u^c, s_l^x, s_u^x &\geq 0. \end{aligned} \end{aligned} \quad (7.12)$$

The dual problem is related to the dual problem for linear optimization (see Sec. 7.1.1), but depends on the variable x which in general can not be eliminated. In the solutions reported by **MOSEK**, the value of x is the same for the primal problem (7.11) and the dual problem (7.12).

7.4.3 Infeasibility for Quadratic and Quadratically Constrained Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see Sec. 7.1.2).

Primal Infeasible Problems

If the problem (7.11) with all $Q^k = 0$ is infeasible, **MOSEK** will report a certificate of primal infeasibility. As the constraints are the same as for a linear problem, the certificate of infeasibility is the same as for linear optimization (see Sec. 7.1.2).

Dual Infeasible Problems

If the problem (7.12) with all $Q^k = 0$ is dual infeasible, **MOSEK** will report a certificate of dual infeasibility. The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{array}{ll} \text{minimize} & c^T x \\ \text{subject to} & \hat{l}^c \leq Ax \leq \hat{u}^c, \\ & 0 \leq Q^o x \leq 0, \\ & \hat{l}^x \leq x \leq \hat{u}^x, \end{array}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that the objective value is strictly negative.

7.5 General Convex Optimization

The general nonlinear optimizer (which may be available for all or some types of nonlinear problems depending on the interface), solves smooth (twice differentiable) convex nonlinear optimization problems of the form

$$\begin{array}{ll} \text{minimize} & f(x) + c^T x + c^f \\ \text{subject to} & l^c \leq g(x) + Ax \leq u^c, \\ & l^x \leq x \leq u^x, \end{array}$$

where

- m is the number of constraints.
- n is the number of decision variables.
- $x \in \mathbb{R}^n$ is a vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear part objective function.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.

- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $f : \mathbb{R}^n \rightarrow \mathbb{R}$ is a nonlinear function.
- $g : \mathbb{R}^n \rightarrow \mathbb{R}^m$ is a nonlinear vector function.

This means that the i -th constraint has the form

$$l_i^c \leq g_i(x) + \sum_{j=1}^n a_{ij}x_j \leq u_i^c.$$

The linear term Ax is not included in $g(x)$ since it can be handled much more efficiently as a separate entity when optimizing.

The nonlinear functions f and g must be smooth in all $x \in [l^x; u^x]$. Moreover, $f(x)$ must be a convex function and $g_i(x)$ must satisfy

$$\begin{aligned} -\infty < l_i^c &\Rightarrow g_i(x) \text{ is concave,} \\ u_i^c < \infty &\Rightarrow g_i(x) \text{ is convex,} \\ -\infty < l_i^c \leq u_i^c < \infty &\Rightarrow g_i(x) = 0. \end{aligned}$$

7.5.1 Duality for General convex Optimization

Similarly to the linear case, **MOSEK** reports dual information in the general nonlinear case. Indeed in this case the Lagrange function is defined by

$$\begin{aligned} L(x, s_l^c, s_u^c, s_l^x, s_u^x) &:= f(x) + c^T x + c^f \\ &\quad - (s_l^c)^T (g(x) + Ax - l^c) - (s_u^c)^T (u^c - g(x) - Ax) \\ &\quad - (s_l^x)^T (x - l^x) - (s_u^x)^T (u^x - x), \end{aligned}$$

and the dual problem is given by

$$\begin{aligned} &\text{maximize} && L(x, s_l^c, s_u^c, s_l^x, s_u^x) \\ &\text{subject to} && \nabla_x L(x, s_l^c, s_u^c, s_l^x, s_u^x)^T = 0, \\ &&& s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \end{aligned}$$

which is equivalent to

$$\begin{aligned} &\text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ &&& + f(x) - g(x)^T y - (\nabla f(x)^T - \nabla g(x)^T y)^T x \\ &\text{subject to} && A^T y + s_l^x - s_u^x - (\nabla f(x)^T - \nabla g(x)^T y) = c, \\ &&& -y + s_l^c - s_u^c = 0, \\ &&& s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{aligned}$$

In this context we use the following definition for scalar functions

$$\nabla f(x) = \left[\frac{\partial f(x)}{\partial x_1}, \dots, \frac{\partial f(x)}{\partial x_n} \right],$$

and accordingly for vector functions

$$\nabla g(x) = \begin{bmatrix} \nabla g_1(x) \\ \vdots \\ \nabla g_m(x) \end{bmatrix}.$$

THE OPTIMIZERS FOR CONTINUOUS PROBLEMS

The most essential part of **MOSEK** are the optimizers. This chapter describes the optimizers for the class of *continuous problems* without integer variables, that is:

- linear problems,
- conic problems (quadratic and semidefinite),
- general convex problems.

MOSEK offers an interior-point optimizer for each class of problems and also a simplex optimizer for linear problems. The structure of a successful optimization process is roughly:

- **Presolve**
 1. *Elimination*: Reduce the size of the problem.
 2. *Dualizer*: Choose whether to solve the primal or the dual form of the problem.
 3. *Scaling*: Scale the problem for better numerical stability.
- **Optimization**
 1. *Optimize*: Solve the problem using selected method.
 2. *Terminate*: Stop the optimization when specific termination criteria have been met.
 3. *Report*: Return the solution or an infeasibility certificate.

The preprocessing stage is transparent to the user, but useful to know about for tuning purposes. The purpose of the preprocessing steps is to make the actual optimization more efficient and robust. We discuss the details of the above steps in the following sections.

8.1 Presolve

Before an optimizer actually performs the optimization the problem is preprocessed using the so-called presolve. The purpose of the presolve is to

1. remove redundant constraints,
2. eliminate fixed variables,
3. remove linear dependencies,
4. substitute out (implied) free variables, and
5. reduce the size of the optimization problem in general.

After the presolved problem has been optimized the solution is automatically postsolved so that the returned solution is valid for the original problem. Hence, the presolve is completely transparent. For further details about the presolve phase, please see [\[AA95\]](#) and [\[AGMX96\]](#).

It is possible to fine-tune the behavior of the presolve or to turn it off entirely. If presolve consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This

is done by setting the parameter `MSK_IPAR_PRESOLVE_USE` to `MSK_PRESOLVE_MODE_OFF`. The two most time-consuming steps of the presolve are

- the eliminator, and
- the linear dependency check.

Therefore, in some cases it is worthwhile to disable one or both of these.

Numerical issues in the presolve

During the presolve the problem is reformulated so that it hopefully solves faster. However, in rare cases the presolved problem may be harder to solve than the original problem. The presolve may also be infeasible although the original problem is not. If it is suspected that presolved problem is much harder to solve than the original, we suggest to first turn the eliminator off by setting the parameter `MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES` to 0. If that does not help, then trying to turn entire presolve off may help.

Since all computations are done in finite precision, the presolve employs some tolerances when concluding a variable is fixed or a constraint is redundant. If it happens that **MOSEK** incorrectly concludes a problem is primal or dual infeasible, then it is worthwhile to try to reduce the parameters `MSK_DPAR_PRESOLVE_TOL_X` and `MSK_DPAR_PRESOLVE_TOL_S`. However, if reducing the parameters actually helps then this should be taken as an indication that the problem is badly formulated.

Eliminator

The purpose of the eliminator is to eliminate free and implied free variables from the problem using substitution. For instance, given the constraints

$$\begin{aligned} y &= \sum_j x_j, \\ y, x &\geq 0, \end{aligned}$$

y is an implied free variable that can be substituted out of the problem, if deemed worthwhile. If the eliminator consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This can be done by setting the parameter `MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES` to 0. In rare cases the eliminator may cause that the problem becomes much hard to solve.

Linear dependency checker

The purpose of the linear dependency check is to remove linear dependencies among the linear equalities. For instance, the three linear equalities

$$\begin{aligned} x_1 + x_2 + x_3 &= 1, \\ x_1 + 0.5x_2 &= 0.5, \\ 0.5x_2 + x_3 &= 0.5. \end{aligned}$$

contain exactly one linear dependency. This implies that one of the constraints can be dropped without changing the set of feasible solutions. Removing linear dependencies is in general a good idea since it reduces the size of the problem. Moreover, the linear dependencies are likely to introduce numerical problems in the optimization phase. It is best practice to build models without linear dependencies, but that is not always easy for the user to control. If the linear dependencies are removed at the modelling stage, the linear dependency check can safely be disabled by setting the parameter `MSK_IPAR_PRESOLVE_LINDEP_USE` to `MSK_OFF`.

Dualizer

All linear, conic, and convex optimization problems have an equivalent dual problem associated with them. **MOSEK** has built-in heuristics to determine if it is more efficient to solve the primal or dual

problem. The form (primal or dual) is displayed in the **MOSEK** log and available as an information item from the solver. Should the internal heuristics not choose the most efficient form of the problem it may be worthwhile to set the dualizer manually by setting the parameters:

- `MSK_IPAR_INTPNT_SOLVE_FORM`: In case of the interior-point optimizer.
- `MSK_IPAR_SIM_SOLVE_FORM`: In case of the simplex optimizer.

Note that currently only linear and conic quadratic problems may be automatically dualized.

Scaling

Problems containing data with large and/or small coefficients, say $1.0e + 9$ or $1.0e - 7$, are often hard to solve. Significant digits may be truncated in calculations with finite precision, which can result in the optimizer relying on inaccurate data. Since computers work in finite precision, extreme coefficients should be avoided. In general, data around the same *order of magnitude* is preferred, and we will refer to a problem, satisfying this loose property, as being *well-scaled*. If the problem is not well scaled, **MOSEK** will try to scale (multiply) constraints and variables by suitable constants. **MOSEK** solves the scaled problem to improve the numerical properties.

The scaling process is transparent, i.e. the solution to the original problem is reported. It is important to be aware that the optimizer terminates when the termination criterion is met on the scaled problem, therefore significant primal or dual infeasibilities may occur after unscaling for badly scaled problems. The best solution of this issue is to reformulate the problem, making it better scaled.

By default **MOSEK** heuristically chooses a suitable scaling. The scaling for interior-point and simplex optimizers can be controlled with the parameters `MSK_IPAR_INTPNT_SCALING` and `MSK_IPAR_SIM_SCALING` respectively.

8.2 Using Multiple Threads in an Optimizer

Multithreading in interior-point optimizers

The interior-point optimizers in **MOSEK** have been parallelized. This means that if you solve linear, quadratic, conic, or general convex optimization problem using the interior-point optimizer, you can take advantage of multiple CPU's. By default **MOSEK** will automatically select the number of threads to be employed when solving the problem. However, the maximum number of threads employed can be changed by setting the parameter `MSK_IPAR_NUM_THREADS`. This should never exceed the number of cores on the computer.

The speed-up obtained when using multiple threads is highly problem and hardware dependent, and consequently, it is advisable to compare single threaded and multi threaded performance for the given problem type to determine the optimal settings. For small problems, using multiple threads is not be worthwhile and may even be counter productive because of the additional coordination overhead. Therefore, it may be advantageous to disable multithreading using the parameter `MSK_IPAR_INTPNT_MULTI_THREAD`.

The interior-point optimizer parallelizes big tasks such linear algebra computations.

Thread Safety

The **MOSEK** API is thread-safe provided that a task is only modified or accessed from one thread at any given time. Also accessing two or more separate tasks from threads at the same time is safe. Sharing an environment between threads is safe.

Determinism

The optimizers are run-to-run deterministic which means if a problem is solved twice on the same computer using the same parameter setting and exactly the same input then exactly the same results is obtained. One restriction is that no time limits must be imposed because the time taken to perform an operation on a computer is dependent on many factors such as the current workload.

8.3 Linear Optimization

8.3.1 Optimizer Selection

Two different types of optimizers are available for linear problems: The default is an interior-point method, and the alternative is the simplex method (primal or dual). The optimizer can be selected using the parameter `MSK_IPAR_OPTIMIZER`.

The Interior-point or the Simplex Optimizer?

Given a linear optimization problem, which optimizer is the best: the simplex or the interior-point optimizer? It is impossible to provide a general answer to this question. However, the interior-point optimizer behaves more predictably: it tends to use between 20 and 100 iterations, almost independently of problem size, but cannot perform warm-start. On the other hand the simplex method can take advantage of an initial solution, but is less predictable from cold-start. The interior-point optimizer is used by default.

The Primal or the Dual Simplex Variant?

MOSEK provides both a primal and a dual simplex optimizer. Predicting which simplex optimizer is faster is impossible, however, in recent years the dual optimizer has seen several algorithmic and computational improvements, which, in our experience, make it faster on average than the primal version. Still, it depends much on the problem structure and size. Setting the `MSK_IPAR_OPTIMIZER` parameter to `MSK_OPTIMIZER_FREE_SIMPLEX` instructs **MOSEK** to choose one of the simplex variants automatically.

To summarize, if you want to know which optimizer is faster for a given problem type, it is best to try all the options.

8.3.2 The Interior-point Optimizer

The purpose of this section is to provide information about the algorithm employed in the **MOSEK** interior-point optimizer for linear problems and about its termination criteria.

The homogeneous primal-dual problem

In order to keep the discussion simple it is assumed that **MOSEK** solves linear optimization problems of standard form

$$\begin{aligned} &\text{minimize} && c^T x \\ &\text{subject to} && Ax = b, \\ &&& x \geq 0. \end{aligned} \tag{8.1}$$

This is in fact what happens inside **MOSEK**; for efficiency reasons **MOSEK** converts the problem to standard form before solving, then converts it back to the input form when reporting the solution.

Since it is not known beforehand whether problem (8.1) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason why **MOSEK** solves the so-called homogeneous model

$$\begin{aligned} Ax - b\tau &= 0, \\ A^T y + s - c\tau &= 0, \\ -c^T x + b^T y - \kappa &= 0, \\ x, s, \tau, \kappa &\geq 0, \end{aligned} \tag{8.2}$$

where y and s correspond to the dual variables in (8.1), and τ and κ are two additional scalar variables. Note that the homogeneous model (8.2) always has solution since

$$(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)$$

is a solution, although not a very interesting one. Any solution

$$(x^*, y^*, s^*, \tau^*, \kappa^*)$$

to the homogeneous model (8.2) satisfies

$$x_j^* s_j^* = 0 \text{ and } \tau^* \kappa^* = 0.$$

Moreover, there is always a solution that has the property $\tau^* + \kappa^* > 0$.

First, assume that $\tau^* > 0$. It follows that

$$\begin{aligned} A \frac{x^*}{\tau^*} &= b, \\ A^T \frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} &= c, \\ -c^T \frac{x^*}{\tau^*} + b^T \frac{y^*}{\tau^*} &= 0, \\ x^*, s^*, \tau^*, \kappa^* &\geq 0. \end{aligned}$$

This shows that $\frac{x^*}{\tau^*}$ is a primal optimal solution and $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau^*})$ is a dual optimal solution; this is reported as the optimal interior-point solution since

$$(x, y, s) = \left\{ \frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*} \right\}$$

is a primal-dual optimal solution (see [Sec. 7.1](#) for the mathematical background on duality and optimality).

On other hand, if $\kappa^* > 0$ then

$$\begin{aligned} Ax^* &= 0, \\ A^T y^* + s^* &= 0, \\ -c^T x^* + b^T y^* &= \kappa^*, \\ x^*, s^*, \tau^*, \kappa^* &\geq 0. \end{aligned}$$

This implies that at least one of

$$c^T x^* < 0 \tag{8.3}$$

or

$$b^T y^* > 0 \tag{8.4}$$

is satisfied. If (8.3) is satisfied then x^* is a certificate of dual infeasibility, whereas if (8.4) is satisfied then y^* is a certificate of primal infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm [\[And09\]](#).

Interior-point Termination Criterion

For efficiency reasons it is not practical to solve the homogeneous model exactly. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In the k -th iteration of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to homogeneous model is generated, where

$$x^k, s^k, \tau^k, \kappa^k > 0.$$

Optimal case

Whenever the trial solution satisfies the criterion

$$\begin{aligned} \left\| A \frac{x^k}{\tau^k} - b \right\|_{\infty} &\leq \epsilon_p (1 + \|b\|_{\infty}), \\ \left\| A^T \frac{y^k}{\tau^k} + \frac{s^k}{\tau^k} - c \right\|_{\infty} &\leq \epsilon_d (1 + \|c\|_{\infty}), \text{ and} \\ \min \left(\frac{(x^k)^T s^k}{(\tau^k)^2}, \left| \frac{c^T x^k}{\tau^k} - \frac{b^T y^k}{\tau^k} \right| \right) &\leq \epsilon_g \max \left(1, \frac{\min(|c^T x^k|, |b^T y^k|)}{\tau^k} \right), \end{aligned} \quad (8.5)$$

the interior-point optimizer is terminated and

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is reported as the primal-dual optimal solution. The interpretation of (8.5) is that the optimizer is terminated if

- $\frac{x^k}{\tau^k}$ is approximately primal feasible,
- $\left\{ \frac{y^k}{\tau^k}, \frac{s^k}{\tau^k} \right\}$ is approximately dual feasible, and
- the duality gap is almost zero.

Dual infeasibility certificate

On the other hand, if the trial solution satisfies

$$-\epsilon_i c^T x^k > \frac{\|c\|_{\infty}}{\max(1, \|b\|_{\infty})} \|Ax^k\|_{\infty}$$

then the problem is declared dual infeasible and x^k is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows: First assume that $\|Ax^k\|_{\infty} = 0$; then x^k is an exact certificate of dual infeasibility. Next assume that this is not the case, i.e.

$$\|Ax^k\|_{\infty} > 0,$$

and define

$$\bar{x} := \epsilon_i \frac{\max(1, \|b\|_{\infty})}{\|Ax^k\|_{\infty} \|c\|_{\infty}} x^k.$$

It is easy to verify that

$$\|A\bar{x}\|_{\infty} = \epsilon_i \frac{\max(1, \|b\|_{\infty})}{\|c\|_{\infty}} \text{ and } -c^T \bar{x} > 1,$$

which shows \bar{x} is an approximate certificate of dual infeasibility, where ϵ_i controls the quality of the approximation. A smaller value means a better approximation.

Primal infeasibility certificate

Finally, if

$$\epsilon_i b^T y^k > \frac{\|b\|_\infty}{\max(1, \|c\|_\infty)} \|A^T y^k + s^k\|_\infty$$

then y^k is reported as a certificate of primal infeasibility.

Adjusting optimality criteria and near optimality

It is possible to adjust the tolerances ε_p , ε_d , ε_g and ε_i using parameters; see table for details.

Table 8.1: Parameters employed in termination criterion

ToleranceParameter	name
ε_p	<i>MSK_DPAR_INTPNT_TOL_PFEAS</i>
ε_d	<i>MSK_DPAR_INTPNT_TOL_DFEAS</i>
ε_g	<i>MSK_DPAR_INTPNT_TOL_REL_GAP</i>
ε_i	<i>MSK_DPAR_INTPNT_TOL_INFEAS</i>

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (8.5) reveals that the quality of the solution depends on $\|b\|_\infty$ and $\|c\|_\infty$; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate [And09]. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances, ε_p , ε_d , ε_g and ε_i , have to be relaxed together to achieve an effect.

In some cases the interior-point method terminates having found a solution not too far from meeting the optimality condition (8.5). A solution is defined as *near optimal* if scaling the termination tolerances ε_p , ε_d , ε_g and ε_i by the same factor $\varepsilon_n \in [1.0, +\infty]$ makes the condition (8.5) satisfied. A near optimal solution is therefore of lower quality but still potentially valuable. If for instance the solver stalls, i.e. it can make no more significant progress towards the optimal solution, a near optimal solution could be available and be good enough for the user. Near infeasibility certificates are defined similarly. The value of ε_n can be adjusted with the parameter *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*.

The basis identification discussed in Sec. 8.3.2 requires an optimal solution to work well; hence basis identification should be turned off if the termination criterion is relaxed.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

Basis Identification

An interior-point optimizer does not return an optimal basic solution unless the problem has a unique primal and dual optimal solution. Therefore, the interior-point optimizer has an optional post-processing step that computes an optimal basic solution starting from the optimal interior-point solution. More information about the basis identification procedure may be found in [AY96]. In the following we provide an overall idea of the procedure.

There are some cases in which a basic solution could be more valuable:

- a basic solution is often more accurate than an interior-point solution,
- a basic solution can be used to warm-start the simplex algorithm in case of reoptimization,
- a basic solution is in general more sparse, i.e. more variables are fixed to zero. This is particularly appealing when solving continuous relaxations of mixed integer problems, as well as in all applications in which sparser solutions are preferred.

problem dimensions as seen by the optimizer, and the **Factor...** lines show various statistics. This is followed by the iteration log.

Using the same notation as in [Sec. 8.3.2](#) the columns of the iteration log have the following meaning:

- **ITE**: Iteration index k .
- **PFEAS**: $\|Ax^k - b\tau^k\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- **DFEAS**: $\|A^T y^k + s^k - c\tau^k\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- **GFEAS**: $|-c^T x^k + b^T y^k - \kappa^k|$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- **PRSTATUS**: This number converges to 1 if the problem has an optimal solution whereas it converges to -1 if that is not the case.
- **POBJ**: $c^T x^k / \tau^k$. An estimate for the primal objective value.
- **DOBJ**: $b^T y^k / \tau^k$. An estimate for the dual objective value.
- **MU**: $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$. The numbers in this column should always converge to zero.
- **TIME**: Time spent since the optimization started.

8.3.3 The Simplex Optimizer

An alternative to the interior-point optimizer is the simplex optimizer. The simplex optimizer uses a different method that allows exploiting an initial guess for the optimal solution to reduce the solution time. Depending on the problem it may be faster or slower to use an initial guess; see [Sec. 8.3.1](#) for a discussion. **MOSEK** provides both a primal and a dual variant of the simplex optimizer.

Simplex Termination Criterion

The simplex optimizer terminates when it finds an optimal basic solution or an infeasibility certificate. A basic solution is optimal when it is primal and dual feasible; see [Sec. 7.1](#) for a definition of the primal and dual problem. Due to the fact that computations are performed in finite precision **MOSEK** allows violations of primal and dual feasibility within certain tolerances. The user can control the allowed primal and dual tolerances with the parameters `MSK_DPAR_BASIS_TOL_X` and `MSK_DPAR_BASIS_TOL_S`.

Setting the parameter `MSK_IPAR_OPTIMIZER` to `MSK_OPTIMIZER_FREE_SIMPLEX` instructs **MOSEK** to select automatically between the primal and the dual simplex optimizers. Hence, **MOSEK** tries to choose the best optimizer for the given problem and the available solution. The same parameter can also be used to force one of the variants.

Starting From an Existing Solution

When using the simplex optimizer it may be possible to reuse an existing solution and thereby reduce the solution time significantly. When a simplex optimizer starts from an existing solution it is said to perform a *warm-start*. If the user is solving a sequence of optimization problems by solving the problem, making modifications, and solving again, **MOSEK** will warm-start automatically.

By default **MOSEK** uses presolve when performing a warm-start. If the optimizer only needs very few iterations to find the optimal solution it may be better to turn off the presolve.

Numerical Difficulties in the Simplex Optimizers

Though **MOSEK** is designed to minimize numerical instability, completely avoiding it is impossible when working in finite precision. **MOSEK** treats a “numerically unexpected behavior” event inside the optimizer as a *set-back*. The user can define how many set-backs the optimizer accepts; if that number is exceeded, the optimization will be aborted. Set-backs are a way to escape long sequences where the optimizer tries to recover from an unstable situation.

Examples of set-backs are: repeated singularities when factorizing the basis matrix, repeated loss of feasibility, degeneracy problems (no progress in objective) and other events indicating numerical difficulties. If the simplex optimizer encounters a lot of set-backs the problem is usually badly scaled; in such a situation try to reformulate it into a better scaled problem. Then, if a lot of set-backs still occur, trying one or more of the following suggestions may be worthwhile:

- Raise tolerances for allowed primal or dual feasibility: increase the value of
 - `MSK_DPAR_BASIS_TOL_X`, and
 - `MSK_DPAR_BASIS_TOL_S`.
- Raise or lower pivot tolerance: Change the `MSK_DPAR_SIMPLEX_ABS_TOL_PIV` parameter.
- Switch optimizer: Try another optimizer.
- Switch off crash: Set both `MSK_IPAR_SIM_PRIMAL_CRASH` and `MSK_IPAR_SIM_DUAL_CRASH` to 0.
- Experiment with other pricing strategies: Try different values for the parameters
 - `MSK_IPAR_SIM_PRIMAL_SELECTION` and
 - `MSK_IPAR_SIM_DUAL_SELECTION`.
- If you are using warm-starts, in rare cases switching off this feature may improve stability. This is controlled by the `MSK_IPAR_SIM_HOTSTART` parameter.
- Increase maximum number of set-backs allowed controlled by `MSK_IPAR_SIM_MAX_NUM_SETBACKS`.
- If the problem repeatedly becomes infeasible try switching off the special degeneracy handling. See the parameter `MSK_IPAR_SIM_DEGEN` for details.

The Simplex Log

Below is a typical log output from the simplex optimizer:

Optimizer	- solved problem	:	the primal			
Optimizer	- Constraints	:	667			
Optimizer	- Scalar variables	:	1424	conic	:	0
Optimizer	- hotstart	:	no			
ITER	DEGITER(%)	PFEAS	DFEAS	POBJ	DOBJ	TIME
↪	TOTTIME					
0	0.00	1.43e+05	NA	6.5584140832e+03	NA	0.00
↪	0.02					
1000	1.10	0.00e+00	NA	1.4588289726e+04	NA	0.13
↪	0.14					
2000	0.75	0.00e+00	NA	7.3705564855e+03	NA	0.21
↪	0.22					
3000	0.67	0.00e+00	NA	6.0509727712e+03	NA	0.29
↪	0.31					
4000	0.52	0.00e+00	NA	5.5771203906e+03	NA	0.38
↪	0.39					
4533	0.49	0.00e+00	NA	5.5018458883e+03	NA	0.42
↪	0.44					

The first lines summarize the problem the optimizer is solving. This is followed by the iteration log, with the following meaning:

- ITER: Number of iterations.
- DEGITER(%): Ratio of degenerate iterations.
- PFEAS: Primal feasibility measure reported by the simplex optimizer. The numbers should be 0 if the problem is primal feasible (when the primal variant is used).
- DFEAS: Dual feasibility measure reported by the simplex optimizer. The number should be 0 if the problem is dual feasible (when the dual variant is used).
- POBJ: An estimate for the primal objective value (when the primal variant is used).
- DOBJ: An estimate for the dual objective value (when the dual variant is used).
- TIME: Time spent since this instance of the simplex optimizer was invoked (in seconds).
- TOTTIME: Time spent since optimization started (in seconds).

8.4 Conic Optimization

For conic optimization problems only an interior-point type optimizer is available.

8.4.1 The Interior-point optimizer

The homogeneous primal-dual problem

The interior-point optimizer is an implementation of the so-called homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see [\[ART03\]](#). In order to keep our discussion simple we will assume that **MOSEK** solves a conic optimization problem of the form:

$$\begin{aligned} & \text{minimize} && c^T x \\ & \text{subject to} && Ax = b, \\ & && x \in \mathcal{K} \end{aligned} \tag{8.6}$$

where \mathcal{K} is a convex cone. The corresponding dual problem is

$$\begin{aligned} & \text{maximize} && b^T y \\ & \text{subject to} && A^T y + s = c, \\ & && x \in \mathcal{K}^* \end{aligned} \tag{8.7}$$

where \mathcal{K}^* is the dual cone of \mathcal{K} . See [Sec. 7.2](#) for definitions.

Since it is not known beforehand whether problem (8.6) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason that **MOSEK** solves the so-called homogeneous model

$$\begin{aligned} Ax - b\tau &= 0, \\ A^T y + s - c\tau &= 0, \\ -c^T x + b^T y - \kappa &= 0, \\ x &\in \mathcal{K}, \\ s &\in \mathcal{K}^*, \\ \tau, \kappa &\geq 0, \end{aligned} \tag{8.8}$$

where y and s correspond to the dual variables in (8.6), and τ and κ are two additional scalar variables. Note that the homogeneous model (8.8) always has a solution since

$$(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)$$

is a solution, although not a very interesting one. Any solution

$$(x^*, y^*, s^*, \tau^*, \kappa^*)$$

to the homogeneous model (8.8) satisfies

$$(x^*)^T s^* + \tau^* \kappa^* = 0$$

i.e. complementarity. Observe that $x^* \in \mathcal{K}$ and $s^* \in \mathcal{K}^*$ implies

$$(x^*)^T s^* \geq 0$$

and therefore

$$\tau^* \kappa^* = 0.$$

since $\tau^*, \kappa^* \geq 0$. Hence, at least one of τ^* and κ^* is zero.

First, assume that $\tau^* > 0$ and hence $\kappa^* = 0$. It follows that

$$\begin{aligned} A \frac{x^*}{\tau^*} &= b, \\ A^T \frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} &= c, \\ -c^T \frac{x^*}{\tau^*} + b^T \frac{y^*}{\tau^*} &= 0, \\ x^*/\tau^* &\in \mathcal{K}, \\ s^*/\tau^* &\in \mathcal{K}^*. \end{aligned}$$

This shows that $\frac{x^*}{\tau^*}$ is a primal optimal solution and $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau^*})$ is a dual optimal solution; this is reported as the optimal interior-point solution since

$$(x, y, s) = \left(\frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*} \right)$$

is a primal-dual optimal solution.

On other hand, if $\kappa^* > 0$ then

$$\begin{aligned} Ax^* &= 0, \\ A^T y^* + s^* &= 0, \\ -c^T x^* + b^T y^* &= \kappa^*, \\ x^* &\in \mathcal{K}, \\ s^* &\in \mathcal{K}^*. \end{aligned}$$

This implies that at least one of

$$c^T x^* < 0 \tag{8.9}$$

or

$$b^T y^* > 0 \tag{8.10}$$

holds. If (8.9) is satisfied, then x^* is a certificate of dual infeasibility, whereas if (8.10) holds then y^* is a certificate of primal infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm [And09].

Interior-point Termination Criterion

Since computations are performed in finite precision, and for efficiency reasons, it is not possible to solve the homogeneous model exactly in general. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In every iteration k of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to the homogeneous model is generated, where

$$x^k \in \mathcal{K}, s^k \in \mathcal{K}^*, \tau^k, \kappa^k > 0.$$

Therefore, it is possible to compute the values:

$$\begin{aligned} \rho_p^k &= \arg \min_{\rho} \left\{ \rho \mid \left\| A \frac{x^k}{\tau^k} - b \right\|_{\infty} \leq \rho \varepsilon_p (1 + \|b\|_{\infty}) \right\}, \\ \rho_d^k &= \arg \min_{\rho} \left\{ \rho \mid \left\| A^T \frac{y^k}{\tau^k} + \frac{s^k}{\tau^k} - c \right\|_{\infty} \leq \rho \varepsilon_d (1 + \|c\|_{\infty}) \right\}, \\ \rho_g^k &= \arg \min_{\rho} \left\{ \rho \mid \left(\frac{(x^k)^T s^k}{(\tau^k)^2}, \left| \frac{c^T x^k}{\tau^k} - \frac{b^T y^k}{\tau^k} \right| \right) \leq \rho \varepsilon_g \max \left(1, \frac{\min(|c^T x^k|, |b^T y^k|)}{\tau^k} \right) \right\}, \\ \rho_{pi}^k &= \arg \min_{\rho} \left\{ \rho \mid \left\| A^T y^k + s^k \right\|_{\infty} \leq \rho \varepsilon_i b^T y^k, b^T y^k > 0 \right\} \text{ and} \\ \rho_{di}^k &= \arg \min_{\rho} \left\{ \rho \mid \left\| A x^k \right\|_{\infty} \leq -\rho \varepsilon_i c^T x^k, c^T x^k < 0 \right\}. \end{aligned}$$

Note $\varepsilon_p, \varepsilon_d, \varepsilon_g$ and ε_i are nonnegative user specified tolerances.

Optimal Case

Observe ρ_p^k measures how far x^k/τ^k is from being a good approximate primal feasible solution. Indeed if $\rho_p^k \leq 1$, then

$$\left\| A \frac{x^k}{\tau^k} - b \right\|_{\infty} \leq \varepsilon_p (1 + \|b\|_{\infty}). \quad (8.11)$$

This shows the violations in the primal equality constraints for the solution x^k/τ^k is small compared to the size of b given ε_p is small.

Similarly, if $\rho_d^k \leq 1$, then $(y^k, s^k)/\tau^k$ is an approximate dual feasible solution. If in addition $\rho_g^k \leq 1$, then the solution $(x^k, y^k, s^k)/\tau^k$ is approximate optimal because the associated primal and dual objective values are almost identical.

In other words if $\max(\rho_p^k, \rho_d^k, \rho_g^k) \leq 1$, then

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is an approximate optimal solution.

Dual Infeasibility Certificate

Next assume that $\rho_{di}^k \leq 1$ and hence

$$\left\| A x^k \right\|_{\infty} \leq -\varepsilon_i c^T x^k \text{ and } -c^T x^k > 0$$

holds. Now in this case the problem is declared dual infeasible and x^k is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows. Let

$$\bar{x} := \frac{x^k}{-c^T x^k}$$

and it is easy to verify that

$$\left\| A \bar{x} \right\|_{\infty} \leq \varepsilon_i \text{ and } c^T \bar{x} = -1$$

which shows \bar{x} is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation.

Primal Infeasibility Certificate

Next assume that $\rho_{pi}^k \leq 1$ and hence

$$\|A^T y^k + s^k\|_\infty \leq \varepsilon_i b^T y^k \text{ and } b^T y^k > 0$$

holds. Now in this case the problem is declared primal infeasible and (y^k, s^k) is reported as a certificate of primal infeasibility. The motivation for this stopping criterion is as follows. Let

$$\bar{y} := \frac{y^k}{b^T y^k} \text{ and } \bar{s} := \frac{s^k}{b^T y^k}$$

and it is easy to verify that

$$\|A^T \bar{y} + \bar{s}\|_\infty \leq \varepsilon_i \text{ and } b^T \bar{y} = 1$$

which shows (y^k, s^k) is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation.

Adjusting optimality criteria and near optimality

It is possible to adjust the tolerances ε_p , ε_d , ε_g and ε_i using parameters; see table for details.

Table 8.2: Parameters employed in termination criterion

Tolerance	Parameter	name
ε_p		<i>MSK_DPAR_INTPNT_CO_TOL_PFEAS</i>
ε_d		<i>MSK_DPAR_INTPNT_CO_TOL_DFEAS</i>
ε_g		<i>MSK_DPAR_INTPNT_CO_TOL_REL_GAP</i>
ε_i		<i>MSK_DPAR_INTPNT_CO_TOL_INFEAS</i>

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (8.11) reveals that the quality of the solution depends on $\|b\|_\infty$ and $\|c\|_\infty$; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate [And09]. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances, ε_p , ε_d , ε_g and ε_i , have to be relaxed together to achieve an effect.

In some cases the interior-point method terminates having found a solution not too far from meeting the optimality condition (8.11). A solution is defined as *near optimal* if scaling the termination tolerances ε_p , ε_d , ε_g and ε_i by the same factor $\varepsilon_n \in [1.0, +\infty]$ makes the condition (8.11) satisfied. A near optimal solution is therefore of lower quality but still potentially valuable. If for instance the solver stalls, i.e. it can make no more significant progress towards the optimal solution, a near optimal solution could be available and be good enough for the user. Near infeasibility certificates are defined similarly. The value of ε_n can be adjusted with the parameter *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

The Interior-point Log

Below is a typical log output from the interior-point optimizer:

```
Optimizer - threads           : 20
Optimizer - solved problem    : the primal
Optimizer - Constraints       : 1
Optimizer - Cones             : 2
```

Optimizer	-	Scalar variables	:	6	conic	:	6	
Optimizer	-	Semi-definite variables:	0	scalarized	:	0		
Factor	-	setup time	:	0.00	dense det. time	:	0.00	
Factor	-	ML order time	:	0.00	GP order time	:	0.00	
Factor	-	nonzeros before factor	:	1	after factor	:	1	
Factor	-	dense dim.	:	0	flops	:	1.70e+01	
ITE	PFEAS	DFEAS	GFEAS	PRSTATUS	POBJ	DOBJ	MU	TIME
0	1.0e+00	2.9e-01	3.4e+00	0.00e+00	2.414213562e+00	0.000000000e+00	1.0e+00	0.01
1	2.7e-01	7.9e-02	2.2e+00	8.83e-01	6.969257574e-01	-9.685901771e-03	2.7e-01	0.01
2	6.5e-02	1.9e-02	1.2e+00	1.16e+00	7.606090061e-01	6.046141322e-01	6.5e-02	0.01
3	1.7e-03	5.0e-04	2.2e-01	1.12e+00	7.084385672e-01	7.045122560e-01	1.7e-03	0.01
4	1.4e-08	4.2e-09	4.9e-08	1.00e+00	7.071067941e-01	7.071067599e-01	1.4e-08	0.01

The first line displays the number of threads used by the optimizer and the second line tells that the optimizer chose to solve the dual problem rather than the primal problem. The next line displays the problem dimensions as seen by the optimizer, and the **Factor...** lines show various statistics. This is followed by the iteration log.

Using the same notation as in [Sec. 8.4.1](#) the columns of the iteration log have the following meaning:

- **ITE**: Iteration index k .
- **PFEAS**: $\|Ax^k - b\tau^k\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- **DFEAS**: $\|A^T y^k + s^k - c\tau^k\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- **GFEAS**: $|-c^T x^k + b^T y^k - \kappa^k|$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- **PRSTATUS**: This number converges to 1 if the problem has an optimal solution whereas it converges to -1 if that is not the case.
- **POBJ**: $c^T x^k / \tau^k$. An estimate for the primal objective value.
- **DOBJ**: $b^T y^k / \tau^k$. An estimate for the dual objective value.
- **MU**: $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$. The numbers in this column should always converge to zero.
- **TIME**: Time spent since the optimization started (in seconds).

8.5 Nonlinear Convex Optimization

8.5.1 The Interior-point Optimizer

For general convex optimization problems an interior-point type optimizer is available. The interior-point optimizer is an implementation of the homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see [\[AY98\]](#), [\[AY99\]](#).

The Convexity Requirement

Continuous nonlinear problems are required to be convex. For quadratic problems **MOSEK** tests this requirement before optimizing. Specifying a non-convex problem results in an error message.

The following parameters are available to control the convexity check:

- **MSK_IPAR_CHECK_CONVEXITY**: Turn convexity check on/off.
- **MSK_DPAR_CHECK_CONVEXITY_REL_TOL**: Tolerance for convexity check.
- **MSK_IPAR_LOG_CHECK_CONVEXITY**: Turn on more log information for debugging.

The Differentiability Requirement

The nonlinear optimizer in **MOSEK** requires both first order and second order derivatives. This of course implies care should be taken when solving problems involving non-differentiable functions.

For instance, the function

$$f(x) = x^2$$

is differentiable everywhere whereas the function

$$f(x) = \sqrt{x}$$

is only differentiable for $x > 0$. In order to make sure that **MOSEK** evaluates the functions at points where they are differentiable, the function domains must be defined by setting appropriate variable bounds.

In general, if a variable is not ranged **MOSEK** will only evaluate that variable at points strictly within the bounds. Hence, imposing the bound

$$x \geq 0$$

in the case of \sqrt{x} is sufficient to guarantee that the function will only be evaluated in points where it is differentiable.

However, if a function is defined on a closed range, specifying the variable bounds is not sufficient. Consider the function

$$f(x) = \frac{1}{x} + \frac{1}{1-x}. \quad (8.12)$$

In this case the bounds

$$0 \leq x \leq 1$$

will not guarantee that **MOSEK** only evaluates the function for x strictly between 0 and 1. To force **MOSEK** to strictly satisfy both bounds on ranged variables set the parameter *MSK_IPAR_INTPNT_STARTING_POINT* to *MSK_STARTING_POINT_SATISFY_BOUNDS*.

For efficiency reasons it may be better to reformulate the problem than to force **MOSEK** to observe ranged bounds strictly. For instance, (8.12) can be reformulated as follows

$$\begin{aligned} f(x) &= \frac{1}{x} + \frac{1}{y} \\ 0 &= 1 - x - y \\ 0 &\leq x \\ 0 &\leq y. \end{aligned}$$

Interior-point Termination Criteria

The parameters controlling when the general convex interior-point optimizer terminates are shown in Table 8.3.

Table 8.3: Parameters employed in termination criteria.

Parameter name	Purpose
<i>MSK_DPAR_INTPNT_NL_TOL_PFEAS</i>	Controls primal feasibility
<i>MSK_DPAR_INTPNT_NL_TOL_DFEAS</i>	Controls dual feasibility
<i>MSK_DPAR_INTPNT_NL_TOL_REL_GAP</i>	Controls relative gap
<i>MSK_DPAR_INTPNT_TOL_INFEAS</i>	Controls when the problem is declared infeasible
<i>MSK_DPAR_INTPNT_NL_TOL_MU_RED</i>	Controls when the complementarity is reduced enough

THE OPTIMIZER FOR MIXED-INTEGER PROBLEMS

A problem is a mixed-integer optimization problem when one or more of the variables are constrained to be integer valued. Readers unfamiliar with integer optimization are recommended to consult some relevant literature, e.g. the book [Wol98] by Wolsey.

9.1 The Mixed-integer Optimizer Overview

MOSEK can solve mixed-integer

- linear,
- quadratic and quadratically constrained, and
- conic quadratic

problems, at least as long as they do not contain both quadratic objective or constraints and conic constraints at the same time. The mixed-integer optimizer is specialized for solving linear and conic optimization problems. Pure quadratic and quadratically constrained problems are automatically converted to conic form.

By default the mixed-integer optimizer is run-to-run deterministic. This means that if a problem is solved twice on the same computer with identical parameter settings and no time limit then the obtained solutions will be identical. If a time limit is set then this may not be case since the time taken to solve a problem is not deterministic. The mixed-integer optimizer is parallelized i.e. it can exploit multiple cores during the optimization.

The solution process can be split into these phases:

1. **Presolve:** See Sec. 8.1.
2. **Cut generation:** Valid inequalities (cuts) are added to improve the lower bound.
3. **Heuristic:** Using heuristics the optimizer tries to guess a good feasible solution. Heuristics can be controlled by the parameter `MSK_IPAR_MIO_HEURISTIC_LEVEL`.
4. **Search:** The optimal solution is located by branching on integer variables.

9.2 Relaxations and bounds

It is important to understand that, in a worst-case scenario, the time required to solve integer optimization problems grows exponentially with the size of the problem (solving mixed-integer problems is NP-hard). For instance, a problem with n binary variables, may require time proportional to 2^n . The value of 2^n is huge even for moderate values of n .

In practice this implies that the focus should be on computing a near-optimal solution quickly rather than on locating an optimal solution. Even if the problem is only solved approximately, it is important to know how far the approximate solution is from an optimal one. In order to say something about the quality of an approximate solution the concept of *relaxation* is important.

Consider for example a mixed-integer optimization problem

$$\begin{aligned} z^* = \quad & \text{minimize} && c^T x \\ & \text{subject to} && Ax = b, \\ & && x \geq 0 \\ & && x_j \in \mathbb{Z}, \quad \forall j \in \mathcal{J}. \end{aligned} \tag{9.1}$$

It has the continuous relaxation

$$\begin{aligned} \underline{z} = \quad & \text{minimize} && c^T x \\ & \text{subject to} && Ax = b, \\ & && x \geq 0 \end{aligned} \tag{9.2}$$

obtained simply by ignoring the integrality restrictions. The relaxation is a continuous problem, and therefore much faster to solve to optimality with a linear (or, in the general case, conic) optimizer. We call the optimal value \underline{z} the *objective bound*. The objective bound \underline{z} normally increases during the solution search process when the continuous relaxation is gradually refined.

Moreover, if \hat{x} is any feasible solution to (9.1) and

$$\bar{z} := c^T \hat{x}$$

then

$$\underline{z} \leq z^* \leq \bar{z}.$$

These two inequalities allow us to estimate the quality of the integer solution: it is no further away from the optimum than $\bar{z} - \underline{z}$ in terms of the objective value. Whenever a mixed-integer problem is solved **MOSEK** reports this lower bound so that the quality of the reported solution can be evaluated.

9.3 Termination Criterion

In general, it is time consuming to find an exact feasible and optimal solution to an integer optimization problem, though in many practical cases it may be possible to find a sufficiently good solution. The issue of terminating the mixed-integer optimizer is rather delicate and the user has numerous possibilities of influencing it with various parameters. The mixed-integer optimizer employs a relaxed feasibility and optimality criterion to determine when a satisfactory solution is located.

A candidate solution that is feasible for the continuous relaxation is said to be an *integer feasible solution* if the criterion

$$\min(x_j - \lfloor x_j \rfloor, \lceil x_j \rceil - x_j) \leq \delta_1 \quad \forall j \in \mathcal{J}$$

is satisfied, meaning that x_j is at most δ_1 from the nearest integer.

Whenever the integer optimizer locates an integer feasible solution it will check if the criterion

$$\bar{z} - \underline{z} \leq \max(\delta_2, \delta_3 \max(10^{-10}, |\bar{z}|))$$

is satisfied. If this is the case, the integer optimizer terminates and reports the integer feasible solution as an optimal solution. If an optimal solution cannot be located after the time specified by the parameter `MSK_DPAR_MIO_DISABLE_TERM_TIME` (in seconds), it may be advantageous to relax the termination criteria, and they become replaced with

$$\bar{z} - \underline{z} \leq \max(\delta_4, \delta_5 \max(10^{-10}, |\bar{z}|)).$$

Any solution satisfying those will now be reported as **near optimal** and the solver will be terminated (note that since this criterion depends on timing, the optimizer will not be run to run deterministic).

All the δ tolerances discussed above can be adjusted using suitable parameters — see [Table 9.1](#).

Table 9.1: Tolerances for the mixed-integer optimizer.

Tolerance	Parameter name
δ_1	<i>MSK_DPAR_MIO_TOL_ABS_RELAX_INT</i>
δ_2	<i>MSK_DPAR_MIO_TOL_ABS_GAP</i>
δ_3	<i>MSK_DPAR_MIO_TOL_REL_GAP</i>
δ_4	<i>MSK_DPAR_MIO_NEAR_TOL_ABS_GAP</i>
δ_5	<i>MSK_DPAR_MIO_NEAR_TOL_REL_GAP</i>

In Table 9.2 some other common parameters affecting the integer optimizer termination criterion are shown. Please note that if the effect of a parameter is delayed, the associated termination criterion is applied only after some time, specified by the *MSK_DPAR_MIO_DISABLE_TERM_TIME* parameter.

Table 9.2: Other parameters affecting the integer optimizer termination criterion.

Parameter name	De-layed	Explanation
<i>MSK_IPAR_MIO_MAX_NUM_BRANCHES</i>	Yes	Maximum number of branches allowed.
<i>MSK_IPAR_MIO_MAX_NUM_RELAXS</i>	Yes	Maximum number of relaxations allowed.
<i>MSK_IPAR_MIO_MAX_NUM_SOLUTIONS</i>	Yes	Maximum number of feasible integer solutions allowed.

9.4 Speeding Up the Solution Process

As mentioned previously, in many cases it is not possible to find an optimal solution to an integer optimization problem in a reasonable amount of time. Some suggestions to reduce the solution time are:

- Relax the termination criterion: In case the run time is not acceptable, the first thing to do is to relax the termination criterion — see Sec. 9.3 for details.
- Specify a good initial solution: In many cases a good feasible solution is either known or easily computed using problem-specific knowledge. If a good feasible solution is known, it is usually worthwhile to use this as a starting point for the integer optimizer.
- Improve the formulation: A mixed-integer optimization problem may be impossible to solve in one form and quite easy in another form. However, it is beyond the scope of this manual to discuss good formulations for mixed-integer problems. For discussions on this topic see for example [Wol98].

9.5 Understanding Solution Quality

To determine the quality of the solution one should check the following:

- The problem status and solution status returned by **MOSEK**, as well as constraint violations in case of suboptimal solutions.
- The *optimality gap* defined as

$$\epsilon = |(\text{objective value of feasible solution}) - (\text{objective bound})| = |\bar{z} - \underline{z}|.$$

which measures how much the located solution can deviate from the optimal solution to the problem. The optimality gap can be retrieved through the information item *MSK_DINF_MIO_OBJ_ABS_GAP*. Often it is more meaningful to look at the relative optimality gap normalized against the magnitude of the solution.

$$\epsilon_{\text{rel}} = \frac{|\bar{z} - \underline{z}|}{\max(10^{-10}, |\bar{z}|)}.$$

The relative optimality gap is available in *MSK_DINF_MIO_OBJ_REL_GAP*.

9.6 The Optimizer Log

Below is a typical log output from the mixed-integer optimizer:

```
Presolved problem: 6573 variables, 35728 constraints, 101258 non-zeros
Presolved problem: 0 general integer, 4294 binary, 2279 continuous
Clique table size: 1636
BRANCHES RELAXS  ACT_NDS  DEPTH  BEST_INT_OBJ      BEST_RELAX_OBJ      REL_GAP(%)  TIME
0          1        0       0      NA             1.8218819866e+07      NA           1.6
0          1        0       0      1.8331557950e+07    1.8218819866e+07      0.61         3.5
0          1        0       0      1.8300507546e+07    1.8218819866e+07      0.45         4.3
Cut generation started.
0          2        0       0      1.8300507546e+07    1.8218819866e+07      0.45         5.3
Cut generation terminated. Time = 1.43
0          3        0       0      1.8286893047e+07    1.8231580587e+07      0.30         7.5
15         18        1       0      1.8286893047e+07    1.8231580587e+07      0.30        10.5
31         34        1       0      1.8286893047e+07    1.8231580587e+07      0.30        11.1
51         54        1       0      1.8286893047e+07    1.8231580587e+07      0.30        11.6
91         94        1       0      1.8286893047e+07    1.8231580587e+07      0.30        12.4
171        174        1       0      1.8286893047e+07    1.8231580587e+07      0.30        14.3
331        334        1       0      1.8286893047e+07    1.8231580587e+07      0.30        17.9

[ ... ]

Objective of best integer solution : 1.825846762609e+07
Best objective bound                : 1.823311032986e+07
Construct solution objective         : Not employed
Construct solution # roundings       : 0
User objective cut value             : 0
Number of cuts generated             : 117
  Number of Gomory cuts              : 108
  Number of CMIR cuts                : 9
Number of branches                   : 4425
Number of relaxations solved         : 4410
Number of interior point iterations: 25
Number of simplex iterations         : 221131
```

The first lines contain a summary of the problem as seen by the optimizer. This is followed by the iteration log. The columns have the following meaning:

- **BRANCHES**: Number of branches generated.
- **RELAXS**: Number of relaxations solved.
- **ACT_NDS**: Number of active branch bound nodes.
- **DEPTH**: Depth of the recently solved node.
- **BEST_INT_OBJ**: The best integer objective value, \bar{z} .
- **BEST_RELAX_OBJ**: The best objective bound, \underline{z} .
- **REL_GAP(%)**: Relative optimality gap, $100\% \cdot \epsilon_{\text{rel}}$
- **TIME**: Time (in seconds) from the start of optimization.

Following that a summary of the optimization process is printed.

PROBLEM ANALYZER

The problem analyzer prints a detailed survey of the

- linear constraints and objective
- quadratic constraints
- conic constraints
- variables

of the model.

In the initial stages of model formulation the problem analyzer may be used as a quick way of verifying that the model has been built or imported correctly. In later stages it can help revealing special structures within the model that may be used to tune the optimizer's performance or to identify the causes of numerical difficulties.

The problem analyzer is run from the command line using the *-anapro* argument and produces something similar to the following (this is the problem analyzer's survey of the *aflow30a* problem from the MIPLIB 2003 collection.)

Analyzing the problem

Constraints	Bounds	Variables
upper bd: 421	ranged : all	cont: 421
fixed : 58		bin : 421

Objective, min cx

range: min c : 0.00000	min c >0: 11.0000	max c : 500.000
distrib: c	vars	
0	421	
[11, 100)	150	
[100, 500]	271	

Constraint matrix A has

479 rows (constraints)
842 columns (variables)
2091 (0.518449%) nonzero entries (coefficients)

Row nonzeros, A_i

range: min A_i: 2 (0.23753%)	max A_i: 34 (4.038%)	
distrib: A_i	rows	rows% acc%
2	421	87.89 87.89
[8, 15]	20	4.18 92.07
[16, 31]	30	6.26 98.33
[32, 34]	8	1.67 100.00

```

Column nonzeros, A|j
  range: min A|j: 2 (0.417537%)    max A|j: 3 (0.626305%)
distrib:      A|j      cols      cols%      acc%
              2        435        51.66        51.66
              3        407        48.34        100.00

```

```

A nonzeros, A(ij)
  range: min |A(ij)|: 1.00000    max |A(ij)|: 100.000
distrib:      A(ij)      coeffs
              [1, 10)      1670
              [10, 100]     421

```

```

-----
Constraint bounds, lb <= Ax <= ub
distrib:      |b|      lbs      lbs      lbs      lbs
              0        421
              [1, 10]     58      58

```

```

Variable bounds, lb <= x <= ub
distrib:      |b|      lbs      lbs      lbs      lbs
              0        842
              [1, 10)     421
              [10, 100]    421

```

The survey is divided into six different sections, each described below. To keep the presentation short with focus on key elements. The analyzer generally attempts to display information on issues relevant for the current model only: e.g., if the model does not have any conic constraints (this is the case in the example above) or any integer variables, those parts of the analysis will not appear.

General Characteristics

The first part of the survey consists of a brief summary of the model's linear and quadratic constraints (indexed by i) and variables (indexed by j). The summary is divided into three subsections:

Constraints

- **upper bd** The number of upper bounded constraints, $\sum_{j=0}^{n-1} a_{ij}x_j \leq u_i^c$
- **lower bd** The number of lower bounded constraints, $l_i^c \leq \sum_{j=0}^{n-1} a_{ij}x_j$
- **ranged** The number of ranged constraints, $l_i^c \leq \sum_{j=0}^{n-1} a_{ij}x_j \leq u_i^c$
- **fixed** The number of fixed constraints, $l_i^c = \sum_{j=0}^{n-1} a_{ij}x_j = u_i^c$
- **free** The number of free constraints

Bounds

- **upper bd** The number of upper bounded variables, $x_j \leq u_j^x$
- **lower bd** The number of lower bounded variables, $l_k^x \leq x_j$
- **ranged** The number of ranged variables, $l_k^x \leq x_j \leq u_j^x$
- **fixed** The number of fixed variables, $l_k^x = x_j = u_j^x$
- **free** The number of free variables

Variables

- **cont** The number of continuous variables, $x_j \in \mathbb{R}$
- **bin** The number of binary variables, $x_j \in \{0, 1\}$
- **int** The number of general integer variables, $x_j \in \mathbb{Z}$

Only constraints, bounds and domains actually in the model will be reported on; if all entities in a section turn out to be of the same kind, the number will be replaced by **all** for brevity.

Objective

The second part of the survey focuses on (the linear part of) the objective, summarizing the optimization sense and the coefficients' absolute value range and distribution. The number of 0 (zero) coefficients is singled out (if any such variables are in the problem).

The range is displayed using three terms:

- **min |c|** The minimum absolute value among all coefficients
- **min |c|>0** The minimum absolute value among the nonzero coefficients
- **max |c|** The maximum absolute value among the coefficients

If some of these extrema turn out to be equal, the display is shortened accordingly:

- If **min |c|** is greater than zero, the **min |c|>0** term is obsolete and will not be displayed
- If only one or two different coefficients occur this will be displayed using **all** and an explicit listing of the coefficients

The absolute value distribution is displayed as a table summarizing the numbers by orders of magnitude (with a ratio of 10). Again, the number of variables with a coefficient of 0 (if any) is singled out. Each line of the table is headed by an interval (half-open intervals including their lower bounds), and is followed by the number of variables with their objective coefficient in this interval. Intervals with no elements are skipped.

Linear Constraints

The third part of the survey displays information on the nonzero coefficients of the linear constraint matrix.

Following a brief summary of the matrix dimensions and the number of nonzero coefficients in total, three sections provide further details on how the nonzero coefficients are distributed by row-wise count (**A_i**), by column-wise count (**A_j**), and by absolute value (**|A(ij)|**). Each section is headed by a brief display of the distribution's range (**min** and **max**), and for the row/column-wise counts the corresponding densities are displayed too (in parentheses).

The distribution tables single out three particularly interesting counts: zero, one, and two nonzeros per row/column; the remaining row/column nonzeros are displayed by orders of magnitude (ratio 2). For each interval the relative and accumulated relative counts are also displayed.

Note that constraints may have both linear and quadratic terms, but the empty rows and columns reported in this part of the survey relate to the linear terms only. If empty rows and/or columns are found in the linear constraint matrix, the problem is analyzed further in order to determine if the corresponding constraints have any quadratic terms or the corresponding variables are used in conic or quadratic constraints.

The distribution of the absolute values, **|A(ij)|**, is displayed just as for the objective coefficients described above.

Constraint and Variable Bounds

The fourth part of the survey displays distributions for the absolute values of the finite lower and upper bounds for both constraints and variables. The number of bounds at 0 is singled out and, otherwise, displayed by orders of magnitude (with a ratio of 10).

Quadratic Constraints

The fifth part of the survey displays distributions for the nonzero elements in the gradient of the quadratic constraints, i.e. the nonzero row counts for the column vectors Qx . The table is similar to the tables for the linear constraints' nonzero row and column counts described in the survey's third part.

Quadratic constraints may also have a linear part, but that will be included in the linear constraints survey; this means that if a problem has one or more pure quadratic constraints, part three of the survey will report the number of linear constraint rows with 0 (zero) nonzeros. Likewise, variables that appear in quadratic terms only will be reported as empty columns (0 nonzeros) in the linear constraint report.

Conic Constraints

The last part of the survey summarizes the model's conic constraints. For each of the two types of cones, quadratic and rotated quadratic, the total number of cones are reported, and the distribution of the cones' dimensions are displayed using intervals. Cones dimensions of 2, 3, and 4 are singled out.

ANALYZING INFEASIBLE PROBLEMS

When developing and implementing a new optimization model, the first attempts will often be either infeasible, due to specification of inconsistent constraints, or unbounded, if important constraints have been left out.

In this section we will

- go over an example demonstrating how to locate infeasible constraints using the **MOSEK** infeasibility report tool,
- discuss in more general terms which properties may cause infeasibilities, and
- present the more formal theory of infeasible and unbounded problems.

11.1 Example: Primal Infeasibility

A problem is said to be *primal infeasible* if no solution exists that satisfies all the constraints of the problem.

As an example of a primal infeasible problem consider the problem of minimizing the cost of transportation between a number of production plants and stores: Each plant produces a fixed number of goods, and each store has a fixed demand that must be met. Supply, demand and cost of transportation per unit are given in Fig. 11.1.

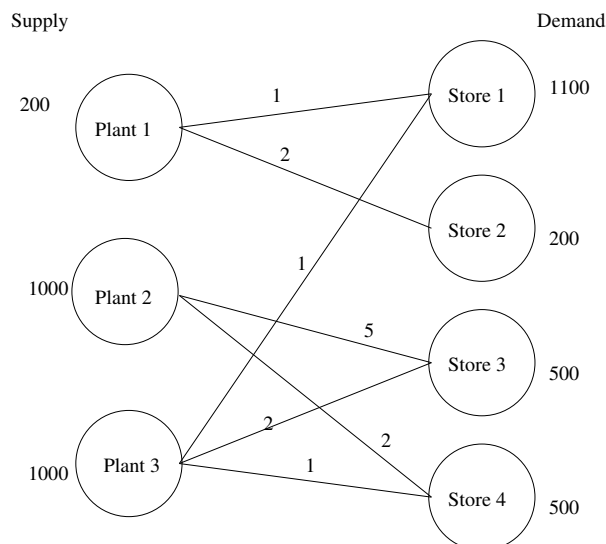


Fig. 11.1: Supply, demand and cost of transportation.

The problem represented in Fig. 11.1 is infeasible, since the total demand

$$2300 = 1100 + 200 + 500 + 500$$

exceeds the total supply

$$2200 = 200 + 1000 + 1000$$

If we denote the number of transported goods from plant i to store j by x_{ij} , the problem can be formulated as the LP:

$$\begin{array}{llllllllll}
 \text{minimize} & x_{11} & + & 2x_{12} & + & 5x_{23} & + & 2x_{24} & + & x_{31} & + & 2x_{33} & + & x_{34} \\
 \text{subject to} & x_{11} & + & x_{12} & & & & & & & & & & \leq 200, \\
 & & & & & x_{23} & + & x_{24} & & & & & & \leq 1000, \\
 & & & & & & & & x_{31} & + & x_{33} & + & x_{34} & \leq 1000, \\
 & x_{11} & & & & & & & + & x_{31} & & & & = 1100, \\
 & & x_{12} & & & & & & & & & & & = 200, \\
 & & & & x_{23} & + & & & & & x_{33} & & & = 500, \\
 & & & & & & x_{24} & + & & & & x_{34} & = 500, \\
 & x_{ij} & \geq 0.
 \end{array}
 \tag{11.1}$$

Solving problem (11.1) using **MOSEK** will result in a solution, a solution status and a problem status. Among the log output from the execution of **MOSEK** on the above problem are the lines:

```

Basic solution
Problem status : PRIMAL_INFEASIBLE
Solution status : PRIMAL_INFEASIBLE_CER

```

The first line indicates that the problem status is primal infeasible. The second line says that a *certificate of the infeasibility* was found. The certificate is returned in place of the solution to the problem.

11.2 Locating the cause of Primal Infeasibility

Usually a primal infeasible problem status is caused by a mistake in formulating the problem and therefore the question arises: *What is the cause of the infeasible status?* When trying to answer this question, it is often advantageous to follow these steps:

- Remove the objective function. This does not change the infeasibility status but simplifies the problem, eliminating any possibility of issues related to the objective function.
- Consider whether your problem has some necessary conditions for feasibility and examine if these are satisfied, e.g. total supply should be greater than or equal to total demand.
- Verify that coefficients and bounds are reasonably sized in your problem.

If the problem is still primal infeasible, some of the constraints must be relaxed or removed completely. The **MOSEK** infeasibility report (Sec. 11.4) may assist you in finding the constraints causing the infeasibility.

Possible ways of relaxing your problem include:

- Increasing (decreasing) upper (lower) bounds on variables and constraints.
- Removing suspected constraints from the problem.

Returning to the transportation example, we discover that removing the fifth constraint

$$x_{12} = 200$$

makes the problem feasible.

11.3 Locating the Cause of Dual Infeasibility

A problem may also be *dual infeasible*. In this case the primal problem is often unbounded, meaning that feasible solutions exist such that the objective tends towards infinity. An example of a dual infeasible and primal unbounded problem is:

$$\begin{array}{ll}\text{minimize} & x_1 \\ \text{subject to} & x_1 \leq 5.\end{array}$$

To resolve a dual infeasibility the primal problem must be made more restricted by

- Adding upper or lower bounds on variables or constraints.
- Removing variables.
- Changing the objective.

11.3.1 A cautionary note

The problem

$$\begin{array}{ll}\text{minimize} & 0 \\ \text{subject to} & 0 \leq x_1, \\ & x_j \leq x_{j+1}, \quad j = 1, \dots, n-1, \\ & x_n \leq -1\end{array}$$

is clearly infeasible. Moreover, if any one of the constraints is dropped, then the problem becomes feasible.

This illustrates the worst case scenario where all, or at least a significant portion of the constraints are involved in causing infeasibility. Hence, it may not always be easy or possible to pinpoint a few constraints responsible for infeasibility.

11.4 The Infeasibility Report

MOSEK includes functionality for diagnosing the cause of a primal or a dual infeasibility. It can be turned on by setting the `MSK_IPAR_INFEAS_REPORT_AUTO` to `MSK_ON`. This causes **MOSEK** to print a report on variables and constraints involved in the infeasibility.

The `MSK_IPAR_INFEAS_REPORT_LEVEL` parameter controls the amount of information presented in the infeasibility report. The default value is 1.

11.4.1 Example: Primal Infeasibility

We will keep working with the problem (11.1) written in LP format:

Listing 11.1: The code for problem (11.1).

```
\
\ An example of an infeasible linear problem.
\
minimize
  obj: + 1 x11 + 2 x12
        + 5 x23 + 2 x24
        + 1 x31 + 2 x33 + 1 x34
st
  s0: + x11 + x12          <= 200
  s1: + x23 + x24          <= 1000
  s2: + x31 + x33 + x34 <= 1000
```

```

d1: + x11 + x31      = 1100
d2: + x12            = 200
d3: + x23 + x33      = 500
d4: + x24 + x34      = 500
bounds
end

```

Using the command line (please remember it accepts options following the C API format)

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON infeas.lp
```

MOSEK produces the following infeasibility report:

MOSEK PRIMAL INFEASIBILITY REPORT.

Problem status: The problem is primal infeasible

The following constraints are involved in the primal infeasibility.

Index	Name	Lower bound	Upper bound	Dual lower	Dual upper
0	s0	NONE	2.000000e+002	0.000000e+000	1.000000e+000
2	s2	NONE	1.000000e+003	0.000000e+000	1.000000e+000
3	d1	1.100000e+003	1.100000e+003	1.000000e+000	0.000000e+000
4	d2	2.000000e+002	2.000000e+002	1.000000e+000	0.000000e+000

The following bound constraints are involved in the infeasibility.

Index	Name	Lower bound	Upper bound	Dual lower	Dual upper
8	x33	0.000000e+000	NONE	1.000000e+000	0.000000e+000
10	x34	0.000000e+000	NONE	1.000000e+000	0.000000e+000

The infeasibility report is divided into two sections corresponding to constraints and variables. It is a selection of those lines from the problem solution (in this case the file `infeas.sol`), which are important in understanding primal infeasibility. In this case the constraints `s0`, `s2`, `d1`, `d2` and variables `x33`, `x34` are of importance.

The columns `Dual lower` and `Dual upper` contain the values of dual variables s_l^c , s_u^c , s_l^x and s_u^x in the primal infeasibility certificate (see [Sec. 7.1.2](#)). Only the non-zero ones, which contribute to the optimization objective and thus are important for infeasibility, are shown.

It is also possible to obtain the infeasible subproblem. The command line

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON infeas.lp -info rinfeas.lp
```

produces the files `rinfeas.bas.inf.lp`. In this case the content of the file `rinfeas.bas.inf.lp` is

```

minimize
obj:  + 0 x11 + 0 x12 + 0 x13 + 0 x21 + 0 x22 + 0 x23
      + 0 x31 + 0 x32 + 0 x33 + 0 x24 + 0 x34
subject to
s0:  + x11 + x12 <= 2e+02
s2:  + x31 + x33 + x34 <= 1e+03
d1:  + x11 + x31 = 1.1e+03
d2:  + x12 = 2e+02
bounds
x11 free
x12 free
x13 free
x21 free
x22 free
x23 free
x31 free

```

```
x32 free
0 <= x33 <= +infinity
x24 free
0 <= x34 <= +infinity
end
```

which is an optimization problem. This problem is identical to (11.1), except that the objective and some of the constraints and bounds have been removed. Executing the command

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON rinfeas.bas.inf.lp
```

demonstrates that the reduced problem is **primal infeasible**. Since the reduced problem is usually smaller than original problem, it should be easier to locate the cause of infeasibility in this rather than in the original (11.1).

11.4.2 Example: Dual Infeasibility

The following problem is dual to (11.1) and therefore it is dual infeasible.

Listing 11.2: The dual of problem (11.1).

```
maximize + 200 y1 + 1000 y2 + 1000 y3 + 1100 y4 + 200 y5 + 500 y6 + 500 y7
subject to
  x11: y1+y4 < 1
  x12: y1+y5 < 2
  x23: y2+y6 < 5
  x24: y2+y7 < 2
  x31: y3+y4 < 1
  x33: y3+y6 < 2
  x34: y3+y7 < 1
bounds
  -inf <= y1 < 0
  -inf <= y2 < 0
  -inf <= y3 < 0
  y4 free
  y5 free
  y6 free
  y7 free
end
```

This can be verified by proving that

$$(y_1, \dots, y_7) = (-1, 0, -1, 1, 1, 0, 0)$$

is a certificate of dual infeasibility (see Sec. 7.1.2) as we can see from this report:

MOSEK DUAL INFEASIBILITY REPORT.

Problem status: The problem is dual infeasible

The following constraints are involved in the infeasibility.

Index	Name	Activity	Objective	Lower bound	Upper bound
5	x33	-1.000000e+00		NONE	2.000000e+00
6	x34	-1.000000e+00		NONE	1.000000e+00

The following variables are involved in the infeasibility.

Index	Name	Activity	Objective	Lower bound	Upper bound
0	y1	-1.000000e+00	2.000000e+02	NONE	0.000000e+00
2	y3	-1.000000e+00	1.000000e+03	NONE	0.000000e+00

3	y4	1.000000e+00	1.100000e+03	NONE	NONE
4	y5	1.000000e+00	2.000000e+02	NONE	NONE
Interior-point solution summary					
Problem status : DUAL_INFEASIBLE					
Solution status : DUAL_INFEASIBLE_CER					
Primal. obj: 1.0000000000e+02 nrm: 1e+00 Viol. con: 0e+00 var: 0e+00					

Let y^* denote the reported primal solution. **MOSEK** states

- that the problem is *dual infeasible*,
- that the reported solution is a certificate of dual infeasibility, and
- that the infeasibility measure for y^* is approximately zero.

Since the original objective was maximization, we have that $c^T y^* > 0$. See [Sec. 7.1.2](#) for how to interpret the parameter values in the infeasibility report for a linear program. We see that the variables y1, y3, y4, y5 and the constraints x33 and x34 contribute to infeasibility with non-zero values in the **Activity** column.

One possible strategy to *fix* the infeasibility is to modify the problem so that the certificate of infeasibility becomes invalid. In this case we could do one the following things:

- Add a lower bound on y3. This will directly invalidate the certificate of dual infeasibility.
- Increase the object coefficient of y3. Changing the coefficients sufficiently will invalidate the inequality $c^T y^* > 0$ and thus the certificate.
- Add lower bounds on x11 or x31. This will directly invalidate the certificate of infeasibility.

Please note that modifying the problem to invalidate the reported certificate does *not* imply that the problem becomes dual feasible — the reason for infeasibility may simply *move*, resulting a problem that is still infeasible, but for a different reason.

More often, the reported certificate can be used to give a hint about errors or inconsistencies in the model that produced the problem.

11.5 Theory Concerning Infeasible Problems

This section discusses the theory of infeasibility certificates and how **MOSEK** uses a certificate to produce an infeasibility report. In general, **MOSEK** solves the problem

$$\begin{array}{ll} \text{minimize} & c^T x + c^f \\ \text{subject to} & \begin{array}{lll} l^c & \leq & Ax & \leq & u^c, \\ l^x & \leq & x & \leq & u^x \end{array} \end{array} \quad (11.2)$$

where the corresponding dual problem is

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c \\ & + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & \begin{array}{ll} A^T y + s_l^x - s_u^x & = c, \\ -y + s_l^c - s_u^c & = 0, \\ s_l^c, s_u^c, s_l^x, s_u^x & \leq 0. \end{array} \end{array} \quad (11.3)$$

We use the convention that for any bound that is not finite, the corresponding dual variable is fixed at zero (and thus will have no influence on the dual problem). For example

$$l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0$$

11.6 The Certificate of Primal Infeasibility

A certificate of primal infeasibility is *any* solution to the homogenized dual problem

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c \\ & && + (l^x)^T s_l^x - (u^x)^T s_u^x \\ & \text{subject to} && A^T y + s_l^x - s_u^x = 0, \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \leq 0. \end{aligned}$$

with a positive objective value. That is, $(s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*})$ is a certificate of primal infeasibility if

$$(l^c)^T s_l^{c*} - (u^c)^T s_u^{c*} + (l^x)^T s_l^{x*} - (u^x)^T s_u^{x*} > 0$$

and

$$\begin{aligned} A^T y + s_l^{x*} - s_u^{x*} &= 0, \\ -y + s_l^{c*} - s_u^{c*} &= 0, \\ s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*} &\leq 0. \end{aligned}$$

The well-known *Farkas Lemma* tells us that (11.2) is infeasible if and only if a certificate of primal infeasibility exists.

Let $(s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*})$ be a certificate of primal infeasibility then

$$(s_l^{c*})_i > 0 ((s_u^{c*})_i > 0)$$

implies that the lower (upper) bound on the i th constraint is important for the infeasibility. Furthermore,

$$(s_l^{x*})_j > 0 ((s_u^{x*})_j > 0)$$

implies that the lower (upper) bound on the j th variable is important for the infeasibility.

11.7 The certificate of dual infeasibility

A certificate of dual infeasibility is *any* solution to the problem

$$\begin{aligned} & \text{minimize} && c^T x \\ & \text{subject to} && \bar{l}^c \leq Ax \leq \bar{u}^c, \\ & && \bar{l}^x \leq x \leq \bar{u}^x \end{aligned}$$

with negative objective value, where we use the definitions

$$\bar{l}_i^c := \begin{cases} 0, & l_i^c > -\infty, \\ -\infty, & \text{otherwise,} \end{cases}, \quad \bar{u}_i^c := \begin{cases} 0, & u_i^c < \infty, \\ \infty, & \text{otherwise,} \end{cases}$$

and

$$\bar{l}_i^x := \begin{cases} 0, & l_i^x > -\infty, \\ -\infty, & \text{otherwise,} \end{cases} \quad \text{and} \quad \bar{u}_i^x := \begin{cases} 0, & u_i^x < \infty, \\ \infty, & \text{otherwise.} \end{cases}$$

Stated differently, a certificate of dual infeasibility is any x^* such that

$$\begin{aligned} c^T x^* &< 0, \\ \bar{l}^c &\leq Ax^* \leq \bar{u}^c, \\ \bar{l}^x &\leq x^* \leq \bar{u}^x \end{aligned} \tag{11.4}$$

The well-known Farkas Lemma tells us that (11.3) is infeasible if and only if a certificate of dual infeasibility exists.

Note that if x^* is a certificate of dual infeasibility then for any j such that

$$x_j^* \leq 0,$$

variable j is involved in the dual infeasibility.

Given the assumption that all weights are 1 then the command

```
mosek -primalrepair -d MSK_IPAR_LOG_FEAS_REPAIR 3 feasrepair.lp
```

will form the repaired problem and solve it. The parameter `MSK_IPAR_LOG_FEAS_REPAIR` controls the amount of log output from the repair. A value of 2 causes the optimal repair to be printed out.

The output from running the above command is:

```
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com

Open file 'feasrepair.lp'

Read summary
Type           : LO (linear optimization problem)
Objective sense : min
Constraints     : 4
Scalar variables : 2
Matrix variables : 0
Time           : 0.0

Computer
Platform       : Windows/64-X86
Cores          : 4

Problem
Name           :
Objective sense : min
Type           : LO (linear optimization problem)
Constraints     : 4
Cones          : 0
Scalar variables : 2
Matrix variables : 0
Integer variables : 0

Primal feasibility repair started.
Optimizer started.
Interior-point optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Total number of eliminations : 2
Eliminator terminated.
Eliminator - tries          : 1          time           : 0.00
Eliminator - elim's        : 2
Lin. dep. - tries          : 1          time           : 0.00
Lin. dep. - number         : 0
Presolve terminated. Time: 0.00
Optimizer - threads         : 1
Optimizer - solved problem  : the primal
Optimizer - Constraints     : 2
Optimizer - Cones          : 0
Optimizer - Scalar variables : 6          conic           : 0
Optimizer - Semi-definite variables: 0      scalarized        : 0
Factor - setup time        : 0.00         dense det. time   : 0.00
Factor - ML order time     : 0.00         GP order time     : 0.00
Factor - nonzeros before factor : 3       after factor      : 3
Factor - dense dim.       : 0            flops             : 5.40e+001
ITE PFEAS   DFEAS   GFEAS   PRSTATUS   POBJ          DOBJ          MU          TIME
0  2.7e+001  1.0e+000  4.8e+000  1.00e+000  4.195228609e+000  0.000000000e+000  1.0e+000  0.00
1  2.4e+001  8.6e-001  1.5e+000  0.00e+000  1.227497414e+001  1.504971820e+001  2.6e+000  0.00
2  2.6e+000  9.7e-002  1.7e-001  -6.19e-001  4.363064729e+001  4.648523094e+001  3.0e-001  0.00
3  4.7e-001  1.7e-002  3.1e-002  1.24e+000  4.256803136e+001  4.298540657e+001  5.2e-002  0.00
4  8.7e-004  3.2e-005  5.7e-005  1.08e+000  4.249989892e+001  4.250078747e+001  9.7e-005  0.00
```

```

5   8.7e-008 3.2e-009 5.7e-009 1.00e+000 4.249999999e+001 4.250000000e+001 9.7e-009 0.00
6   8.7e-012 3.2e-013 5.7e-013 1.00e+000 4.250000000e+001 4.250000000e+001 9.7e-013 0.00
Basis identification started.
Primal basis identification phase started.
ITER      TIME
0          0.00
Primal basis identification phase terminated. Time: 0.00
Dual basis identification phase started.
ITER      TIME
0          0.00
Dual basis identification phase terminated. Time: 0.00
Basis identification terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.00.

Optimizer terminated. Time: 0.03
Basic solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: 4.250000000e+001  Viol.  con: 1e-013  var: 0e+000
Dual.    obj: 4.250000000e+001  Viol.  con: 0e+000  var: 5e-013
Optimal objective value of the penalty problem: 4.250000000e+001

Repairing bounds.
Increasing the upper bound -2.25e+001 on constraint 'c4' (3) with 1.35e+002.
Decreasing the lower bound 6.50e+002 on variable 'x2' (4) with 2.00e+001.
Primal feasibility repair terminated.
Optimizer started.
Interior-point optimizer started.
Presolve started.
Presolve terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.00.

Optimizer terminated. Time: 0.00

Interior-point solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: -5.670000000e+003  Viol.  con: 0e+000  var: 0e+000
Dual.    obj: -5.670000000e+003  Viol.  con: 0e+000  var: 0e+000

Basic solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: -5.670000000e+003  Viol.  con: 0e+000  var: 0e+000
Dual.    obj: -5.670000000e+003  Viol.  con: 0e+000  var: 0e+000

Optimizer summary
Optimizer          -                      time: 0.00
Interior-point    - iterations : 0          time: 0.00
Basis identification -                  time: 0.00
Primal           - iterations : 0          time: 0.00
Dual             - iterations : 0          time: 0.00
Clean primal     - iterations : 0          time: 0.00
Clean dual       - iterations : 0          time: 0.00
Clean primal-dual - iterations : 0          time: 0.00
Simplex          -                      time: 0.00
Primal simplex   - iterations : 0          time: 0.00
Dual simplex     - iterations : 0          time: 0.00
Primal-dual simplex - iterations : 0          time: 0.00
Mixed integer    - relaxations: 0          time: 0.00

```

reports the optimal repair. In this case it is to increase the upper bound on constraint c4 by 1.35e2 and

decrease the lower bound on variable x_2 by 20.

SENSITIVITY ANALYSIS

Given an optimization problem it is often useful to obtain information about how the optimal objective value changes when the problem parameters are perturbed. E.g, assume that a bound represents the capacity of a machine. Now, it may be possible to expand the capacity for a certain cost and hence it is worthwhile knowing what the value of additional capacity is. This is precisely the type of questions the sensitivity analysis deals with.

Analyzing how the optimal objective value changes when the problem data is changed is called *sensitivity analysis*.

References

The book [Chv83] discusses the classical sensitivity analysis in Chapter 10 whereas the book [RTV97] presents a modern introduction to sensitivity analysis. Finally, it is recommended to read the short paper [Wal00] to avoid some of the pitfalls associated with sensitivity analysis.

Warning: Currently, sensitivity analysis is only available for continuous linear optimization problems. Moreover, **MOSEK** can only deal with perturbations of bounds and objective function coefficients.

12.1 Sensitivity Analysis for Linear Problems

12.1.1 The Optimal Objective Value Function

Assume that we are given the problem

$$\begin{aligned} z(l^c, u^c, l^x, u^x, c) = & \text{minimize} && c^T x \\ & \text{subject to} && l^c \leq Ax \leq u^c, \\ & && l^x \leq x \leq u^x, \end{aligned} \quad (12.1)$$

and we want to know how the optimal objective value changes as l_i^c is perturbed. To answer this question we define the perturbed problem for l_i^c as follows

$$\begin{aligned} f_{l_i^c}(\beta) = & \text{minimize} && c^T x \\ & \text{subject to} && l^c + \beta e_i \leq Ax \leq u^c, \\ & && l^x \leq x \leq u^x, \end{aligned}$$

where e_i is the i -th column of the identity matrix. The function

$$f_{l_i^c}(\beta) \quad (12.2)$$

shows the optimal objective value as a function of β . Please note that a change in β corresponds to a perturbation in l_i^c and hence (12.2) shows the optimal objective value as a function of varying l_i^c with the other bounds fixed.

It is possible to prove that the function (12.2) is a piecewise linear and convex function, i.e. its graph may look like in Fig. 12.1 and Fig. 12.2.

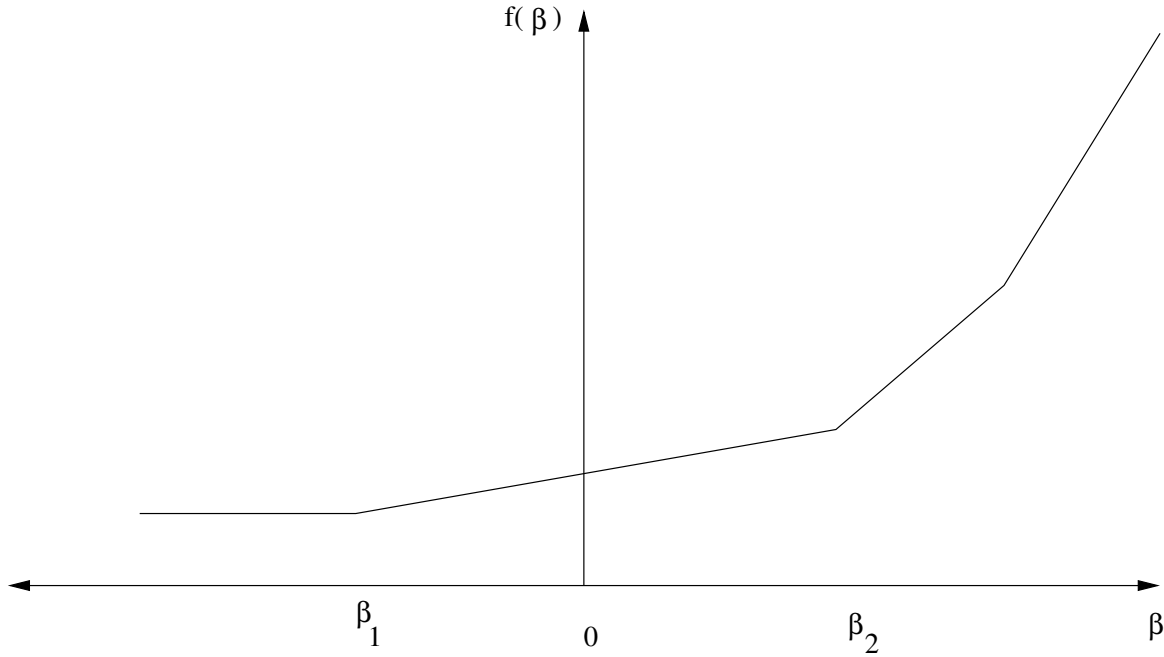


Fig. 12.1: $\beta = 0$ is in the interior of linearity interval.

Clearly, if the function $f_{l_i^c}(\beta)$ does not change much when β is changed, then we can conclude that the optimal objective value is insensitive to changes in l_i^c . Therefore, we are interested in the rate of change in $f_{l_i^c}(\beta)$ for small changes in β — specifically the gradient

$$f'_{l_i^c}(0),$$

which is called the *shadow price* related to l_i^c . The shadow price specifies how the objective value changes for small changes of β around zero. Moreover, we are interested in the *linearity interval*

$$\beta \in [\beta_1, \beta_2]$$

for which

$$f'_{l_i^c}(\beta) = f'_{l_i^c}(0).$$

Since $f_{l_i^c}$ is not a smooth function $f'_{l_i^c}$ may not be defined at 0, as illustrated in Fig. 12.2. In this case we can define a left and a right shadow price and a left and a right linearity interval.

The function $f_{l_i^c}$ considered only changes in l_i^c . We can define similar functions for the remaining parameters of the z defined in (12.1) as well:

$$\begin{aligned} f_{l_i^c}(\beta) &= z(l^c + \beta e_i, u^c, l^x, u^x, c), & i = 1, \dots, m, \\ f_{u_i^c}(\beta) &= z(l^c, u^c + \beta e_i, l^x, u^x, c), & i = 1, \dots, m, \\ f_{l_j^x}(\beta) &= z(l^c, u^c, l^x + \beta e_j, u^x, c), & j = 1, \dots, n, \\ f_{u_j^x}(\beta) &= z(l^c, u^c, l^x, u^x + \beta e_j, c), & j = 1, \dots, n, \\ f_{c_j}(\beta) &= z(l^c, u^c, l^x, u^x, c + \beta e_j), & j = 1, \dots, n. \end{aligned}$$

Given these definitions it should be clear how linearity intervals and shadow prices are defined for the parameters u_i^c etc.

Equality Constraints

In **MOSEK** a constraint can be specified as either an equality constraint or a ranged constraint. If some constraint e_i^c is an equality constraint, we define the optimal value function for this constraint as

$$f_{e_i^c}(\beta) = z(l^c + \beta e_i, u^c + \beta e_i, l^x, u^x, c)$$

Fig. 12.2: $\beta = 0$ is a breakpoint.

Thus for an equality constraint the upper and the lower bounds (which are equal) are perturbed simultaneously. Therefore, **MOSEK** will handle sensitivity analysis differently for a ranged constraint with $l_i^c = u_i^c$ and for an equality constraint.

12.1.2 The Basis Type Sensitivity Analysis

The classical sensitivity analysis discussed in most textbooks about linear optimization, e.g. [Chv83], is based on an optimal basic solution or, equivalently, on an optimal basis. This method may produce misleading results [RTV97] but is **computationally cheap**. Therefore, and for historical reasons, this method is available in **MOSEK**.

We will now briefly discuss the basis type sensitivity analysis. Given an optimal basic solution which provides a partition of variables into basic and non-basic variables, the basis type sensitivity analysis computes the linearity interval $[\beta_1, \beta_2]$ so that the basis remains optimal for the perturbed problem. A shadow price associated with the linearity interval is also computed. However, it is well-known that an optimal basic solution may not be unique and therefore the result depends on the optimal basic solution employed in the sensitivity analysis. This implies that the computed interval is only a subset of the largest interval for which the shadow price is constant. Furthermore, the optimal objective value function might have a breakpoint for $\beta = 0$. In this case the basis type sensitivity method will only provide a subset of either the left or the right linearity interval.

In summary, the basis type sensitivity analysis is computationally cheap but does not provide complete information. Hence, the results of the basis type sensitivity analysis should be used with care.

12.1.3 The Optimal Partition Type Sensitivity Analysis

Another method for computing the complete linearity interval is called the *optimal partition type sensitivity analysis*. The main drawback of the optimal partition type sensitivity analysis is that it is computationally expensive compared to the basis type analysis. This type of sensitivity analysis is currently provided as an experimental feature in **MOSEK**.

Given the optimal primal and dual solutions to (12.1), i.e. x^* and $((s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$ the optimal

objective value is given by

$$z^* := c^T x^*.$$

The left and right shadow prices σ_1 and σ_2 for l_i^c are given by this pair of optimization problems:

$$\begin{aligned} \sigma_1 = & \text{minimize} && e_i^T s_l^c \\ & \text{subject to} && A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c, \\ & && (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) = z^*, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0 \end{aligned}$$

and

$$\begin{aligned} \sigma_2 = & \text{maximize} && e_i^T s_l^c \\ & \text{subject to} && A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c, \\ & && (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) = z^*, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{aligned}$$

These two optimization problems make it easy to interpret the shadow price. Indeed, if $((s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$ is an arbitrary optimal solution then

$$(s_l^c)_i^* \in [\sigma_1, \sigma_2].$$

Next, the linearity interval $[\beta_1, \beta_2]$ for l_i^c is computed by solving the two optimization problems

$$\begin{aligned} \beta_1 = & \text{minimize} && \beta \\ & \text{subject to} && l^c + \beta e_i \leq Ax \leq u^c, \\ & && c^T x - \sigma_1 \beta = z^*, \\ & && l^x \leq x \leq u^x, \end{aligned}$$

and

$$\begin{aligned} \beta_2 = & \text{maximize} && \beta \\ & \text{subject to} && l^c + \beta e_i \leq Ax \leq u^c, \\ & && c^T x - \sigma_2 \beta = z^*, \\ & && l^x \leq x \leq u^x. \end{aligned}$$

The linearity intervals and shadow prices for u_i^c , l_j^x , and u_j^x are computed similarly to l_i^c .

The left and right shadow prices for c_j denoted σ_1 and σ_2 respectively are computed as follows:

$$\begin{aligned} \sigma_1 = & \text{minimize} && e_j^T x \\ & \text{subject to} && l^c + \beta e_i \leq Ax \leq u^c, \\ & && c^T x = z^*, \\ & && l^x \leq x \leq u^x, \end{aligned}$$

and

$$\begin{aligned} \sigma_2 = & \text{maximize} && e_j^T x \\ & \text{subject to} && l^c + \beta e_i \leq Ax \leq u^c, \\ & && c^T x = z^*, \\ & && l^x \leq x \leq u^x. \end{aligned}$$

Once again the above two optimization problems make it easy to interpret the shadow prices. Indeed, if x^* is an arbitrary primal optimal solution, then

$$x_j^* \in [\sigma_1, \sigma_2].$$

The linearity interval $[\beta_1, \beta_2]$ for a c_j is computed as follows:

$$\begin{aligned} \beta_1 = & \text{minimize} && \beta \\ & \text{subject to} && A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c + \beta e_j, \\ & && (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) - \sigma_1 \beta \leq z^*, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0 \end{aligned}$$

and

$$\begin{aligned} \beta_2 = & \text{maximize} && \beta \\ & \text{subject to} && A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c + \beta e_j, \\ & && (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) - \sigma_2 \beta \leq z^*, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{aligned}$$

12.1.4 Example: Sensitivity Analysis

As an example we will use the following transportation problem. Consider the problem of minimizing the transportation cost between a number of production plants and stores. Each plant supplies a number of goods and each store has a given demand that must be met. Supply, demand and cost of transportation per unit are shown in Fig. 12.3.

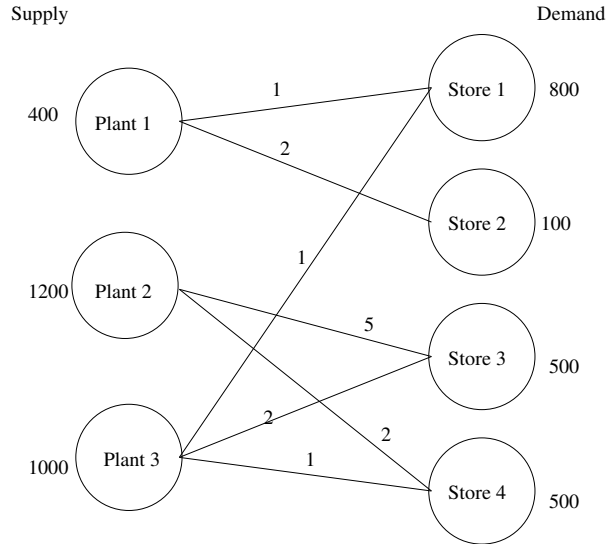


Fig. 12.3: Supply, demand and cost of transportation.

If we denote the number of transported goods from location i to location j by x_{ij} , problem can be formulated as the linear optimization problem of minimizing

$$1x_{11} + 2x_{12} + 5x_{23} + 2x_{24} + 1x_{31} + 2x_{33} + 1x_{34}$$

subject to

$$\begin{array}{rcl} x_{11} + x_{12} & & \leq 400, \\ & x_{23} + x_{24} & \leq 1200, \\ & & x_{31} + x_{33} + x_{34} \leq 1000, \\ x_{11} & & + x_{31} = 800, \\ & x_{12} & = 100, \\ & & x_{23} + x_{33} = 500, \\ & & x_{24} + x_{34} = 500, \\ x_{11}, x_{12}, x_{23}, x_{24}, x_{31}, x_{33}, x_{34} & \geq 0. \end{array} \quad (12.3)$$

The sensitivity parameters are shown in Table 12.1 and Table 12.2 for the basis type analysis and in Table 12.3 and Table 12.4 for the optimal partition type analysis.

Table 12.1: Ranges and shadow prices related to bounds on constraints and variables: results for the basis type sensitivity analysis.

Con.	β_1	β_2	σ_1	σ_2
1	-300.00	0.00	3.00	3.00
2	-700.00	$+\infty$	0.00	0.00
3	-500.00	0.00	3.00	3.00
4	-0.00	500.00	4.00	4.00
5	-0.00	300.00	5.00	5.00
6	-0.00	700.00	5.00	5.00
7	-500.00	700.00	2.00	2.00
Var.	β_1	β_2	σ_1	σ_2
x_{11}	$-\infty$	300.00	0.00	0.00
x_{12}	$-\infty$	100.00	0.00	0.00
x_{23}	$-\infty$	0.00	0.00	0.00
x_{24}	$-\infty$	500.00	0.00	0.00
x_{31}	$-\infty$	500.00	0.00	0.00
x_{33}	$-\infty$	500.00	0.00	0.00
x_{34}	-0.000000	500.00	2.00	2.00

Table 12.2: Ranges and shadow prices related to bounds on constraints and variables: results for the optimal partition type sensitivity analysis.

Con.	β_1	β_2	σ_1	σ_2
1	-300.00	500.00	3.00	1.00
2	-700.00	$+\infty$	-0.00	-0.00
3	-500.00	500.00	3.00	1.00
4	-500.00	500.00	2.00	4.00
5	-100.00	300.00	3.00	5.00
6	-500.00	700.00	3.00	5.00
7	-500.00	700.00	2.00	2.00
Var.	β_1	β_2	σ_1	σ_2
x_{11}	$-\infty$	300.00	0.00	0.00
x_{12}	$-\infty$	100.00	0.00	0.00
x_{23}	$-\infty$	500.00	0.00	2.00
x_{24}	$-\infty$	500.00	0.00	0.00
x_{31}	$-\infty$	500.00	0.00	0.00
x_{33}	$-\infty$	500.00	0.00	0.00
x_{34}	$-\infty$	500.00	0.00	2.00

Table 12.3: Ranges and shadow prices related to the objective coefficients: results for the basis type sensitivity analysis.

Var.	β_1	β_2	σ_1	σ_2
c_1	$-\infty$	3.00	300.00	300.00
c_2	$-\infty$	∞	100.00	100.00
c_3	-2.00	∞	0.00	0.00
c_4	$-\infty$	2.00	500.00	500.00
c_5	-3.00	∞	500.00	500.00
c_6	$-\infty$	2.00	500.00	500.00
c_7	-2.00	∞	0.00	0.00

Table 12.4: Ranges and shadow prices related to the objective coefficients: results for the optimal partition type sensitivity analysis.

Var.	β_1	β_2	σ_1	σ_2
c_1	$-\infty$	3.00	300.00	300.00
c_2	$-\infty$	∞	100.00	100.00
c_3	-2.00	∞	0.00	0.00
c_4	$-\infty$	2.00	500.00	500.00
c_5	-3.00	∞	500.00	500.00
c_6	$-\infty$	2.00	500.00	500.00
c_7	-2.00	∞	0.00	0.00

Examining the results from the optimal partition type sensitivity analysis we see that for constraint number 1 we have $\sigma_1 = 3$, $\sigma_2 = 1$ and $\beta_1 = -300$, $\beta_2 = 500$. Therefore, we have a left linearity interval of $[-300, 0]$ and a right interval of $[0, 500]$. The corresponding left and right shadow prices are 3 and 1 respectively. This implies that if the upper bound on constraint 1 increases by

$$\beta \in [0, \beta_1] = [0, 500]$$

then the optimal objective value will decrease by the value

$$\sigma_2 \beta = 1\beta.$$

Correspondingly, if the upper bound on constraint 1 is decreased by

$$\beta \in [0, 300]$$

then the optimal objective value will increase by the value

$$\sigma_1 \beta = 3\beta.$$

12.2 Sensitivity Analysis with MOSEK

A sensitivity analysis can be performed with the **MOSEK** command line tool specifying the option `-sen`, e.g.

```
mosek myproblem.mps -sen sensitivity.ssp
```

where `sensitivity.ssp` is a file in the format described in the next section. The `ssp` file describes which parts of the problem the sensitivity analysis should be performed on, see [Sec. 12.2.1](#).

By default results are written to a file named `myproblem.sen`. If necessary, this file name can be changed by setting the `MSK_SPAR_SENSITIVITY_RES_FILE_NAME` parameter. By default a basis type sensitivity analysis is performed. However, the type of sensitivity analysis (basis or optimal partition) can be changed by setting the parameter `MSK_IPAR_SENSITIVITY_TYPE` appropriately. Following values are accepted for this parameter:

- `MSK_SENSITIVITY_TYPE_BASIS`
- `MSK_SENSITIVITY_TYPE_OPTIMAL_PARTITION`

12.2.1 Sensitivity Analysis Specification File

MOSEK employs an MPS-like file format to specify on which model parameters the sensitivity analysis should be performed. As the optimal partition type sensitivity analysis can be computationally expensive it is important to limit the sensitivity analysis.

The format of the sensitivity specification file is shown in [Listing 12.1](#), where capitalized names are keywords, and names in brackets are names of the constraints and variables to be included in the analysis.

Listing 12.1: Sensitivity analysis file specification.

```
BOUNDS CONSTRAINTS
U|L|LU [cname1]
U|L|LU [cname2] - [cname3]
BOUNDS VARIABLES
U|L|LU [vname1]
U|L|LU [vname2] - [vname3]
OBJECTIVE VARIABLES
[vname1]
[vname2] - [vname3]
```

The sensitivity specification file has three sections, i.e.

- **BOUNDS CONSTRAINTS:** Specifies on which bounds on constraints the sensitivity analysis should be performed.
- **BOUNDS VARIABLES:** Specifies on which bounds on variables the sensitivity analysis should be performed.
- **OBJECTIVE VARIABLES:** Specifies on which objective coefficients the sensitivity analysis should be performed.

A line in the body of a section must begin with a whitespace. In the **BOUNDS** sections one of the keys L, U, and LU must appear next. These keys specify whether the sensitivity analysis is performed on the lower bound, on the upper bound, or on both the lower and the upper bound respectively. Next, a single constraint (variable) or range of constraints (variables) is specified.

Recall from [Sec. 12.1.1](#) that equality constraints are handled in a special way. Sensitivity analysis of an equality constraint can be specified with either L, U, or LU, all indicating the same, namely that upper and lower bounds (which are equal) are perturbed simultaneously.

As an example consider

```
BOUNDS CONSTRAINTS
L "cons1"
U "cons2"
LU "cons3" - "cons6"
```


which requests that sensitivity analysis is performed on the lower bound of the constraint named `cons1`, on the upper bound of the constraint named `cons2`, and on both lower and upper bound on the constraints named `cons3` to `cons6`.

It is allowed to use indexes instead of names, for instance

```
BOUNDS CONSTRAINTS
L "cons1"
U 2
LU 3 - 6
```

The character `*` indicates that the line contains a comment and is ignored.

12.2.2 Example: Sensitivity Analysis from Command Line

As an example consider problem (12.3): the sensitivity file shown below (included in the distribution among the examples).

Listing 12.2: Sensitivity file for problem (12.3).

```
* Comment 1

BOUNDS CONSTRAINTS
U "c1"          * Analyze upper bound for constraints named c1
U 2             * Analyze upper bound for constraints with index 2
U 3-5           * Analyze upper bound for constraint with index in interval [3:5]

VARIABLES CONSTRAINTS
L 2-4           * This section specifies which bounds on variables should be analyzed.
L "x11"

OBJECTIVE CONSTRAINTS
"x11"          * This section specifies which objective coefficients should be analysed.
2
```

The command

```
mosek transport.lp -sen sensitivity.ssp -d MSK_IPAR_SENSITIVITY_TYPE sensitivitytype.basis
```

produces the output file as follow

Listing 12.3: Results of sensitivity analysis

```
BOUNDS CONSTRAINTS
INDEX  NAME          BOUND  LEFTRANGE  RIGHTRANGE  LEFTPRICE  └
└─RIGHTPRICE
0      c1            UP      -6.574875e-18  5.000000e+02  1.000000e+00  1.
└─000000e+00
2      c3            UP      -6.574875e-18  5.000000e+02  1.000000e+00  1.
└─000000e+00
3      c4            FIX      -5.000000e+02  6.574875e-18  2.000000e+00  2.
└─000000e+00
4      c5            FIX      -1.000000e+02  6.574875e-18  3.000000e+00  3.
└─000000e+00
5      c6            FIX      -5.000000e+02  6.574875e-18  3.000000e+00  3.
└─000000e+00

BOUNDS VARIABLES
INDEX  NAME          BOUND  LEFTRANGE  RIGHTRANGE  LEFTPRICE  └
└─RIGHTPRICE
2      x23          LO      -6.574875e-18  5.000000e+02  2.000000e+00  2.
└─000000e+00
3      x24          LO      -inf        5.000000e+02  0.000000e+00  0.
└─000000e+00
```

4	x31	L0	-inf	5.000000e+02	0.000000e+00	0.
↪	000000e+00					
0	x11	L0	-inf	3.000000e+02	0.000000e+00	0.
↪	000000e+00					
OBJECTIVE VARIABLES						
INDEX	NAME	LEFTRANGE	RIGHTRANGE	LEFTPRICE		
↪	RIGHTPRICE					
0	x11	-inf	1.000000e+00	3.000000e+02	3.	
↪	000000e+02					
2	x23	-2.000000e+00	+inf	0.000000e+00	0.	
↪	000000e+00					

12.2.3 Controlling Log Output

Setting the parameter *MSK_IPAR_LOG_SENSITIVITY* to 1 or 0 (default) controls whether or not the results from sensitivity calculations are printed to the message stream.

The parameter *MSK_IPAR_LOG_SENSITIVITY_OPT* controls the amount of debug information on internal calculations from the sensitivity analysis.

API REFERENCE

- **Optimizer parameters:**
 - *Double, Integer, String*
 - *Full list*
 - *Browse by topic*
- *Optimizer response codes*
- *Constants*

13.1 Parameters grouped by topic

Analysis

- *MSK_DPAR_ANA_SOL_INFEAS_TOL*
- *MSK_IPAR_ANA_SOL_BASIS*
- *MSK_IPAR_ANA_SOL_PRINT_VIOLATED*
- *MSK_IPAR_LOG_ANA_PRO*

Basis identification

- *MSK_DPAR_SIM_LU_TOL_REL_PIV*
- *MSK_IPAR_BI_CLEAN_OPTIMIZER*
- *MSK_IPAR_BI_IGNORE_MAX_ITER*
- *MSK_IPAR_BI_IGNORE_NUM_ERROR*
- *MSK_IPAR_BI_MAX_ITERATIONS*
- *MSK_IPAR_INTPNT_BASIS*
- *MSK_IPAR_LOG_BI*
- *MSK_IPAR_LOG_BI_FREQ*

Conic interior-point method

- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*

- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*

Data check

- *MSK_DPAR_DATA_SYM_MAT_TOL*
- *MSK_DPAR_DATA_SYM_MAT_TOL_HUGE*
- *MSK_DPAR_DATA_SYM_MAT_TOL_LARGE*
- *MSK_DPAR_DATA_TOL_AIJ*
- *MSK_DPAR_DATA_TOL_AIJ_HUGE*
- *MSK_DPAR_DATA_TOL_AIJ_LARGE*
- *MSK_DPAR_DATA_TOL_BOUND_INF*
- *MSK_DPAR_DATA_TOL_BOUND_WRN*
- *MSK_DPAR_DATA_TOL_C_HUGE*
- *MSK_DPAR_DATA_TOL_CJ_LARGE*
- *MSK_DPAR_DATA_TOL_QIJ*
- *MSK_DPAR_DATA_TOL_X*
- *MSK_DPAR_SEMIDEFINITE_TOL_APPROX*
- *MSK_IPAR_CHECK_CONVEXITY*
- *MSK_IPAR_LOG_CHECK_CONVEXITY*

Data input/output

- *MSK_IPAR_INFEAS_REPORT_AUTO*
- *MSK_IPAR_LOG_FILE*
- *MSK_IPAR_OPF_MAX_TERMS_PER_LINE*
- *MSK_IPAR_OPF_WRITE_HEADER*
- *MSK_IPAR_OPF_WRITE_HINTS*
- *MSK_IPAR_OPF_WRITE_PARAMETERS*
- *MSK_IPAR_OPF_WRITE_PROBLEM*
- *MSK_IPAR_OPF_WRITE_SOL_BAS*
- *MSK_IPAR_OPF_WRITE_SOL_ITG*
- *MSK_IPAR_OPF_WRITE_SOL_ITR*
- *MSK_IPAR_OPF_WRITE_SOLUTIONS*
- *MSK_IPAR_PARAM_READ_CASE_NAME*
- *MSK_IPAR_PARAM_READ_IGN_ERROR*
- *MSK_IPAR_READ_DATA_COMPRESSED*
- *MSK_IPAR_READ_DATA_FORMAT*
- *MSK_IPAR_READ_DEBUG*

- *MSK_IPAR_READ_KEEP_FREE_CON*
- *MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU*
- *MSK_IPAR_READ_LP_QUOTED_NAMES*
- *MSK_IPAR_READ_MPS_FORMAT*
- *MSK_IPAR_READ_MPS_WIDTH*
- *MSK_IPAR_READ_TASK_IGNORE_PARAM*
- *MSK_IPAR_SOL_READ_NAME_WIDTH*
- *MSK_IPAR_SOL_READ_WIDTH*
- *MSK_IPAR_WRITE_BAS_CONSTRAINTS*
- *MSK_IPAR_WRITE_BAS_HEAD*
- *MSK_IPAR_WRITE_BAS_VARIABLES*
- *MSK_IPAR_WRITE_DATA_COMPRESSED*
- *MSK_IPAR_WRITE_DATA_FORMAT*
- *MSK_IPAR_WRITE_DATA_PARAM*
- *MSK_IPAR_WRITE_FREE_CON*
- *MSK_IPAR_WRITE_GENERIC_NAMES*
- *MSK_IPAR_WRITE_GENERIC_NAMES_IO*
- *MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS*
- *MSK_IPAR_WRITE_INT_CONSTRAINTS*
- *MSK_IPAR_WRITE_INT_HEAD*
- *MSK_IPAR_WRITE_INT_VARIABLES*
- *MSK_IPAR_WRITE_LP_FULL_OBJ*
- *MSK_IPAR_WRITE_LP_LINE_WIDTH*
- *MSK_IPAR_WRITE_LP_QUOTED_NAMES*
- *MSK_IPAR_WRITE_LP_STRICT_FORMAT*
- *MSK_IPAR_WRITE_LP_TERMS_PER_LINE*
- *MSK_IPAR_WRITE_MPS_FORMAT*
- *MSK_IPAR_WRITE_MPS_INT*
- *MSK_IPAR_WRITE_PRECISION*
- *MSK_IPAR_WRITE_SOL_BARVARIABLES*
- *MSK_IPAR_WRITE_SOL_CONSTRAINTS*
- *MSK_IPAR_WRITE_SOL_HEAD*
- *MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES*
- *MSK_IPAR_WRITE_SOL_VARIABLES*
- *MSK_IPAR_WRITE_TASK_INC_SOL*
- *MSK_IPAR_WRITE_XML_MODE*
- *MSK_SPAR_BAS_SOL_FILE_NAME*
- *MSK_SPAR_DATA_FILE_NAME*
- *MSK_SPAR_DEBUG_FILE_NAME*

- *MSK_SPAR_INT_SOL_FILE_NAME*
- *MSK_SPAR_ITR_SOL_FILE_NAME*
- *MSK_SPAR_MIO_DEBUG_STRING*
- *MSK_SPAR_PARAM_COMMENT_SIGN*
- *MSK_SPAR_PARAM_READ_FILE_NAME*
- *MSK_SPAR_PARAM_WRITE_FILE_NAME*
- *MSK_SPAR_READ_MPS_BOU_NAME*
- *MSK_SPAR_READ_MPS_OBJ_NAME*
- *MSK_SPAR_READ_MPS_RAN_NAME*
- *MSK_SPAR_READ_MPS_RHS_NAME*
- *MSK_SPAR_SENSITIVITY_FILE_NAME*
- *MSK_SPAR_SENSITIVITY_RES_FILE_NAME*
- *MSK_SPAR_SOL_FILTER_XC_LOW*
- *MSK_SPAR_SOL_FILTER_XC_UPR*
- *MSK_SPAR_SOL_FILTER_XX_LOW*
- *MSK_SPAR_SOL_FILTER_XX_UPR*
- *MSK_SPAR_STAT_FILE_NAME*
- *MSK_SPAR_STAT_KEY*
- *MSK_SPAR_STAT_NAME*
- *MSK_SPAR_WRITE_LP_GEN_VAR_NAME*

Debugging

- *MSK_IPAR_AUTO_SORT_A_BEFORE_OPT*

Dual simplex

- *MSK_IPAR_SIM_DUAL_CRASH*
- *MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION*
- *MSK_IPAR_SIM_DUAL_SELECTION*

Infeasibility report

- *MSK_IPAR_INFEAS_GENERIC_NAMES*
- *MSK_IPAR_INFEAS_REPORT_LEVEL*
- *MSK_IPAR_LOG_INFEAS_ANA*

Interior-point method

- *MSK_DPAR_CHECK_CONVEXITY_REL_TOL*
- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_NL_MERIT_BAL*
- *MSK_DPAR_INTPNT_NL_TOL_DFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_MU_RED*
- *MSK_DPAR_INTPNT_NL_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_NL_TOL_PFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_NL_TOL_REL_STEP*
- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_DFEAS*
- *MSK_DPAR_INTPNT_TOL_DSAFE*
- *MSK_DPAR_INTPNT_TOL_INFEAS*
- *MSK_DPAR_INTPNT_TOL_MU_RED*
- *MSK_DPAR_INTPNT_TOL_PATH*
- *MSK_DPAR_INTPNT_TOL_PFEAS*
- *MSK_DPAR_INTPNT_TOL_PSAFE*
- *MSK_DPAR_INTPNT_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_REL_STEP*
- *MSK_DPAR_INTPNT_TOL_STEP_SIZE*
- *MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL*
- *MSK_IPAR_BI_IGNORE_MAX_ITER*
- *MSK_IPAR_BI_IGNORE_NUM_ERROR*
- *MSK_IPAR_INTPNT_BASIS*
- *MSK_IPAR_INTPNT_DIFF_STEP*
- *MSK_IPAR_INTPNT_HOTSTART*
- *MSK_IPAR_INTPNT_MAX_ITERATIONS*

- *MSK_IPAR_INTPNT_MAX_NUM_COR*
- *MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS*
- *MSK_IPAR_INTPNT_OFF_COL_TRH*
- *MSK_IPAR_INTPNT_ORDER_METHOD*
- *MSK_IPAR_INTPNT_REGULARIZATION_USE*
- *MSK_IPAR_INTPNT_SCALING*
- *MSK_IPAR_INTPNT_SOLVE_FORM*
- *MSK_IPAR_INTPNT_STARTING_POINT*
- *MSK_IPAR_LOG_INTPNT*

License manager

- *MSK_IPAR_CACHE_LICENSE*
- *MSK_IPAR_LICENSE_DEBUG*
- *MSK_IPAR_LICENSE_PAUSE_TIME*
- *MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS*
- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*
- *MSK_IPAR_LICENSE_WAIT*

Logging

- *MSK_IPAR_LOG*
- *MSK_IPAR_LOG_ANA_PRO*
- *MSK_IPAR_LOG_BI*
- *MSK_IPAR_LOG_BI_FREQ*
- *MSK_IPAR_LOG_CUT_SECOND_OPT*
- *MSK_IPAR_LOG_EXPAND*
- *MSK_IPAR_LOG_FEAS_REPAIR*
- *MSK_IPAR_LOG_FILE*
- *MSK_IPAR_LOG_INFEAS_ANA*
- *MSK_IPAR_LOG_INTPNT*
- *MSK_IPAR_LOG_MIO*
- *MSK_IPAR_LOG_MIO_FREQ*
- *MSK_IPAR_LOG_ORDER*
- *MSK_IPAR_LOG_PRESOLVE*
- *MSK_IPAR_LOG_RESPONSE*
- *MSK_IPAR_LOG_SENSITIVITY*
- *MSK_IPAR_LOG_SENSITIVITY_OPT*
- *MSK_IPAR_LOG_SIM*
- *MSK_IPAR_LOG_SIM_FREQ*

- *MSK_IPAR_LOG_STORAGE*

Mixed-integer optimization

- *MSK_DPAR_MIO_DISABLE_TERM_TIME*
- *MSK_DPAR_MIO_MAX_TIME*
- *MSK_DPAR_MIO_NEAR_TOL_ABS_GAP*
- *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*
- *MSK_DPAR_MIO_REL_GAP_CONST*
- *MSK_DPAR_MIO_TOL_ABS_GAP*
- *MSK_DPAR_MIO_TOL_ABS_RELAX_INT*
- *MSK_DPAR_MIO_TOL_FEAS*
- *MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT*
- *MSK_DPAR_MIO_TOL_REL_GAP*
- *MSK_IPAR_LOG_MIO*
- *MSK_IPAR_LOG_MIO_FREQ*
- *MSK_IPAR_MIO_BRANCH_DIR*
- *MSK_IPAR_MIO_CONSTRUCT_SOL*
- *MSK_IPAR_MIO_CUT_CLIQUE*
- *MSK_IPAR_MIO_CUT_CMIR*
- *MSK_IPAR_MIO_CUT_GMI*
- *MSK_IPAR_MIO_CUT_IMPLIED_BOUND*
- *MSK_IPAR_MIO_CUT_KNAPSACK_COVER*
- *MSK_IPAR_MIO_CUT_SELECTION_LEVEL*
- *MSK_IPAR_MIO_HEURISTIC_LEVEL*
- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*
- *MSK_IPAR_MIO_MAX_NUM_RELAXS*
- *MSK_IPAR_MIO_MAX_NUM_SOLUTIONS*
- *MSK_IPAR_MIO_NODE_OPTIMIZER*
- *MSK_IPAR_MIO_NODE_SELECTION*
- *MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE*
- *MSK_IPAR_MIO_PROBING_LEVEL*
- *MSK_IPAR_MIO_RINS_MAX_NODES*
- *MSK_IPAR_MIO_ROOT_OPTIMIZER*
- *MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL*
- *MSK_IPAR_MIO_VB_DETECTION_LEVEL*

Nonlinear convex method

- *MSK_DPAR_INTPNT_NL_MERIT_BAL*
- *MSK_DPAR_INTPNT_NL_TOL_DFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_MU_RED*
- *MSK_DPAR_INTPNT_NL_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_NL_TOL_PFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_NL_TOL_REL_STEP*
- *MSK_DPAR_INTPNT_TOL_INFEAS*
- *MSK_IPAR_CHECK_CONVEXITY*
- *MSK_IPAR_LOG_CHECK_CONVEXITY*

Output information

- *MSK_IPAR_INFEAS_REPORT_LEVEL*
- *MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS*
- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*
- *MSK_IPAR_LOG*
- *MSK_IPAR_LOG_BI*
- *MSK_IPAR_LOG_BI_FREQ*
- *MSK_IPAR_LOG_CUT_SECOND_OPT*
- *MSK_IPAR_LOG_EXPAND*
- *MSK_IPAR_LOG_FEAS_REPAIR*
- *MSK_IPAR_LOG_FILE*
- *MSK_IPAR_LOG_INFEAS_ANA*
- *MSK_IPAR_LOG_INTPNT*
- *MSK_IPAR_LOG_MIO*
- *MSK_IPAR_LOG_MIO_FREQ*
- *MSK_IPAR_LOG_ORDER*
- *MSK_IPAR_LOG_RESPONSE*
- *MSK_IPAR_LOG_SENSITIVITY*
- *MSK_IPAR_LOG_SENSITIVITY_OPT*
- *MSK_IPAR_LOG_SIM*
- *MSK_IPAR_LOG_SIM_FREQ*
- *MSK_IPAR_LOG_SIM_MINOR*
- *MSK_IPAR_LOG_STORAGE*
- *MSK_IPAR_MAX_NUM_WARNINGS*

Overall solver

- *MSK_IPAR_BI_CLEAN_OPTIMIZER*
- *MSK_IPAR_INFEAS_PREFER_PRIMAL*
- *MSK_IPAR_LICENSE_WAIT*
- *MSK_IPAR_MIO_MODE*
- *MSK_IPAR_OPTIMIZER*
- *MSK_IPAR_PRESOLVE_LEVEL*
- *MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS*
- *MSK_IPAR_PRESOLVE_USE*
- *MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER*
- *MSK_IPAR_SENSITIVITY_ALL*
- *MSK_IPAR_SENSITIVITY_OPTIMIZER*
- *MSK_IPAR_SENSITIVITY_TYPE*
- *MSK_IPAR_SOLUTION_CALLBACK*

Overall system

- *MSK_IPAR_AUTO_UPDATE_SOL_INFO*
- *MSK_IPAR_INTPNT_MULTI_THREAD*
- *MSK_IPAR_LICENSE_WAIT*
- *MSK_IPAR_LOG_STORAGE*
- *MSK_IPAR_MIO_MT_USER_CB*
- *MSK_IPAR_MT_SPINCOUNT*
- *MSK_IPAR_NUM_THREADS*
- *MSK_IPAR_REMOVE_UNUSED_SOLUTIONS*
- *MSK_IPAR_TIMING_LEVEL*
- *MSK_SPAR_REMOTE_ACCESS_TOKEN*

Presolve

- *MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP*
- *MSK_DPAR_PRESOLVE_TOL_AIJ*
- *MSK_DPAR_PRESOLVE_TOL_REL_LINDEP*
- *MSK_DPAR_PRESOLVE_TOL_S*
- *MSK_DPAR_PRESOLVE_TOL_X*
- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL*
- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES*
- *MSK_IPAR_PRESOLVE_LEVEL*
- *MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH*
- *MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH*

- *MSK_IPAR_PRESOLVE_LINDEP_USE*
- *MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS*
- *MSK_IPAR_PRESOLVE_USE*

Primal simplex

- *MSK_IPAR_SIM_PRIMAL_CRASH*
- *MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION*
- *MSK_IPAR_SIM_PRIMAL_SELECTION*

Progress callback

- *MSK_IPAR_SOLUTION_CALLBACK*

Simplex optimizer

- *MSK_DPAR_BASIS_REL_TOL_S*
- *MSK_DPAR_BASIS_TOL_S*
- *MSK_DPAR_BASIS_TOL_X*
- *MSK_DPAR_SIM_LU_TOL_REL_PIV*
- *MSK_DPAR_SIMPLEX_ABS_TOL_PIV*
- *MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE*
- *MSK_IPAR_LOG_SIM*
- *MSK_IPAR_LOG_SIM_FREQ*
- *MSK_IPAR_LOG_SIM_MINOR*
- *MSK_IPAR_SENSITIVITY_OPTIMIZER*
- *MSK_IPAR_SIM_BASIS_FACTOR_USE*
- *MSK_IPAR_SIM_DEGEN*
- *MSK_IPAR_SIM_DUAL_PHASEONE_METHOD*
- *MSK_IPAR_SIM_EXPLOIT_DUPVEC*
- *MSK_IPAR_SIM_HOTSTART*
- *MSK_IPAR_SIM_HOTSTART_LU*
- *MSK_IPAR_SIM_MAX_ITERATIONS*
- *MSK_IPAR_SIM_MAX_NUM_SETBACKS*
- *MSK_IPAR_SIM_NON_SINGULAR*
- *MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD*
- *MSK_IPAR_SIM_REFACTOR_FREQ*
- *MSK_IPAR_SIM_REFORMULATION*
- *MSK_IPAR_SIM_SAVE_LU*
- *MSK_IPAR_SIM_SCALING*
- *MSK_IPAR_SIM_SCALING_METHOD*

- *MSK_IPAR_SIM_SOLVE_FORM*
- *MSK_IPAR_SIM_STABILITY_PRIORITY*
- *MSK_IPAR_SIM_SWITCH_OPTIMIZER*

Solution input/output

- *MSK_IPAR_INFEAS_REPORT_AUTO*
- *MSK_IPAR_SOL_FILTER_KEEP_BASIC*
- *MSK_IPAR_SOL_FILTER_KEEP_RANGED*
- *MSK_IPAR_SOL_READ_NAME_WIDTH*
- *MSK_IPAR_SOL_READ_WIDTH*
- *MSK_IPAR_WRITE_BAS_CONSTRAINTS*
- *MSK_IPAR_WRITE_BAS_HEAD*
- *MSK_IPAR_WRITE_BAS_VARIABLES*
- *MSK_IPAR_WRITE_INT_CONSTRAINTS*
- *MSK_IPAR_WRITE_INT_HEAD*
- *MSK_IPAR_WRITE_INT_VARIABLES*
- *MSK_IPAR_WRITE_SOL_BARVARIABLES*
- *MSK_IPAR_WRITE_SOL_CONSTRAINTS*
- *MSK_IPAR_WRITE_SOL_HEAD*
- *MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES*
- *MSK_IPAR_WRITE_SOL_VARIABLES*
- *MSK_SPAR_BAS_SOL_FILE_NAME*
- *MSK_SPAR_INT_SOL_FILE_NAME*
- *MSK_SPAR_ITR_SOL_FILE_NAME*
- *MSK_SPAR_SOL_FILTER_XC_LOW*
- *MSK_SPAR_SOL_FILTER_XC_UPR*
- *MSK_SPAR_SOL_FILTER_XX_LOW*
- *MSK_SPAR_SOL_FILTER_XX_UPR*

Termination criteria

- *MSK_DPAR_BASIS_REL_TOL_S*
- *MSK_DPAR_BASIS_TOL_S*
- *MSK_DPAR_BASIS_TOL_X*
- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*

- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_NL_TOL_DFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_MU_RED*
- *MSK_DPAR_INTPNT_NL_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_NL_TOL_PFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_DFEAS*
- *MSK_DPAR_INTPNT_TOL_INFEAS*
- *MSK_DPAR_INTPNT_TOL_MU_RED*
- *MSK_DPAR_INTPNT_TOL_PFEAS*
- *MSK_DPAR_INTPNT_TOL_REL_GAP*
- *MSK_DPAR_LOWER_OBJ_CUT*
- *MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH*
- *MSK_DPAR_MIO_DISABLE_TERM_TIME*
- *MSK_DPAR_MIO_MAX_TIME*
- *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*
- *MSK_DPAR_MIO_REL_GAP_CONST*
- *MSK_DPAR_MIO_TOL_REL_GAP*
- *MSK_DPAR_OPTIMIZER_MAX_TIME*
- *MSK_DPAR_UPPER_OBJ_CUT*
- *MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH*
- *MSK_IPAR_BI_MAX_ITERATIONS*
- *MSK_IPAR_INTPNT_MAX_ITERATIONS*
- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*
- *MSK_IPAR_MIO_MAX_NUM_SOLUTIONS*
- *MSK_IPAR_SIM_MAX_ITERATIONS*

Other

- *MSK_IPAR_COMPRESS_STATFILE*

13.2 Parameters (alphabetical list sorted by type)

- *Double parameters*
- *Integer parameters*
- *String parameters*

13.2.1 Double parameters

MSK_DPAR_ANA_SOL_INFEAS_TOL

If a constraint violates its bound with an amount larger than this value, the constraint name, index and violation will be printed by the solution analyzer.

Default 1e-6

Accepted [0.0; +inf]

Groups *Analysis*

MSK_DPAR_BASIS_REL_TOL_S

Maximum relative dual bound violation allowed in an optimal basic solution.

Default 1.0e-12

Accepted [0.0; +inf]

Groups *Simplex optimizer, Termination criteria*

MSK_DPAR_BASIS_TOL_S

Maximum absolute dual bound violation in an optimal basic solution.

Default 1.0e-6

Accepted [1.0e-9; +inf]

Groups *Simplex optimizer, Termination criteria*

MSK_DPAR_BASIS_TOL_X

Maximum absolute primal bound violation allowed in an optimal basic solution.

Default 1.0e-6

Accepted [1.0e-9; +inf]

Groups *Simplex optimizer, Termination criteria*

MSK_DPAR_CHECK_CONVEXITY_REL_TOL

This parameter controls when the full convexity check declares a problem to be non-convex. Increasing this tolerance relaxes the criteria for declaring the problem non-convex.

A problem is declared non-convex if negative (positive) pivot elements are detected in the Cholesky factor of a matrix which is required to be PSD (NSD). This parameter controls how much this non-negativity requirement may be violated.

If d_i is the pivot element for column i , then the matrix Q is considered to not be PSD if:

$$d_i \leq -|Q_{ii}| \text{check_convexity_rel_tol}$$

Default 1e-10

Accepted [0; +inf]

Groups *Interior-point method*

MSK_DPAR_DATA_SYM_MAT_TOL

Absolute zero tolerance for elements in symmetric matrixes. If any value in a symmetric matrix is smaller than this parameter in absolute terms MOSEK will treat the values as zero and generate a warning.

Default 1.0e-12

Accepted [1.0e-16; 1.0e-6]

Groups *Data check*

MSK_DPAR_DATA_SYM_MAT_TOL_HUGE

An element in a symmetric matrix which is larger than this value in absolute size causes an error.

Default 1.0e20

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_SYM_MAT_TOL_LARGE

An element in a symmetric matrix which is larger than this value in absolute size causes a warning message to be printed.

Default 1.0e10

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_AIJ

Absolute zero tolerance for elements in A . If any value A_{ij} is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Default 1.0e-12

Accepted [1.0e-16; 1.0e-6]

Groups *Data check*

MSK_DPAR_DATA_TOL_AIJ_HUGE

An element in A which is larger than this value in absolute size causes an error.

Default 1.0e20

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_AIJ_LARGE

An element in A which is larger than this value in absolute size causes a warning message to be printed.

Default 1.0e10

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_BOUND_INF

Any bound which in absolute value is greater than this parameter is considered infinite.

Default 1.0e16

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_BOUND_WRN

If a bound value is larger than this value in absolute size, then a warning message is issued.

Default 1.0e8

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_C_HUGE

An element in c which is larger than the value of this parameter in absolute terms is considered to be huge and generates an error.

Default 1.0e16

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_CJ_LARGE

An element in c which is larger than this value in absolute terms causes a warning message to be printed.

Default 1.0e8

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_QIJ

Absolute zero tolerance for elements in Q matrices.

Default 1.0e-16

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_DATA_TOL_X

Zero tolerance for constraints and variables i.e. if the distance between the lower and upper bound is less than this value, then the lower and upper bound is considered identical.

Default 1.0e-8

Accepted [0.0; +inf]

Groups *Data check*

MSK_DPAR_INTPNT_CO_TOL_DFEAS

Dual feasibility tolerance used by the conic interior-point optimizer.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Conic interior-point method*

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

MSK_DPAR_INTPNT_CO_TOL_INFEAS

Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-10

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Conic interior-point method*

MSK_DPAR_INTPNT_CO_TOL_MU_RED

Relative complementarity gap feasibility tolerance used by the conic interior-point optimizer.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Conic interior-point method*

MSK_DPAR_INTPNT_CO_TOL_NEAR_REL

If **MOSEK** cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Default 1000

Accepted [1.0; +inf]

Groups *Interior-point method, Termination criteria, Conic interior-point method*

MSK_DPAR_INTPNT_CO_TOL_PFEAS

Primal feasibility tolerance used by the conic interior-point optimizer.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Conic interior-point method*

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

MSK_DPAR_INTPNT_CO_TOL_REL_GAP

Relative gap termination tolerance used by the conic interior-point optimizer.

Default 1.0e-7

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Conic interior-point method*

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

MSK_DPAR_INTPNT_NL_MERIT_BAL

Controls if the complementarity and infeasibility is converging to zero at about equal rates.

Default 1.0e-4

Accepted [0.0; 0.99]

Groups *Interior-point method, Nonlinear convex method*

MSK_DPAR_INTPNT_NL_TOL_DFEAS

Dual feasibility tolerance used when a nonlinear model is solved.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Nonlinear convex method*

MSK_DPAR_INTPNT_NL_TOL_MU_RED

Relative complementarity gap tolerance for the nonlinear solver.

Default 1.0e-12

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Nonlinear convex method*

MSK_DPAR_INTPNT_NL_TOL_NEAR_REL

If the MOSEK nonlinear interior-point optimizer cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Default 1000.0

Accepted [1.0; +inf]

Groups *Interior-point method, Termination criteria, Nonlinear convex method*

MSK_DPAR_INTPNT_NL_TOL_PFEAS

Primal feasibility tolerance used when a nonlinear model is solved.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Nonlinear convex method*

MSK_DPAR_INTPNT_NL_TOL_REL_GAP

Relative gap termination tolerance for nonlinear problems.

Default 1.0e-6

Accepted [1.0e-14; +inf]

Groups *Termination criteria, Interior-point method, Nonlinear convex method*

MSK_DPAR_INTPNT_NL_TOL_REL_STEP

Relative step size to the boundary for general nonlinear optimization problems.

Default 0.995

Accepted [1.0e-4; 0.9999999]

Groups *Interior-point method, Nonlinear convex method*

MSK_DPAR_INTPNT_QO_TOL_DFEAS

Dual feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem..

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

See also *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*

MSK_DPAR_INTPNT_QO_TOL_INFEAS

Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-10

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_MU_RED

Relative complementarity gap feasibility tolerance used when interior-point optimizer is applied to a quadratic optimization problem.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_NEAR_REL

If **MOSEK** cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Default 1000

Accepted [1.0; +inf]

Groups *Interior-point method, Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_PFEAS

Primal feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

See also [*MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*](#)

MSK_DPAR_INTPNT_QO_TOL_REL_GAP

Relative gap termination tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

See also [*MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*](#)

MSK_DPAR_INTPNT_TOL_DFEAS

Dual feasibility tolerance used for linear optimization problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

MSK_DPAR_INTPNT_TOL_DSAFE

Controls the initial dual starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it might be worthwhile to increase this value.

Default 1.0

Accepted [1.0e-4; +inf]

Groups *Interior-point method*

MSK_DPAR_INTPNT_TOL_INFEAS

Controls when the optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-10

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria, Nonlinear convex method*

MSK_DPAR_INTPNT_TOL_MU_RED

Relative complementarity gap tolerance for linear problems.

Default 1.0e-16

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

MSK_DPAR_INTPNT_TOL_PATH

Controls how close the interior-point optimizer follows the central path. A large value of this parameter means the central is followed very closely. On numerical unstable problems it may be worthwhile to increase this parameter.

Default 1.0e-8

Accepted [0.0; 0.9999]

Groups *Interior-point method*

MSK_DPAR_INTPNT_TOL_PFEAS

Primal feasibility tolerance used for linear optimization problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method, Termination criteria*

MSK_DPAR_INTPNT_TOL_PSAFE

Controls the initial primal starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it may be worthwhile to increase this value.

Default 1.0

Accepted [1.0e-4; +inf]

Groups *Interior-point method*

MSK_DPAR_INTPNT_TOL_REL_GAP

Relative gap termination tolerance for linear problems.

Default 1.0e-8

Accepted [1.0e-14; +inf]

Groups *Termination criteria, Interior-point method*

MSK_DPAR_INTPNT_TOL_REL_STEP

Relative step size to the boundary for linear and quadratic optimization problems.

Default 0.9999

Accepted [1.0e-4; 0.999999]

Groups *Interior-point method*

MSK_DPAR_INTPNT_TOL_STEP_SIZE

Minimal step size tolerance. If the step size falls below the value of this parameter, then the interior-point optimizer assumes that it is stalled. In other words the interior-point optimizer does not make any progress and therefore it is better stop.

Default 1.0e-6

Accepted [0.0; 1.0]

Groups *Interior-point method*

MSK_DPAR_LOWER_OBJ_CUT

If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [*MSK_DPAR_LOWER_OBJ_CUT*, *MSK_DPAR_UPPER_OBJ_CUT*], then **MOSEK** is terminated.

Default -1.0e30

Accepted [-inf; +inf]

Groups *Termination criteria*

See also *MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH*

MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH

If the lower objective cut is less than the value of this parameter value, then the lower objective cut i.e. *MSK_DPAR_LOWER_OBJ_CUT* is treated as $-\infty$.

Default -0.5e30

Accepted [-inf; +inf]

Groups *Termination criteria*

MSK_DPAR_MIO_DISABLE_TERM_TIME

This parameter specifies the number of seconds n during which the termination criteria governed by

- *MSK_IPAR_MIO_MAX_NUM_RELAXS*
- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*

- *MSK_DPAR_MIO_NEAR_TOL_ABS_GAP*
- *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*

is disabled since the beginning of the optimization.

A negative value is identical to infinity i.e. the termination criteria are never checked.

Default -1.0

Accepted [-inf; +inf]

Groups *Mixed-integer optimization, Termination criteria*

See also *MSK_IPAR_MIO_MAX_NUM_RELAXS*, *MSK_IPAR_MIO_MAX_NUM_BRANCHES*,
MSK_DPAR_MIO_NEAR_TOL_ABS_GAP, *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*

MSK_DPAR_MIO_MAX_TIME

This parameter limits the maximum time spent by the mixed-integer optimizer. A negative number means infinity.

Default -1.0

Accepted [-inf; +inf]

Groups *Mixed-integer optimization, Termination criteria*

MSK_DPAR_MIO_NEAR_TOL_ABS_GAP

Relaxed absolute optimality tolerance employed by the mixed-integer optimizer. This termination criteria is delayed. See *MSK_DPAR_MIO_DISABLE_TERM_TIME* for details.

Default 0.0

Accepted [0.0; +inf]

Groups *Mixed-integer optimization*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

MSK_DPAR_MIO_NEAR_TOL_REL_GAP

The mixed-integer optimizer is terminated when this tolerance is satisfied. This termination criteria is delayed. See *MSK_DPAR_MIO_DISABLE_TERM_TIME* for details.

Default 1.0e-3

Accepted [0.0; +inf]

Groups *Mixed-integer optimization, Termination criteria*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

MSK_DPAR_MIO_REL_GAP_CONST

This value is used to compute the relative gap for the solution to an integer optimization problem.

Default 1.0e-10

Accepted [1.0e-15; +inf]

Groups *Mixed-integer optimization, Termination criteria*

MSK_DPAR_MIO_TOL_ABS_GAP

Absolute optimality tolerance employed by the mixed-integer optimizer.

Default 0.0

Accepted [0.0; +inf]

Groups *Mixed-integer optimization*

MSK_DPAR_MIO_TOL_ABS_RELAX_INT

Absolute integer feasibility tolerance. If the distance to the nearest integer is less than this tolerance then an integer constraint is assumed to be satisfied.

Default 1.0e-5

Accepted [1e-9; +inf]

Groups *Mixed-integer optimization*

MSK_DPAR_MIO_TOL_FEAS

Feasibility tolerance for mixed integer solver.

Default 1.0e-6

Accepted [1e-9; 1e-3]

Groups *Mixed-integer optimization*

MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT

If the relative improvement of the dual bound is smaller than this value, the solver will terminate the root cut generation. A value of 0.0 means that the value is selected automatically.

Default 0.0

Accepted [0.0; 1.0]

Groups *Mixed-integer optimization*

MSK_DPAR_MIO_TOL_REL_GAP

Relative optimality tolerance employed by the mixed-integer optimizer.

Default 1.0e-4

Accepted [0.0; +inf]

Groups *Mixed-integer optimization, Termination criteria*

MSK_DPAR_OPTIMIZER_MAX_TIME

Maximum amount of time the optimizer is allowed to spent on the optimization. A negative number means infinity.

Default -1.0

Accepted [-inf; +inf]

Groups *Termination criteria*

MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP

Absolute tolerance employed by the linear dependency checker.

Default 1.0e-6

Accepted [0.0; +inf]

Groups *Presolve*

MSK_DPAR_PRESOLVE_TOL_AIJ

Absolute zero tolerance employed for a_{ij} in the presolve.

Default 1.0e-12

Accepted [1.0e-15; +inf]

Groups *Presolve*

MSK_DPAR_PRESOLVE_TOL_REL_LINDEP

Relative tolerance employed by the linear dependency checker.

Default 1.0e-10

Accepted [0.0; +inf]

Groups *Presolve*

MSK_DPAR_PRESOLVE_TOL_S

Absolute zero tolerance employed for s_i in the presolve.

Default 1.0e-8

Accepted [0.0; +inf]

Groups *Presolve*

MSK_DPAR_PREOLVE_TOL_X

Absolute zero tolerance employed for x_j in the presolve.

Default 1.0e-8

Accepted [0.0; +inf]

Groups *Presolve*

MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL

This parameter determines when columns are dropped in incomplete Cholesky factorization during reformulation of quadratic problems.

Default 1e-15

Accepted [0; +inf]

Groups *Interior-point method*

MSK_DPAR_SEMIDEFINITE_TOL_APPROX

Tolerance to define a matrix to be positive semidefinite.

Default 1.0e-10

Accepted [1.0e-15; +inf]

Groups *Data check*

MSK_DPAR_SIM_LU_TOL_REL_PIV

Relative pivot tolerance employed when computing the LU factorization of the basis in the simplex optimizers and in the basis identification procedure.

A value closer to 1.0 generally improves numerical stability but typically also implies an increase in the computational work.

Default 0.01

Accepted [1.0e-6; 0.999999]

Groups *Basis identification, Simplex optimizer*

MSK_DPAR_SIMPLEX_ABS_TOL_PIV

Absolute pivot tolerance employed by the simplex optimizers.

Default 1.0e-7

Accepted [1.0e-12; +inf]

Groups *Simplex optimizer*

MSK_DPAR_UPPER_OBJ_CUT

If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [*MSK_DPAR_LOWER_OBJ_CUT*, *MSK_DPAR_UPPER_OBJ_CUT*], then **MOSEK** is terminated.

Default 1.0e30

Accepted [-inf; +inf]

Groups *Termination criteria*

See also *MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH*

MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH

If the upper objective cut is greater than the value of this parameter, then the upper objective cut *MSK_DPAR_UPPER_OBJ_CUT* is treated as ∞ .

Default 0.5e30

Accepted [-inf; +inf]

Groups *Termination criteria*

13.2.2 Integer parameters

MSK_IPAR_ANA_SOL_BASIS

Controls whether the basis matrix is analyzed in solution analyzer.

Default *ON*

Accepted *ON, OFF*

Groups *Analysis*

MSK_IPAR_ANA_SOL_PRINT_VIOLATED

Controls whether a list of violated constraints is printed.

All constraints violated by more than the value set by the parameter *MSK_DPAR_ANA_SOL_INFEAS_TOL* will be printed.

Default *OFF*

Accepted *ON, OFF*

Groups *Analysis*

MSK_IPAR_AUTO_SORT_A_BEFORE_OPT

Controls whether the elements in each column of *A* are sorted before an optimization is performed. This is not required but makes the optimization more deterministic.

Default *OFF*

Accepted *ON, OFF*

Groups *Debugging*

MSK_IPAR_AUTO_UPDATE_SOL_INFO

Controls whether the solution information items are automatically updated after an optimization is performed.

Default *OFF*

Accepted *ON, OFF*

Groups *Overall system*

MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE

If a slack variable is in the basis, then the corresponding column in the basis is a unit vector with -1 in the right position. However, if this parameter is set to *MSK_ON*, -1 is replaced by 1.

Default *OFF*

Accepted *ON, OFF*

Groups *Simplex optimizer*

MSK_IPAR_BI_CLEAN_OPTIMIZER

Controls which simplex optimizer is used in the clean-up phase.

Default *FREE*

Accepted *FREE, INTPNT, CONIC, PRIMAL_SIMPLEX, DUAL_SIMPLEX, FREE_SIMPLEX, MIXED_INT*

Groups *Basis identification, Overall solver*

MSK_IPAR_BI_IGNORE_MAX_ITER

If the parameter *MSK_IPAR_INTPNT_BASIS* has the value *MSK_BI_NO_ERROR* and the interior-point optimizer has terminated due to maximum number of iterations, then basis identification is performed if this parameter has the value *MSK_ON*.

Default *OFF*

Accepted *ON, OFF*

Groups *Interior-point method, Basis identification*

MSK_IPAR_BI_IGNORE_NUM_ERROR

If the parameter *MSK_IPAR_INTPNT_BASIS* has the value *MSK_BI_NO_ERROR* and the interior-point optimizer has terminated due to a numerical problem, then basis identification is performed if this parameter has the value *MSK_ON*.

Default *OFF*

Accepted *ON, OFF*

Groups *Interior-point method, Basis identification*

MSK_IPAR_BI_MAX_ITERATIONS

Controls the maximum number of simplex iterations allowed to optimize a basis after the basis identification.

Default 1000000

Accepted [0; +inf]

Groups *Basis identification, Termination criteria*

MSK_IPAR_CACHE_LICENSE

Specifies if the license is kept checked out for the lifetime of the mosek environment (*MSK_ON*) or returned to the server immediately after the optimization (*MSK_OFF*).

By default the license is checked out for the lifetime of the **MOSEK** environment by the first call to the optimizer.

Check-in and check-out of licenses have an overhead. Frequent communication with the license server should be avoided.

Default *ON*

Accepted *ON, OFF*

Groups *License manager*

MSK_IPAR_CHECK_CONVEXITY

Specify the level of convexity check on quadratic problems.

Default *FULL*

Accepted *NONE, SIMPLE, FULL*

Groups *Data check, Nonlinear convex method*

MSK_IPAR_COMPRESS_STATFILE

Control compression of stat files.

Default *ON*

Accepted *ON, OFF*

MSK_IPAR_INFEAS_GENERIC_NAMES

Controls whether generic names are used when an infeasible subproblem is created.

Default *OFF*

Accepted *ON, OFF*

Groups *Infeasibility report*

MSK_IPAR_INFEAS_PREFER_PRIMAL

If both certificates of primal and dual infeasibility are supplied then only the primal is used when this option is turned on.

Default *ON*

Accepted *ON, OFF*

Groups *Overall solver*

MSK_IPAR_INFEAS_REPORT_AUTO

Controls whether an infeasibility report is automatically produced after the optimization if the problem is primal or dual infeasible.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_INFEAS_REPORT_LEVEL

Controls the amount of information presented in an infeasibility report. Higher values imply more information.

Default *1*

Accepted *[0; +inf]*

Groups *Infeasibility report, Output information*

MSK_IPAR_INTPNT_BASIS

Controls whether the interior-point optimizer also computes an optimal basis.

Default *ALWAYS*

Accepted *NEVER, ALWAYS, NO_ERROR, IF_FEASIBLE, RESERVED*

Groups *Interior-point method, Basis identification*

See also *MSK_IPAR_BI_IGNORE_MAX_ITER, MSK_IPAR_BI_IGNORE_NUM_ERROR, MSK_IPAR_BI_MAX_ITERATIONS, MSK_IPAR_BI_CLEAN_OPTIMIZER*

MSK_IPAR_INTPNT_DIFF_STEP

Controls whether different step sizes are allowed in the primal and dual space.

Default *ON*

Accepted

- *ON*: Different step sizes are allowed.
- *OFF*: Different step sizes are not allowed.

Groups *Interior-point method*

MSK_IPAR_INTPNT_HOTSTART

Currently not in use.

Default *NONE*

Accepted *NONE, PRIMAL, DUAL, PRIMAL_DUAL*

Groups *Interior-point method*

MSK_IPAR_INTPNT_MAX_ITERATIONS

Controls the maximum number of iterations allowed in the interior-point optimizer.

Default *400*

Accepted *[0; +inf]*

Groups *Interior-point method, Termination criteria*

MSK_IPAR_INTPNT_MAX_NUM_COR

Controls the maximum number of correctors allowed by the multiple corrector procedure. A negative value means that **MOSEK** is making the choice.

Default -1

Accepted [-1; +inf]

Groups *Interior-point method*

MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS

Maximum number of steps to be used by the iterative refinement of the search direction. A negative value implies that the optimizer chooses the maximum number of iterative refinement steps.

Default -1

Accepted [-inf; +inf]

Groups *Interior-point method*

MSK_IPAR_INTPNT_MULTI_THREAD

Controls whether the interior-point optimizers are allowed to employ multiple threads if more threads is available.

Default *ON*

Accepted *ON, OFF*

Groups *Overall system*

MSK_IPAR_INTPNT_OFF_COL_TRH

Controls how many offending columns are detected in the Jacobian of the constraint matrix.

0	no detection
1	aggressive detection
> 1	higher values mean less aggressive detection

Default 40

Accepted [0; +inf]

Groups *Interior-point method*

MSK_IPAR_INTPNT_ORDER_METHOD

Controls the ordering strategy used by the interior-point optimizer when factorizing the Newton equation system.

Default *FREE*

Accepted *FREE, APPMINLOC, EXPERIMENTAL, TRY_GRAPHPAR, FORCE_GRAPHPAR, NONE*

Groups *Interior-point method*

MSK_IPAR_INTPNT_REGULARIZATION_USE

Controls whether regularization is allowed.

Default *ON*

Accepted *ON, OFF*

Groups *Interior-point method*

MSK_IPAR_INTPNT_SCALING

Controls how the problem is scaled before the interior-point optimizer is used.

Default *FREE*

Accepted *FREE, NONE, MODERATE, AGGRESSIVE*

Groups *Interior-point method*

MSK_IPAR_INTPNT_SOLVE_FORM

Controls whether the primal or the dual problem is solved.

Default *FREE*

Accepted *FREE, PRIMAL, DUAL*

Groups *Interior-point method*

MSK_IPAR_INTPNT_STARTING_POINT

Starting point used by the interior-point optimizer.

Default *FREE*

Accepted *FREE, GUESS, CONSTANT, SATISFY_BOUNDS*

Groups *Interior-point method*

MSK_IPAR_LICENSE_DEBUG

This option is used to turn on debugging of the license manager.

Default *OFF*

Accepted *ON, OFF*

Groups *License manager*

MSK_IPAR_LICENSE_PAUSE_TIME

If *MSK_IPAR_LICENSE_WAIT* = *MSK_ON* and no license is available, then **MOSEK** sleeps a number of milliseconds between each check of whether a license has become free.

Default 100

Accepted [0; 1000000]

Groups *License manager*

MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS

Controls whether license features expire warnings are suppressed.

Default *OFF*

Accepted *ON, OFF*

Groups *License manager, Output information*

MSK_IPAR_LICENSE_TRH_EXPIRY_WRN

If a license feature expires in a numbers days less than the value of this parameter then a warning will be issued.

Default 7

Accepted [0; +inf]

Groups *License manager, Output information*

MSK_IPAR_LICENSE_WAIT

If all licenses are in use **MOSEK** returns with an error code. However, by turning on this parameter **MOSEK** will wait for an available license.

Default *OFF*

Accepted *ON, OFF*

Groups *Overall solver, Overall system, License manager*

MSK_IPAR_LOG

Controls the amount of log information. The value 0 implies that all log information is suppressed. A higher level implies that more information is logged.

Please note that if a task is employed to solve a sequence of optimization problems the value of this parameter is reduced by the value of *MSK_IPAR_LOG_CUT_SECOND_OPT* for the second and any subsequent optimizations.

Default 10

Accepted [0; +inf]

Groups *Output information, Logging*

See also *MSK_IPAR_LOG_CUT_SECOND_OPT*

MSK_IPAR_LOG_ANA_PRO

Controls amount of output from the problem analyzer.

Default 1

Accepted [0; +inf]

Groups *Analysis, Logging*

MSK_IPAR_LOG_BI

Controls the amount of output printed by the basis identification procedure. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Basis identification, Output information, Logging*

MSK_IPAR_LOG_BI_FREQ

Controls how frequent the optimizer outputs information about the basis identification and how frequent the user-defined callback function is called.

Default 2500

Accepted [0; +inf]

Groups *Basis identification, Output information, Logging*

MSK_IPAR_LOG_CHECK_CONVEXITY

Controls logging in convexity check on quadratic problems. Set to a positive value to turn logging on. If a quadratic coefficient matrix is found to violate the requirement of PSD (NSD) then a list of negative (positive) pivot elements is printed. The absolute value of the pivot elements is also shown.

Default 0

Accepted [0; +inf]

Groups *Data check, Nonlinear convex method*

MSK_IPAR_LOG_CUT_SECOND_OPT

If a task is employed to solve a sequence of optimization problems, then the value of the log levels is reduced by the value of this parameter. E.g *MSK_IPAR_LOG* and *MSK_IPAR_LOG_SIM* are reduced by the value of this parameter for the second and any subsequent optimizations.

Default 1

Accepted [0; +inf]

Groups *Output information, Logging*

See also *MSK_IPAR_LOG*, *MSK_IPAR_LOG_INTPNT*, *MSK_IPAR_LOG_MIO*,
MSK_IPAR_LOG_SIM

MSK_IPAR_LOG_EXPAND

Controls the amount of logging when a data item such as the maximum number constraints is expanded.

Default 0

Accepted [0; +inf]

Groups *Output information, Logging*

MSK_IPAR_LOG_FEAS_REPAIR

Controls the amount of output printed when performing feasibility repair. A value higher than one means extensive logging.

Default 1

Accepted [0; +inf]

Groups *Output information, Logging*

MSK_IPAR_LOG_FILE

If turned on, then some log info is printed when a file is written or read.

Default 1

Accepted [0; +inf]

Groups *Data input/output, Output information, Logging*

MSK_IPAR_LOG_INFEAS_ANA

Controls amount of output printed by the infeasibility analyzer procedures. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Infeasibility report, Output information, Logging*

MSK_IPAR_LOG_INTPNT

Controls amount of output printed by the interior-point optimizer. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Interior-point method, Output information, Logging*

MSK_IPAR_LOG_MIO

Controls the log level for the mixed-integer optimizer. A higher level implies that more information is logged.

Default 4

Accepted [0; +inf]

Groups *Mixed-integer optimization, Output information, Logging*

MSK_IPAR_LOG_MIO_FREQ

Controls how frequent the mixed-integer optimizer prints the log line. It will print line every time *MSK_IPAR_LOG_MIO_FREQ* relaxations have been solved.

Default 10

Accepted [-inf; +inf]

Groups *Mixed-integer optimization, Output information, Logging*

MSK_IPAR_LOG_ORDER

If turned on, then factor lines are added to the log.

Default 1

Accepted [0; +inf]

Groups *Output information, Logging*

MSK_IPAR_LOG_PRESOLVE

Controls amount of output printed by the presolve procedure. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Logging*

MSK_IPAR_LOG_RESPONSE

Controls amount of output printed when response codes are reported. A higher level implies that more information is logged.

Default 0

Accepted [0; +inf]

Groups *Output information, Logging*

MSK_IPAR_LOG_SENSITIVITY

Controls the amount of logging during the sensitivity analysis.

0. Means no logging information is produced.
1. Timing information is printed.
2. Sensitivity results are printed.

Default 1

Accepted [0; +inf]

Groups *Output information, Logging*

MSK_IPAR_LOG_SENSITIVITY_OPT

Controls the amount of logging from the optimizers employed during the sensitivity analysis. 0 means no logging information is produced.

Default 0

Accepted [0; +inf]

Groups *Output information, Logging*

MSK_IPAR_LOG_SIM

Controls amount of output printed by the simplex optimizer. A higher level implies that more information is logged.

Default 4

Accepted [0; +inf]

Groups *Simplex optimizer, Output information, Logging*

MSK_IPAR_LOG_SIM_FREQ

Controls how frequent the simplex optimizer outputs information about the optimization and how frequent the user-defined callback function is called.

Default 1000

Accepted [0; +inf]

Groups *Simplex optimizer, Output information, Logging*

MSK_IPAR_LOG_SIM_MINOR

Currently not in use.

Default 1

Accepted [0; +inf]

Groups *Simplex optimizer, Output information*

MSK_IPAR_LOG_STORAGE

When turned on, **MOSEK** prints messages regarding the storage usage and allocation.

Default 0

Accepted [0; +inf]

Groups *Output information, Overall system, Logging*

MSK_IPAR_MAX_NUM_WARNINGS

Each warning is shown a limit number times controlled by this parameter. A negative value is identical to infinite number of times.

Default 10

Accepted [-inf; +inf]

Groups *Output information*

MSK_IPAR_MIO_BRANCH_DIR

Controls whether the mixed-integer optimizer is branching up or down by default.

Default *FREE*

Accepted *FREE, UP, DOWN, NEAR, FAR, ROOT_LP, GUIDED, PSEUDOCOST*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CONSTRUCT_SOL

If set to *MSK_ON* and all integer variables have been given a value for which a feasible mixed integer solution exists, then **MOSEK** generates an initial solution to the mixed integer problem by fixing all integer values and solving the remaining problem.

Default *OFF*

Accepted *ON, OFF*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_CLIQUE

Controls whether clique cuts should be generated.

Default *ON*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_CMIR

Controls whether mixed integer rounding cuts should be generated.

Default *ON*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_GMI

Controls whether GMI cuts should be generated.

Default *ON*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_IMPLIED_BOUND

Controls whether implied bound cuts should be generated.

Default *OFF*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_KNAPSACK_COVER

Controls whether knapsack cover cuts should be generated.

Default *OFF*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_CUT_SELECTION_LEVEL

Controls how aggressively generated cuts are selected to be included in the relaxation.

- 1. The optimizer chooses the level of cut selection
- 0. Generated cuts less likely to be added to the relaxation
- 1. Cuts are more aggressively selected to be included in the relaxation

Default -1

Accepted [-1; +1]

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_HEURISTIC_LEVEL

Controls the heuristic employed by the mixed-integer optimizer to locate an initial good integer feasible solution. A value of zero means the heuristic is not used at all. A larger value than 0 means that a gradually more sophisticated heuristic is used which is computationally more expensive. A negative value implies that the optimizer chooses the heuristic. Normally a value around 3 to 5 should be optimal.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_MAX_NUM_BRANCHES

Maximum number of branches allowed during the branch and bound search. A negative value means infinite.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization, Termination criteria*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

MSK_IPAR_MIO_MAX_NUM_RELAXS

Maximum number of relaxations allowed during the branch and bound search. A negative value means infinite.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

MSK_IPAR_MIO_MAX_NUM_SOLUTIONS

The mixed-integer optimizer can be terminated after a certain number of different feasible solutions has been located. If this parameter has the value $n > 0$, then the mixed-integer optimizer will be terminated when n feasible solutions have been located.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization, Termination criteria*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

MSK_IPAR_MIO_MODE

Controls whether the optimizer includes the integer restrictions when solving a (mixed) integer optimization problem.

Default *SATISFIED*

Accepted *IGNORED, SATISFIED*

Groups *Overall solver*

MSK_IPAR_MIO_MT_USER_CB

If true user callbacks are called from each thread used by mixed-integer optimizer. Otherwise it is only called from a single thread.

Default *OFF*

Accepted *ON, OFF*

Groups *Overall system*

MSK_IPAR_MIO_NODE_OPTIMIZER

Controls which optimizer is employed at the non-root nodes in the mixed-integer optimizer.

Default *FREE*

Accepted *FREE, INTPNT, CONIC, PRIMAL_SIMPLEX, DUAL_SIMPLEX, FREE_SIMPLEX, MIXED_INT*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_NODE_SELECTION

Controls the node selection strategy employed by the mixed-integer optimizer.

Default *FREE*

Accepted *FREE, FIRST, BEST, WORST, HYBRID, PSEUDO*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE

Enables or disables perspective reformulation in presolve.

Default *ON*

Accepted *ON, OFF*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_PROBING_LEVEL

Controls the amount of probing employed by the mixed-integer optimizer in presolve.

-1. The optimizer chooses the level of probing employed

0. Probing is disabled

1. A low amount of probing is employed
2. A medium amount of probing is employed
3. A high amount of probing is employed

Default -1

Accepted [-1; 3]

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_RINS_MAX_NODES

Controls the maximum number of nodes allowed in each call to the RINS heuristic. The default value of -1 means that the value is determined automatically. A value of zero turns off the heuristic.

Default -1

Accepted [-1; +inf]

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_ROOT_OPTIMIZER

Controls which optimizer is employed at the root node in the mixed-integer optimizer.

Default *FREE*

Accepted *FREE, INTPNT, CONIC, PRIMAL_SIMPLEX, DUAL_SIMPLEX, FREE_SIMPLEX, MIXED_INT*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL

Controls whether presolve can be repeated at root node.

- -1 The optimizer chooses whether presolve is repeated
- 0 Never repeat presolve
- 1 Always repeat presolve

Default -1

Accepted [-1; 1]

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_VB_DETECTION_LEVEL

Controls how much effort is put into detecting variable bounds.

- 1. The optimizer chooses
- 0. No variable bounds are detected
- 1. Only detect variable bounds that are directly represented in the problem
- 2. Detect variable bounds in probing

Default -1

Accepted [-1; +2]

Groups *Mixed-integer optimization*

MSK_IPAR_MT_SPINCOUNT

Set the number of iterations to spin before sleeping.

Default 0

Accepted [0; 1000000000]

Groups *Overall system***MSK_IPAR_NUM_THREADS**

Controls the number of threads employed by the optimizer. If set to 0 the number of threads used will be equal to the number of cores detected on the machine.

Default 0

Accepted [0; +inf]

Groups *Overall system*

MSK_IPAR_OPF_MAX_TERMS_PER_LINE

The maximum number of terms (linear and quadratic) per line when an OPF file is written.

Default 5

Accepted [0; +inf]

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_HEADER

Write a text header with date and **MOSEK** version in an OPF file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_HINTS

Write a hint section with problem dimensions in the beginning of an OPF file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_PARAMETERS

Write a parameter section in an OPF file.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_PROBLEM

Write objective, constraints, bounds etc. to an OPF file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_BAS

If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and a basic solution is defined, include the basic solution in OPF files.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_ITG

If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and an integer solution is defined, write the integer solution in OPF files.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output***MSK_IPAR_OPF_WRITE_SOL_ITR**

If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and an interior solution is defined, write the interior solution in OPF files.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output***MSK_IPAR_OPF_WRITE_SOLUTIONS**

Enable inclusion of solutions in the OPF files.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output***MSK_IPAR_OPTIMIZER**

The parameter controls which optimizer is used to optimize the task.

Default *FREE*

Accepted *FREE, INTPNT, CONIC, PRIMAL_SIMPLEX, DUAL_SIMPLEX, FREE_SIMPLEX, MIXED_INT*

Groups *Overall solver***MSK_IPAR_PARAM_READ_CASE_NAME**

If turned on, then names in the parameter file are case sensitive.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output***MSK_IPAR_PARAM_READ_IGN_ERROR**

If turned on, then errors in parameter settings is ignored.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output***MSK_IPAR_PREOLVE_ELIMINATOR_MAX_FILL**

Controls the maximum amount of fill-in that can be created by one pivot in the elimination phase of the presolve. A negative value means the parameter value is selected automatically.

Default *-1*

Accepted *[-inf; +inf]*

Groups *Presolve***MSK_IPAR_PREOLVE_ELIMINATOR_MAX_NUM_TRIES**

Control the maximum number of times the eliminator is tried. A negative value implies **MOSEK** decides.

Default *-1*

Accepted *[-inf; +inf]*

Groups *Presolve***MSK_IPAR_PREOLVE_LEVEL**

Currently not used.

Default *-1*

Accepted [-inf; +inf]

Groups *Overall solver, Presolve*

MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH

The linear dependency check is potentially computationally expensive.

Default 100

Accepted [-inf; +inf]

Groups *Presolve*

MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH

The linear dependency check is potentially computationally expensive.

Default 100

Accepted [-inf; +inf]

Groups *Presolve*

MSK_IPAR_PRESOLVE_LINDEP_USE

Controls whether the linear constraints are checked for linear dependencies.

Default *ON*

Accepted

- *ON*: Turns the linear dependency check on.
- *OFF*: Turns the linear dependency check off.

Groups *Presolve*

MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS

Controls the maximum number of reductions performed by the presolve. The value of the parameter is normally only changed in connection with debugging. A negative value implies that an infinite number of reductions are allowed.

Default -1

Accepted [-inf; +inf]

Groups *Overall solver, Presolve*

MSK_IPAR_PRESOLVE_USE

Controls whether the presolve is applied to a problem before it is optimized.

Default *FREE*

Accepted *OFF, ON, FREE*

Groups *Overall solver, Presolve*

MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER

Controls which optimizer that is used to find the optimal repair.

Default *FREE*

Accepted *FREE, INTPNT, CONIC, PRIMAL_SIMPLEX, DUAL_SIMPLEX, FREE_SIMPLEX, MIXED_INT*

Groups *Overall solver*

MSK_IPAR_READ_DATA_COMPRESSED

If this option is turned on, it is assumed that the data file is compressed.

Default *FREE*

Accepted *NONE, FREE, GZIP*

Groups *Data input/output*

MSK_IPAR_READ_DATA_FORMAT

Format of the data file to be read.

Default *EXTENSION*

Accepted *EXTENSION, MPS, LP, OP, XML, FREE_MPS, TASK, CB, JSON_TASK*

Groups *Data input/output*

MSK_IPAR_READ_DEBUG

Turns on additional debugging information when reading files.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_READ_KEEP_FREE_CON

Controls whether the free constraints are included in the problem.

Default *OFF*

Accepted

- *ON*: The free constraints are kept.
- *OFF*: The free constraints are discarded.

Groups *Data input/output*

MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU

If this option is turned on, **MOSEK** will drop variables that are defined for the first time in the bounds section.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_READ_LP_QUOTED_NAMES

If a name is in quotes when reading an LP file, the quotes will be removed.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_READ_MPS_FORMAT

Controls how strictly the MPS file reader interprets the MPS format.

Default *FREE*

Accepted *STRICT, RELAXED, FREE, CPLEX*

Groups *Data input/output*

MSK_IPAR_READ_MPS_WIDTH

Controls the maximal number of characters allowed in one line of the MPS file.

Default 1024

Accepted [80; +inf]

Groups *Data input/output*

MSK_IPAR_READ_TASK_IGNORE_PARAM

Controls whether **MOSEK** should ignore the parameter setting defined in the task file and use the default parameter setting instead.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_REMOVE_UNUSED_SOLUTIONS

Removes unused solutions before the optimization is performed.

Default *OFF*

Accepted *ON, OFF*

Groups *Overall system*

MSK_IPAR_SENSITIVITY_ALL

Not applicable.

Default *OFF*

Accepted *ON, OFF*

Groups *Overall solver*

MSK_IPAR_SENSITIVITY_OPTIMIZER

Controls which optimizer is used for optimal partition sensitivity analysis.

Default *FREE_SIMPLEX*

Accepted *FREE, INTPNT, CONIC, PRIMAL_SIMPLEX, DUAL_SIMPLEX, FREE_SIMPLEX, MIXED_INT*

Groups *Overall solver, Simplex optimizer*

MSK_IPAR_SENSITIVITY_TYPE

Controls which type of sensitivity analysis is to be performed.

Default *BASIS*

Accepted *BASIS, OPTIMAL_PARTITION*

Groups *Overall solver*

MSK_IPAR_SIM_BASIS_FACTOR_USE

Controls whether an LU factorization of the basis is used in a hot-start. Forcing a refactorization sometimes improves the stability of the simplex optimizers, but in most cases there is a performance penalty.

Default *ON*

Accepted *ON, OFF*

Groups *Simplex optimizer*

MSK_IPAR_SIM_DEGEN

Controls how aggressively degeneration is handled.

Default *FREE*

Accepted *NONE, FREE, AGGRESSIVE, MODERATE, MINIMUM*

Groups *Simplex optimizer*

MSK_IPAR_SIM_DUAL_CRASH

Controls whether crashing is performed in the dual simplex optimizer.

If this parameter is set to x , then a crash will be performed if a basis consists of more than $(100 - x) \bmod f_v$ entries, where f_v is the number of fixed variables.

Default *90*

Accepted *[0; +inf]*

Groups *Dual simplex*

MSK_IPAR_SIM_DUAL_PHASEONE_METHOD

An experimental feature.

Default 0

Accepted [0; 10]

Groups *Simplex optimizer*

MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION

The dual simplex optimizer can use a so-called restricted selection/pricing strategy to chooses the outgoing variable. Hence, if restricted selection is applied, then the dual simplex optimizer first choose a subset of all the potential outgoing variables. Next, for some time it will choose the outgoing variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Default 50

Accepted [0; 100]

Groups *Dual simplex*

MSK_IPAR_SIM_DUAL_SELECTION

Controls the choice of the incoming variable, known as the selection strategy, in the dual simplex optimizer.

Default *FREE*

Accepted *FREE, FULL, ASE, DEVEX, SE, PARTIAL*

Groups *Dual simplex*

MSK_IPAR_SIM_EXPLOIT_DUPVEC

Controls if the simplex optimizers are allowed to exploit duplicated columns.

Default *OFF*

Accepted *ON, OFF, FREE*

Groups *Simplex optimizer*

MSK_IPAR_SIM_HOTSTART

Controls the type of hot-start that the simplex optimizer perform.

Default *FREE*

Accepted *NONE, FREE, STATUS_KEYS*

Groups *Simplex optimizer*

MSK_IPAR_SIM_HOTSTART_LU

Determines if the simplex optimizer should exploit the initial factorization.

Default *ON*

Accepted

- *ON*: Factorization is reused if possible.
- *OFF*: Factorization is recomputed.

Groups *Simplex optimizer*

MSK_IPAR_SIM_MAX_ITERATIONS

Maximum number of iterations that can be used by a simplex optimizer.

Default 10000000

Accepted [0; +inf]

Groups *Simplex optimizer, Termination criteria*

MSK_IPAR_SIM_MAX_NUM_SETBACKS

Controls how many set-backs are allowed within a simplex optimizer. A set-back is an event where the optimizer moves in the wrong direction. This is impossible in theory but may happen due to numerical problems.

Default 250

Accepted [0; +inf]

Groups *Simplex optimizer*

MSK_IPAR_SIM_NON_SINGULAR

Controls if the simplex optimizer ensures a non-singular basis, if possible.

Default *ON*

Accepted *ON, OFF*

Groups *Simplex optimizer*

MSK_IPAR_SIM_PRIMAL_CRASH

Controls whether crashing is performed in the primal simplex optimizer.

In general, if a basis consists of more than (100-this parameter value)% fixed variables, then a crash will be performed.

Default 90

Accepted [0; +inf]

Groups *Primal simplex*

MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD

An experimental feature.

Default 0

Accepted [0; 10]

Groups *Simplex optimizer*

MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION

The primal simplex optimizer can use a so-called restricted selection/pricing strategy to choose the outgoing variable. Hence, if restricted selection is applied, then the primal simplex optimizer first choose a subset of all the potential incoming variables. Next, for some time it will choose the incoming variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Default 50

Accepted [0; 100]

Groups *Primal simplex*

MSK_IPAR_SIM_PRIMAL_SELECTION

Controls the choice of the incoming variable, known as the selection strategy, in the primal simplex optimizer.

Default *FREE*

Accepted *FREE, FULL, ASE, DEVEX, SE, PARTIAL*

Groups *Primal simplex*

MSK_IPAR_SIM_REFACTOR_FREQ

Controls how frequent the basis is refactorized. The value 0 means that the optimizer determines the best point of refactorization.

It is strongly recommended NOT to change this parameter.

Default 0

Accepted [0; +inf]

Groups *Simplex optimizer*

MSK_IPAR_SIM_REFORMULATION

Controls if the simplex optimizers are allowed to reformulate the problem.

Default *OFF*

Accepted *ON, OFF, FREE, AGGRESSIVE*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SAVE_LU

Controls if the LU factorization stored should be replaced with the LU factorization corresponding to the initial basis.

Default *OFF*

Accepted *ON, OFF*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SCALING

Controls how much effort is used in scaling the problem before a simplex optimizer is used.

Default *FREE*

Accepted *FREE, NONE, MODERATE, AGGRESSIVE*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SCALING_METHOD

Controls how the problem is scaled before a simplex optimizer is used.

Default *POW2*

Accepted *POW2, FREE*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SOLVE_FORM

Controls whether the primal or the dual problem is solved by the primal-/dual-simplex optimizer.

Default *FREE*

Accepted *FREE, PRIMAL, DUAL*

Groups *Simplex optimizer*

MSK_IPAR_SIM_STABILITY_PRIORITY

Controls how high priority the numerical stability should be given.

Default 50

Accepted [0; 100]

Groups *Simplex optimizer*

MSK_IPAR_SIM_SWITCH_OPTIMIZER

The simplex optimizer sometimes chooses to solve the dual problem instead of the primal problem. This implies that if you have chosen to use the dual simplex optimizer and the problem is dualized, then it actually makes sense to use the primal simplex optimizer instead. If this parameter is on and the problem is dualized and furthermore the simplex optimizer is chosen to be the primal (dual) one, then it is switched to the dual (primal).

Default *OFF*

Accepted *ON, OFF*

Groups *Simplex optimizer*

MSK_IPAR_SOL_FILTER_KEEP_BASIC

If turned on, then basic and super basic constraints and variables are written to the solution file independent of the filter setting.

Default *OFF*

Accepted *ON, OFF*

Groups *Solution input/output*

MSK_IPAR_SOL_FILTER_KEEP_RANGED

If turned on, then ranged constraints and variables are written to the solution file independent of the filter setting.

Default *OFF*

Accepted *ON, OFF*

Groups *Solution input/output*

MSK_IPAR_SOL_READ_NAME_WIDTH

When a solution is read by **MOSEK** and some constraint, variable or cone names contain blanks, then a maximum name width must be specified. A negative value implies that no name contain blanks.

Default *-1*

Accepted *[-inf; +inf]*

Groups *Data input/output, Solution input/output*

MSK_IPAR_SOL_READ_WIDTH

Controls the maximal acceptable width of line in the solutions when read by **MOSEK**.

Default *1024*

Accepted *[80; +inf]*

Groups *Data input/output, Solution input/output*

MSK_IPAR_SOLUTION_CALLBACK

Indicates whether solution callbacks will be performed during the optimization.

Default *OFF*

Accepted *ON, OFF*

Groups *Progress callback, Overall solver*

MSK_IPAR_TIMING_LEVEL

Controls the amount of timing performed inside **MOSEK**.

Default *1*

Accepted *[0; +inf]*

Groups *Overall system*

MSK_IPAR_WRITE_BAS_CONSTRAINTS

Controls whether the constraint section is written to the basic solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_BAS_HEAD

Controls whether the header section is written to the basic solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_BAS_VARIABLES

Controls whether the variables section is written to the basic solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_DATA_COMPRESSED

Controls whether the data file is compressed while it is written. 0 means no compression while higher values mean more compression.

Default 0

Accepted [0; +inf]

Groups *Data input/output*

MSK_IPAR_WRITE_DATA_FORMAT

Controls the file format when writing task data to a file.

Default *EXTENSION*

Accepted *EXTENSION, MPS, LP, OP, XML, FREE_MPS, TASK, CB, JSON_TASK*

Groups *Data input/output*

MSK_IPAR_WRITE_DATA_PARAM

If this option is turned on the parameter settings are written to the data file as parameters.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_WRITE_FREE_CON

Controls whether the free constraints are written to the data file.

Default *ON*

Accepted

- *ON*: The free constraints are written.
- *OFF*: The free constraints are discarded.

Groups *Data input/output*

MSK_IPAR_WRITE_GENERIC_NAMES

Controls whether the generic names or user-defined names are used in the data file.

Default *OFF*

Accepted

- *ON*: Generic names are used.
- *OFF*: Generic names are not used.

Groups *Data input/output*

MSK_IPAR_WRITE_GENERIC_NAMES_IO

Index origin used in generic names.

Default 1

Accepted [0; +inf]

Groups *Data input/output*

MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS

Controls if the writer ignores incompatible problem items when writing files.

Default *OFF*

Accepted

- *ON*: Ignore items that cannot be written to the current output file format.
- *OFF*: Produce an error if the problem contains items that cannot be written to the current output file format.

Groups *Data input/output*

MSK_IPAR_WRITE_INT_CONSTRAINTS

Controls whether the constraint section is written to the integer solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_INT_HEAD

Controls whether the header section is written to the integer solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_INT_VARIABLES

Controls whether the variables section is written to the integer solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_LP_FULL_OBJ

Write all variables, including the ones with 0-coefficients, in the objective.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_WRITE_LP_LINE_WIDTH

Maximum width of line in an LP file written by **MOSEK**.

Default 80

Accepted [40; +inf]

Groups *Data input/output*

MSK_IPAR_WRITE_LP_QUOTED_NAMES

If this option is turned on, then **MOSEK** will quote invalid LP names when writing an LP file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_WRITE_LP_STRICT_FORMAT

Controls whether LP output files satisfy the LP format strictly.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output***MSK_IPAR_WRITE_LP_TERMS_PER_LINE**

Maximum number of terms on a single line in an LP file written by **MOSEK**. 0 means unlimited.

Default 10

Accepted [0; +inf]

Groups *Data input/output***MSK_IPAR_WRITE_MPS_FORMAT**

Controls in which format the MPS is written.

Default *FREE*

Accepted *STRICT, RELAXED, FREE, CPLEX*

Groups *Data input/output***MSK_IPAR_WRITE_MPS_INT**

Controls if marker records are written to the MPS file to indicate whether variables are integer restricted.

Default *ON*

Accepted

- *ON*: Marker records are written.
- *OFF*: Marker records are not written.

Groups *Data input/output***MSK_IPAR_WRITE_PRECISION**

Controls the precision with which **double** numbers are printed in the MPS data file. In general it is not worthwhile to use a value higher than 15.

Default 15

Accepted [0; +inf]

Groups *Data input/output***MSK_IPAR_WRITE_SOL_BARVARIABLES**

Controls whether the symmetric matrix variables section is written to the solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output***MSK_IPAR_WRITE_SOL_CONSTRAINTS**

Controls whether the constraint section is written to the solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output***MSK_IPAR_WRITE_SOL_HEAD**

Controls whether the header section is written to the solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output***MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES**

Even if the names are invalid MPS names, then they are employed when writing the solution file.

Default *OFF*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_SOL_VARIABLES

Controls whether the variables section is written to the solution file.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output, Solution input/output*

MSK_IPAR_WRITE_TASK_INC_SOL

Controls whether the solutions are stored in the task file too.

Default *ON*

Accepted *ON, OFF*

Groups *Data input/output*

MSK_IPAR_WRITE_XML_MODE

Controls if linear coefficients should be written by row or column when writing in the XML file format.

Default *ROW*

Accepted *ROW, COL*

Groups *Data input/output*

13.2.3 String parameters

MSK_SPAR_BAS_SOL_FILE_NAME

Name of the `bas` solution file.

Accepted Any valid file name.

Groups *Data input/output, Solution input/output*

MSK_SPAR_DATA_FILE_NAME

Data are read and written to this file.

Accepted Any valid file name.

Groups *Data input/output*

MSK_SPAR_DEBUG_FILE_NAME

MOSEK debug file.

Accepted Any valid file name.

Groups *Data input/output*

MSK_SPAR_INT_SOL_FILE_NAME

Name of the `int` solution file.

Accepted Any valid file name.

Groups *Data input/output, Solution input/output*

MSK_SPAR_ITR_SOL_FILE_NAME

Name of the `itr` solution file.

Accepted Any valid file name.

Groups *Data input/output, Solution input/output*

MSK_SPAR_MIO_DEBUG_STRING

For internal debugging purposes.

Accepted Any valid string.

Groups *Data input/output*

MSK_SPAR_PARAM_COMMENT_SIGN

Only the first character in this string is used. It is considered as a start of comment sign in the **MOSEK** parameter file. Spaces are ignored in the string.

Default

%%

Accepted Any valid string.

Groups *Data input/output*

MSK_SPAR_PARAM_READ_FILE_NAME

Modifications to the parameter database is read from this file.

Accepted Any valid file name.

Groups *Data input/output*

MSK_SPAR_PARAM_WRITE_FILE_NAME

The parameter database is written to this file.

Accepted Any valid file name.

Groups *Data input/output*

MSK_SPAR_READ_MPS_BOU_NAME

Name of the BOUNDS vector used. An empty name means that the first BOUNDS vector is used.

Accepted Any valid MPS name.

Groups *Data input/output*

MSK_SPAR_READ_MPS_OBJ_NAME

Name of the free constraint used as objective function. An empty name means that the first constraint is used as objective function.

Accepted Any valid MPS name.

Groups *Data input/output*

MSK_SPAR_READ_MPS_RAN_NAME

Name of the RANGE vector used. An empty name means that the first RANGE vector is used.

Accepted Any valid MPS name.

Groups *Data input/output*

MSK_SPAR_READ_MPS_RHS_NAME

Name of the RHS used. An empty name means that the first RHS vector is used.

Accepted Any valid MPS name.

Groups *Data input/output*

MSK_SPAR_REMOTE_ACCESS_TOKEN

An access token used to submit tasks to a remote **MOSEK** server. An access token is a random 32-byte string encoded in base64, i.e. it is a 44 character ASCII string.

Accepted Any valid string.

Groups *Overall system*

MSK_SPAR_SENSITIVITY_FILE_NAME

Not applicable.

Accepted Any valid string.

Groups *Data input/output*

MSK_SPAR_SENSITIVITY_RES_FILE_NAME

Not applicable.

Accepted Any valid string.

Groups *Data input/output*

MSK_SPAR_SOL_FILTER_XC_LOW

A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having $xc[i] > 0.5$ should be listed, whereas +0.5 means that all constraints having $xc[i] \geq blc[i] + 0.5$ should be listed. An empty filter means that no filter is applied.

Accepted Any valid filter.

Groups *Data input/output, Solution input/output*

MSK_SPAR_SOL_FILTER_XC_UPR

A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having $xc[i] < 0.5$ should be listed, whereas -0.5 means all constraints having $xc[i] \leq buc[i] - 0.5$ should be listed. An empty filter means that no filter is applied.

Accepted Any valid filter.

Groups *Data input/output, Solution input/output*

MSK_SPAR_SOL_FILTER_XX_LOW

A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having $xx[j] \geq 0.5$ should be listed, whereas "+0.5" means that all constraints having $xx[j] \geq blx[j] + 0.5$ should be listed. An empty filter means no filter is applied.

Accepted Any valid filter.

Groups *Data input/output, Solution input/output*

MSK_SPAR_SOL_FILTER_XX_UPR

A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having $xx[j] < 0.5$ should be printed, whereas "-0.5" means all constraints having $xx[j] \leq bux[j] - 0.5$ should be listed. An empty filter means no filter is applied.

Accepted Any valid file name.

Groups *Data input/output, Solution input/output*

MSK_SPAR_STAT_FILE_NAME

Statistics file name.

Accepted Any valid file name.

Groups *Data input/output*

MSK_SPAR_STAT_KEY

Key used when writing the summary file.

Accepted Any valid string.

Groups *Data input/output*

MSK_SPAR_STAT_NAME

Name used when writing the statistics file.

Accepted Any valid XML string.

Groups *Data input/output*

MSK_SPAR_WRITE_LP_GEN_VAR_NAME

Sometimes when an LP file is written additional variables must be inserted. They will have the prefix denoted by this parameter.

Default xmskgen

Accepted Any valid string.

Groups *Data input/output*

13.3 Response codes

- *Termination*
- *Warnings*
- *Errors*

13.3.1 Termination

MSK_RES_OK

No error occurred.

MSK_RES_TRM_MAX_ITERATIONS

The optimizer terminated at the maximum number of iterations.

MSK_RES_TRM_MAX_TIME

The optimizer terminated at the maximum amount of time.

MSK_RES_TRM_OBJECTIVE_RANGE

The optimizer terminated with an objective value outside the objective range.

MSK_RES_TRM_MIO_NEAR_REL_GAP

The mixed-integer optimizer terminated as the delayed near optimal relative gap tolerance was satisfied.

MSK_RES_TRM_MIO_NEAR_ABS_GAP

The mixed-integer optimizer terminated as the delayed near optimal absolute gap tolerance was satisfied.

MSK_RES_TRM_MIO_NUM_RELAXS

The mixed-integer optimizer terminated as the maximum number of relaxations was reached.

MSK_RES_TRM_MIO_NUM_BRANCHES

The mixed-integer optimizer terminated as the maximum number of branches was reached.

MSK_RES_TRM_NUM_MAX_NUM_INT_SOLUTIONS

The mixed-integer optimizer terminated as the maximum number of feasible solutions was reached.

MSK_RES_TRM_STALL

The optimizer is terminated due to slow progress.

Stalling means that numerical problems prevent the optimizer from making reasonable progress and that it make no sense to continue. In many cases this happens if the problem is badly scaled or otherwise ill-conditioned. There is no guarantee that the solution will be (near) feasible or near optimal. However, often stalling happens near the optimum, and the returned solution may be of good quality. Therefore, it is recommended to check the status of then solution. If the solution near optimal the solution is most likely good enough for most practical purposes.

Please note that if a linear optimization problem is solved using the interior-point optimizer with basis identification turned on, the returned basic solution likely to have high accuracy, even though the optimizer stalled.

Some common causes of stalling are a) badly scaled models, b) near feasible or near infeasible problems and c) a non-convex problems. Case c) is only relevant for general non-linear problems. It is not possible in general for **MOSEK** to check if a specific problems is convex since such a check would be NP hard in itself. This implies that care should be taken when solving problems involving general user defined functions.

MSK_RES_TRM_USER_CALLBACK

The optimizer terminated due to the return of the user-defined callback function.

MSK_RES_TRM_MAX_NUM_SETBACKS

The optimizer terminated as the maximum number of set-backs was reached. This indicates serious numerical problems and a possibly badly formulated problem.

MSK_RES_TRM_NUMERICAL_PROBLEM

The optimizer terminated due to numerical problems.

MSK_RES_TRM_INTERNAL

The optimizer terminated due to some internal reason. Please contact **MOSEK** support.

MSK_RES_TRM_INTERNAL_STOP

The optimizer terminated for internal reasons. Please contact **MOSEK** support.

13.3.2 Warnings

MSK_RES_WRN_OPEN_PARAM_FILE

The parameter file could not be opened.

MSK_RES_WRN_LARGE_BOUND

A numerically large bound value is specified.

MSK_RES_WRN_LARGE_LO_BOUND

A numerically large lower bound value is specified.

MSK_RES_WRN_LARGE_UP_BOUND

A numerically large upper bound value is specified.

MSK_RES_WRN_LARGE_CON_FX

An equality constraint is fixed to a numerically large value. This can cause numerical problems.

MSK_RES_WRN_LARGE_CJ

A numerically large value is specified for one c_j .

MSK_RES_WRN_LARGE_AIJ

A numerically large value is specified for an $a_{i,j}$ element in A . The parameter *MSK_DPAR_DATA_TOL_AIJ_LARGE* controls when an $a_{i,j}$ is considered large.

MSK_RES_WRN_ZERO_AIJ

One or more zero elements are specified in A .

MSK_RES_WRN_NAME_MAX_LEN

A name is longer than the buffer that is supposed to hold it.

MSK_RES_WRN_SPAR_MAX_LEN

A value for a string parameter is longer than the buffer that is supposed to hold it.

MSK_RES_WRN_MPS_SPLIT_RHS_VECTOR

An RHS vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_MPS_SPLIT_RAN_VECTOR

A RANGE vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_MPS_SPLIT_BOU_VECTOR

A BOUNDS vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_LP_OLD_QUAD_FORMAT

Missing ‘/2’ after quadratic expressions in bound or objective.

MSK_RES_WRN_LP_DROP_VARIABLE

Ignored a variable because the variable was not previously defined. Usually this implies that a variable appears in the bound section but not in the objective or the constraints.

MSK_RES_WRN_NZ_IN_UPR_TRI

Non-zero elements specified in the upper triangle of a matrix were ignored.

MSK_RES_WRN_DROPPED_NZ_QOBJ

One or more non-zero elements were dropped in the Q matrix in the objective.

MSK_RES_WRN_IGNORE_INTEGER

Ignored integer constraints.

MSK_RES_WRN_NO_GLOBAL_OPTIMIZER

No global optimizer is available.

MSK_RES_WRN_MIO_INFEASIBLE_FINAL

The final mixed-integer problem with all the integer variables fixed at their optimal values is infeasible.

MSK_RES_WRN_SOL_FILTER

Invalid solution filter is specified.

MSK_RES_WRN_UNDEF_SOL_FILE_NAME

Undefined name occurred in a solution.

MSK_RES_WRN_SOL_FILE_IGNORED_CON

One or more lines in the constraint section were ignored when reading a solution file.

MSK_RES_WRN_SOL_FILE_IGNORED_VAR

One or more lines in the variable section were ignored when reading a solution file.

MSK_RES_WRN_TOO_FEW_BASIS_VARS

An incomplete basis has been specified. Too few basis variables are specified.

MSK_RES_WRN_TOO_MANY_BASIS_VARS

A basis with too many variables has been specified.

MSK_RES_WRN_NO_NONLINEAR_FUNCTION_WRITE

The problem contains a general nonlinear function in either the objective or the constraints. Such a nonlinear function cannot be written to a disk file. Note that quadratic terms when inputted explicitly can be written to disk.

MSK_RES_WRN_LICENSE_EXPIRE

The license expires.

MSK_RES_WRN_LICENSE_SERVER

The license server is not responding.

MSK_RES_WRN_EMPTY_NAME

A variable or constraint name is empty. The output file may be invalid.

MSK_RES_WRN_USING_GENERIC_NAMES

Generic names are used because a name is not valid. For instance when writing an LP file the names must not contain blanks or start with a digit.

MSK_RES_WRN_LICENSE_FEATURE_EXPIRE

The license expires.

MSK_RES_WRN_PARAM_NAME_DOUB

The parameter name is not recognized as a double parameter.

MSK_RES_WRN_PARAM_NAME_INT

The parameter name is not recognized as an integer parameter.

MSK_RES_WRN_PARAM_NAME_STR

The parameter name is not recognized as a string parameter.

MSK_RES_WRN_PARAM_STR_VALUE

The string is not recognized as a symbolic value for the parameter.

MSK_RES_WRN_PARAM_IGNORED_CMIO

A parameter was ignored by the conic mixed integer optimizer.

MSK_RES_WRN_ZEROS_IN_SPARSE_ROW

One or more (near) zero elements are specified in a sparse row of a matrix. Since, it is redundant to specify zero elements then it may indicate an error.

MSK_RES_WRN_ZEROS_IN_SPARSE_COL

One or more (near) zero elements are specified in a sparse column of a matrix. It is redundant to specify zero elements. Hence, it may indicate an error.

MSK_RES_WRN_INCOMPLETE_LINEAR_DEPENDENCY_CHECK

The linear dependency check(s) is incomplete. Normally this is not an important warning unless the optimization problem has been formulated with linear dependencies. Linear dependencies may prevent **MOSEK** from solving the problem.

MSK_RES_WRN_ELIMINATOR_SPACE

The eliminator is skipped at least once due to lack of space.

MSK_RES_WRN_PRESOLVE_OUTOFSPACE

The presolve is incomplete due to lack of space.

MSK_RES_WRN_WRITE_CHANGED_NAMES

Some names were changed because they were invalid for the output file format.

MSK_RES_WRN_WRITE_DISCARDED_CFIX

The fixed objective term could not be converted to a variable and was discarded in the output file.

MSK_RES_WRN_CONSTRUCT_SOLUTION_INFEAS

After fixing the integer variables at the suggested values then the problem is infeasible.

MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG

The initial value for one or more of the integer variables is not feasible.

MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG

The construct solution requires an integer solution.

MSK_RES_WRN_DUPLICATE_CONSTRAINT_NAMES

Two constraint names are identical.

MSK_RES_WRN_DUPLICATE_VARIABLE_NAMES

Two variable names are identical.

MSK_RES_WRN_DUPLICATE_BARVARIABLE_NAMES

Two barvariable names are identical.

MSK_RES_WRN_DUPLICATE_CONE_NAMES

Two cone names are identical.

MSK_RES_WRN_ANA_LARGE_BOUNDS

This warning is issued by the problem analyzer, if one or more constraint or variable bounds are very large. One should consider omitting these bounds entirely by setting them to $+\text{inf}$ or $-\text{inf}$.

MSK_RES_WRN_ANA_C_ZERO

This warning is issued by the problem analyzer, if the coefficients in the linear part of the objective are all zero.

MSK_RES_WRN_ANA_EMPTY_COLS

This warning is issued by the problem analyzer, if columns, in which all coefficients are zero, are found.

MSK_RES_WRN_ANA_CLOSE_BOUNDS

This warning is issued by problem analyzer, if ranged constraints or variables with very close upper and lower bounds are detected. One should consider treating such constraints as equalities and such variables as constants.

MSK_RES_WRN_ANA_ALMOST_INT_BOUNDS

This warning is issued by the problem analyzer if a constraint is bound nearly integral.

MSK_RES_WRN_QUAD_CONES_WITH_ROOT_FIXED_AT_ZERO

For at least one quadratic cone the root is fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

MSK_RES_WRN_RQUAD_CONES_WITH_ROOT_FIXED_AT_ZERO

For at least one rotated quadratic cone at least one of the root variables are fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

MSK_RES_WRN_NO_DUALIZER

No automatic dualizer is available for the specified problem. The primal problem is solved.

MSK_RES_WRN_SYM_MAT_LARGE

A numerically large value is specified for an $e_{i,j}$ element in E . The parameter *MSK_DPAR_DATA_SYM_MAT_TOL_LARGE* controls when an $e_{i,j}$ is considered large.

13.3.3 Errors

MSK_RES_ERR_LICENSE

Invalid license.

MSK_RES_ERR_LICENSE_EXPIRED

The license has expired.

MSK_RES_ERR_LICENSE_VERSION

The license is valid for another version of **MOSEK**.

MSK_RES_ERR_SIZE_LICENSE

The problem is bigger than the license.

MSK_RES_ERR_PROB_LICENSE

The software is not licensed to solve the problem.

MSK_RES_ERR_FILE_LICENSE

Invalid license file.

MSK_RES_ERR_MISSING_LICENSE_FILE

MOSEK cannot license file or a token server. See the **MOSEK** installation manual for details.

MSK_RES_ERR_SIZE_LICENSE_CON

The problem has too many constraints to be solved with the available license.

MSK_RES_ERR_SIZE_LICENSE_VAR

The problem has too many variables to be solved with the available license.

MSK_RES_ERR_SIZE_LICENSE_INTVAR

The problem contains too many integer variables to be solved with the available license.

MSK_RES_ERR_OPTIMIZER_LICENSE

The optimizer required is not licensed.

MSK_RES_ERR_FLEXLM

The FLEXlm license manager reported an error.

MSK_RES_ERR_LICENSE_SERVER

The license server is not responding.

MSK_RES_ERR_LICENSE_MAX

Maximum number of licenses is reached.

MSK_RES_ERR_LICENSE_MOSEKLM_DAEMON

The MOSEKLM license manager daemon is not up and running.

MSK_RES_ERR_LICENSE_FEATURE

A requested feature is not available in the license file(s). Most likely due to an incorrect license system setup.

MSK_RES_ERR_PLATFORM_NOT_LICENSED

A requested license feature is not available for the required platform.

MSK_RES_ERR_LICENSE_CANNOT_ALLOCATE

The license system cannot allocate the memory required.

MSK_RES_ERR_LICENSE_CANNOT_CONNECT

MOSEK cannot connect to the license server. Most likely the license server is not up and running.

MSK_RES_ERR_LICENSE_INVALID_HOSTID

The host ID specified in the license file does not match the host ID of the computer.

MSK_RES_ERR_LICENSE_SERVER_VERSION

The version specified in the checkout request is greater than the highest version number the daemon supports.

MSK_RES_ERR_LICENSE_NO_SERVER_SUPPORT

The license server does not support the requested feature. Possible reasons for this error include:

- The feature has expired.
- The feature's start date is later than today's date.
- The version requested is higher than feature's the highest supported version.
- A corrupted license file.

Try restarting the license and inspect the license server debug file, usually called `lmgrd.log`.

MSK_RES_ERR_LICENSE_NO_SERVER_LINE

There is no **SERVER** line in the license file. All non-zero license count features need at least one **SERVER** line.

MSK_RES_ERR_OPEN_DL

A dynamic link library could not be opened.

MSK_RES_ERR_OLDER_DLL

The dynamic link library is older than the specified version.

MSK_RES_ERR_NEWER_DLL

The dynamic link library is newer than the specified version.

MSK_RES_ERR_LINK_FILE_DLL

A file cannot be linked to a stream in the DLL version.

MSK_RES_ERR_THREAD_MUTEX_INIT

Could not initialize a mutex.

MSK_RES_ERR_THREAD_MUTEX_LOCK

Could not lock a mutex.

MSK_RES_ERR_THREAD_MUTEX_UNLOCK

Could not unlock a mutex.

MSK_RES_ERR_THREAD_CREATE

Could not create a thread. This error may occur if a large number of environments are created and not deleted again. In any case it is a good practice to minimize the number of environments created.

MSK_RES_ERR_THREAD_COND_INIT

Could not initialize a condition.

MSK_RES_ERR_UNKNOWN

Unknown error.

MSK_RES_ERR_SPACE

Out of space.

MSK_RES_ERR_FILE_OPEN

Error while opening a file.

MSK_RES_ERR_FILE_READ

File read error.

MSK_RES_ERR_FILE_WRITE

File write error.

MSK_RES_ERR_DATA_FILE_EXT

The data file format cannot be determined from the file name.

MSK_RES_ERR_INVALID_FILE_NAME

An invalid file name has been specified.

MSK_RES_ERR_INVALID_SOL_FILE_NAME

An invalid file name has been specified.

MSK_RES_ERR_END_OF_FILE

End of file reached.

MSK_RES_ERR_NULL_ENV

`env` is a NULL pointer.

MSK_RES_ERR_NULL_TASK

`task` is a NULL pointer.

MSK_RES_ERR_INVALID_STREAM

An invalid stream is referenced.

MSK_RES_ERR_NO_INIT_ENV

`env` is not initialized.

MSK_RES_ERR_INVALID_TASK

The `task` is invalid.

MSK_RES_ERR_NULL_POINTER

An argument to a function is unexpectedly a NULL pointer.

MSK_RES_ERR_LIVING_TASKS

All tasks associated with an environment must be deleted before the environment is deleted. There are still some undeleted tasks.

MSK_RES_ERR_BLANK_NAME

An all blank name has been specified.

MSK_RES_ERR_DUP_NAME

The same name was used multiple times for the same problem item type.

MSK_RES_ERR_INVALID_OBJ_NAME

An invalid objective name is specified.

MSK_RES_ERR_INVALID_CON_NAME

An invalid constraint name is used.

MSK_RES_ERR_INVALID_VAR_NAME

An invalid variable name is used.

MSK_RES_ERR_INVALID_CONE_NAME

An invalid cone name is used.

MSK_RES_ERR_INVALID_BARVAR_NAME

An invalid symmetric matrix variable name is used.

MSK_RES_ERR_SPACE_LEAKING

MOSEK is leaking memory. This can be due to either an incorrect use of **MOSEK** or a bug.

MSK_RES_ERR_SPACE_NO_INFO

No available information about the space usage.

MSK_RES_ERR_READ_FORMAT

The specified format cannot be read.

MSK_RES_ERR_MPS_FILE

An error occurred while reading an MPS file.

MSK_RES_ERR_MPS_INV_FIELD

A field in the MPS file is invalid. Probably it is too wide.

MSK_RES_ERR_MPS_INV_MARKER

An invalid marker has been specified in the MPS file.

MSK_RES_ERR_MPS_NULL_CON_NAME

An empty constraint name is used in an MPS file.

MSK_RES_ERR_MPS_NULL_VAR_NAME

An empty variable name is used in an MPS file.

MSK_RES_ERR_MPS_UNDEF_CON_NAME

An undefined constraint name occurred in an MPS file.

MSK_RES_ERR_MPS_UNDEF_VAR_NAME

An undefined variable name occurred in an MPS file.

MSK_RES_ERR_MPS_INV_CON_KEY

An invalid constraint key occurred in an MPS file.

MSK_RES_ERR_MPS_INV_BOUND_KEY

An invalid bound key occurred in an MPS file.

MSK_RES_ERR_MPS_INV_SEC_NAME

An invalid section name occurred in an MPS file.

MSK_RES_ERR_MPS_NO_OBJECTIVE

No objective is defined in an MPS file.

MSK_RES_ERR_MPS_SPLITTED_VAR

All elements in a column of the A matrix must be specified consecutively. Hence, it is illegal to specify non-zero elements in A for variable 1, then for variable 2 and then variable 1 again.

MSK_RES_ERR_MPS_MUL_CON_NAME

A constraint name was specified multiple times in the **ROWS** section.

MSK_RES_ERR_MPS_MUL_QSEC

Multiple **QSECTION**s are specified for a constraint in the MPS data file.

MSK_RES_ERR_MPS_MUL_QOBJ

The **Q** term in the objective is specified multiple times in the MPS data file.

MSK_RES_ERR_MPS_INV_SEC_ORDER

The sections in the MPS data file are not in the correct order.

MSK_RES_ERR_MPS_MUL_CSEC

Multiple **CSECTION**s are given the same name.

MSK_RES_ERR_MPS_CONE_TYPE

Invalid cone type specified in a **CSECTION**.

MSK_RES_ERR_MPS_CONE_OVERLAP

A variable is specified to be a member of several cones.

MSK_RES_ERR_MPS_CONE_REPEAT

A variable is repeated within the **CSECTION**.

MSK_RES_ERR_MPS_NON_SYMMETRIC_Q

A non symmetric matrix has been specified.

MSK_RES_ERR_MPS_DUPLICATE_Q_ELEMENT

Duplicate elements is specified in a Q matrix.

MSK_RES_ERR_MPS_INVALID_OBJSENSE

An invalid objective sense is specified.

MSK_RES_ERR_MPS_TAB_IN_FIELD2

A tab char occurred in field 2.

MSK_RES_ERR_MPS_TAB_IN_FIELD3

A tab char occurred in field 3.

MSK_RES_ERR_MPS_TAB_IN_FIELD5

A tab char occurred in field 5.

MSK_RES_ERR_MPS_INVALID_OBJ_NAME

An invalid objective name is specified.

MSK_RES_ERR_LP_INCOMPATIBLE

The problem cannot be written to an LP formatted file.

MSK_RES_ERR_LP_EMPTY

The problem cannot be written to an LP formatted file.

MSK_RES_ERR_LP_DUP_SLACK_NAME

The name of the slack variable added to a ranged constraint already exists.

MSK_RES_ERR_WRITE_MPS_INVALID_NAME

An invalid name is created while writing an MPS file. Usually this will make the MPS file unreadable.

MSK_RES_ERR_LP_INVALID_VAR_NAME

A variable name is invalid when used in an LP formatted file.

MSK_RES_ERR_LP_FREE_CONSTRAINT

Free constraints cannot be written in LP file format.

MSK_RES_ERR_WRITE_OPF_INVALID_VAR_NAME

Empty variable names cannot be written to OPF files.

MSK_RES_ERR_LP_FILE_FORMAT

Syntax error in an LP file.

MSK_RES_ERR_WRITE_LP_FORMAT

Problem cannot be written as an LP file.

MSK_RES_ERR_READ_LP_MISSING_END_TAG

Syntax error in LP file. Possibly missing End tag.

MSK_RES_ERR_LP_FORMAT

Syntax error in an LP file.

MSK_RES_ERR_WRITE_LP_NON_UNIQUE_NAME

An auto-generated name is not unique.

MSK_RES_ERR_READ_LP_NONEXISTING_NAME

A variable never occurred in objective or constraints.

MSK_RES_ERR_LP_WRITE_CONIC_PROBLEM

The problem contains cones that cannot be written to an LP formatted file.

MSK_RES_ERR_LP_WRITE_GECO_PROBLEM

The problem contains general convex terms that cannot be written to an LP formatted file.

MSK_RES_ERR_WRITING_FILE

An error occurred while writing file

MSK_RES_ERR_OPF_FORMAT

Syntax error in an OPF file

MSK_RES_ERR_OPF_NEW_VARIABLE

Introducing new variables is now allowed. When a [variables] section is present, it is not allowed to introduce new variables later in the problem.

MSK_RES_ERR_INVALID_NAME_IN_SOL_FILE

An invalid name occurred in a solution file.

MSK_RES_ERR_LP_INVALID_CON_NAME

A constraint name is invalid when used in an LP formatted file.

MSK_RES_ERR_OPF_PREMATURE_EOF

Premature end of file in an OPF file.

MSK_RES_ERR_JSON_SYNTAX

Syntax error in an JSON data

MSK_RES_ERR_JSON_STRING

Error in JSON string.

MSK_RES_ERR_JSON_NUMBER_OVERFLOW

Invalid number entry - wrong type or value overflow.

MSK_RES_ERR_JSON_FORMAT

Error in an JSON Task file

MSK_RES_ERR_JSON_DATA

Inconsistent data in JSON Task file

MSK_RES_ERR_JSON_MISSING_DATA

Missing data section in JSON task file.

MSK_RES_ERR_ARGUMENT_LENNEQ

Incorrect length of arguments.

MSK_RES_ERR_ARGUMENT_TYPE

Incorrect argument type.

MSK_RES_ERR_NR_ARGUMENTS

Incorrect number of function arguments.

MSK_RES_ERR_IN_ARGUMENT

A function argument is incorrect.

MSK_RES_ERR_ARGUMENT_DIMENSION

A function argument is of incorrect dimension.

MSK_RES_ERR_INDEX_IS_TOO_SMALL

An index in an argument is too small.

MSK_RES_ERR_INDEX_IS_TOO_LARGE

An index in an argument is too large.

MSK_RES_ERR_PARAM_NAME

The parameter name is not correct.

MSK_RES_ERR_PARAM_NAME_DOUB

The parameter name is not correct for a double parameter.

MSK_RES_ERR_PARAM_NAME_INT

The parameter name is not correct for an integer parameter.

MSK_RES_ERR_PARAM_NAME_STR

The parameter name is not correct for a string parameter.

MSK_RES_ERR_PARAM_INDEX

Parameter index is out of range.

MSK_RES_ERR_PARAM_IS_TOO_LARGE

The parameter value is too large.

MSK_RES_ERR_PARAM_IS_TOO_SMALL

The parameter value is too small.

MSK_RES_ERR_PARAM_VALUE_STR

The parameter value string is incorrect.

MSK_RES_ERR_PARAM_TYPE

The parameter type is invalid.

MSK_RES_ERR_INF_DOU_INDEX

A double information index is out of range for the specified type.

MSK_RES_ERR_INF_INT_INDEX

An integer information index is out of range for the specified type.

MSK_RES_ERR_INDEX_ARR_IS_TOO_SMALL

An index in an array argument is too small.

MSK_RES_ERR_INDEX_ARR_IS_TOO_LARGE

An index in an array argument is too large.

MSK_RES_ERR_INF_LINT_INDEX

A long integer information index is out of range for the specified type.

MSK_RES_ERR_ARG_IS_TOO_SMALL

The value of a argument is too small.

MSK_RES_ERR_ARG_IS_TOO_LARGE

The value of a argument is too small.

MSK_RES_ERR_INVALID_WHICHSOL

whichsol is invalid.

MSK_RES_ERR_INF_DOU_NAME

A double information name is invalid.

MSK_RES_ERR_INF_INT_NAME

An integer information name is invalid.

MSK_RES_ERR_INF_TYPE

The information type is invalid.

MSK_RES_ERR_INF_LINT_NAME

A long integer information name is invalid.

MSK_RES_ERR_INDEX

An index is out of range.

MSK_RES_ERR_WHICHSOL

The solution defined by *whichsol* does not exists.

MSK_RES_ERR_SOLITEM

The solution item number *solitem* is invalid. Please note that *MSK_SOL_ITEM_SNX* is invalid for the basic solution.

MSK_RES_ERR_WHICHITEM_NOT_ALLOWED

whichitem is unacceptable.

MSK_RES_ERR_MAXNUMCON

The maximum number of constraints specified is smaller than the number of constraints in the task.

MSK_RES_ERR_MAXNUMVAR

The maximum number of variables specified is smaller than the number of variables in the task.

MSK_RES_ERR_MAXNUMBARVAR

The maximum number of semidefinite variables specified is smaller than the number of semidefinite variables in the task.

MSK_RES_ERR_MAXNUMQNZ

The maximum number of non-zeros specified for the Q matrices is smaller than the number of non-zeros in the current Q matrices.

MSK_RES_ERR_TOO_SMALL_MAX_NUM_NZ

The maximum number of non-zeros specified is too small.

MSK_RES_ERR_INVALID_IDX

A specified index is invalid.

MSK_RES_ERR_INVALID_MAX_NUM

A specified index is invalid.

MSK_RES_ERR_NUMCONLIM

Maximum number of constraints limit is exceeded.

MSK_RES_ERR_NUMVARLIM

Maximum number of variables limit is exceeded.

MSK_RES_ERR_TOO_SMALL_MAXNUMANZ

The maximum number of non-zeros specified for A is smaller than the number of non-zeros in the current A .

MSK_RES_ERR_INV_APTRE

`aptre[j]` is strictly smaller than `aptrb[j]` for some j .

MSK_RES_ERR_MUL_A_ELEMENT

An element in A is defined multiple times.

MSK_RES_ERR_INV_BK

Invalid bound key.

MSK_RES_ERR_INV_BKC

Invalid bound key is specified for a constraint.

MSK_RES_ERR_INV_BKX

An invalid bound key is specified for a variable.

MSK_RES_ERR_INV_VAR_TYPE

An invalid variable type is specified for a variable.

MSK_RES_ERR_SOLVER_PROBTYPE

Problem type does not match the chosen optimizer.

MSK_RES_ERR_OBJECTIVE_RANGE

Empty objective range.

MSK_RES_ERR_FIRST

Invalid `first`.

MSK_RES_ERR_LAST

Invalid index `last`. A given index was out of expected range.

MSK_RES_ERR_NEGATIVE_SURPLUS

Negative surplus.

MSK_RES_ERR_NEGATIVE_APPEND

Cannot append a negative number.

MSK_RES_ERR_UNDEF_SOLUTION

MOSEK has the following solution types:

- an interior-point solution,
- an basic solution,
- and an integer solution.

Each optimizer may set one or more of these solutions; e.g by default a successful optimization with the interior-point optimizer defines the interior-point solution, and, for linear problems, also the basic solution. This error occurs when asking for a solution or for information about a solution that is not defined.

MSK_RES_ERR_BASIS

An invalid basis is specified. Either too many or too few basis variables are specified.

MSK_RES_ERR_INV_SKC

Invalid value in `skc`.

MSK_RES_ERR_INV_SKX

Invalid value in `skx`.

MSK_RES_ERR_INV_SKN

Invalid value in `skn`.

MSK_RES_ERR_INV_SK_STR

Invalid status key string encountered.

MSK_RES_ERR_INV_SK

Invalid status key code.

MSK_RES_ERR_INV_CONE_TYPE_STR

Invalid cone type string encountered.

MSK_RES_ERR_INV_CONE_TYPE

Invalid cone type code is encountered.

MSK_RES_ERR_INVALID_SURPLUS

Invalid surplus.

MSK_RES_ERR_INV_NAME_ITEM

An invalid name item code is used.

MSK_RES_ERR_PRO_ITEM

An invalid problem is used.

MSK_RES_ERR_INVALID_FORMAT_TYPE

Invalid format type.

MSK_RES_ERR_FIRSTI

Invalid `firsti`.

MSK_RES_ERR_LASTI

Invalid `lasti`.

MSK_RES_ERR_FIRSTJ

Invalid `firstj`.

MSK_RES_ERR_LASTJ

Invalid `lastj`.

MSK_RES_ERR_MAX_LEN_IS_TOO_SMALL

An maximum length that is too small has been specified.

MSK_RES_ERR_NONLINEAR_EQUALITY

The model contains a nonlinear equality which defines a nonconvex set.

MSK_RES_ERR_NONCONVEX

The optimization problem is nonconvex.

MSK_RES_ERR_NONLINEAR_RANGED

Nonlinear constraints with finite lower and upper bound always define a nonconvex feasible set.

MSK_RES_ERR_CON_Q_NOT_PSD

The quadratic constraint matrix is not positive semidefinite as expected for a constraint with finite upper bound. This results in a nonconvex problem. The parameter `MSK_DPAR_CHECK_CONVEXITY_REL_TOL` can be used to relax the convexity check.

MSK_RES_ERR_CON_Q_NOT_NSD

The quadratic constraint matrix is not negative semidefinite as expected for a constraint with finite lower bound. This results in a nonconvex problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

MSK_RES_ERR_OBJ_Q_NOT_PSD

The quadratic coefficient matrix in the objective is not positive semidefinite as expected for a minimization problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

MSK_RES_ERR_OBJ_Q_NOT_NSD

The quadratic coefficient matrix in the objective is not negative semidefinite as expected for a maximization problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

MSK_RES_ERR_ARGUMENT_PERM_ARRAY

An invalid permutation array is specified.

MSK_RES_ERR_CONE_INDEX

An index of a non-existing cone has been specified.

MSK_RES_ERR_CONE_SIZE

A cone with too few members is specified.

MSK_RES_ERR_CONE_OVERLAP

One or more of the variables in the cone to be added is already member of another cone. Now assume the variable is x_j then add a new variable say x_k and the constraint

$$x_j = x_k$$

and then let x_k be member of the cone to be appended.

MSK_RES_ERR_CONE_REP_VAR

A variable is included multiple times in the cone.

MSK_RES_ERR_MAXNUMCONE

The value specified for `maxnumcone` is too small.

MSK_RES_ERR_CONE_TYPE

Invalid cone type specified.

MSK_RES_ERR_CONE_TYPE_STR

Invalid cone type specified.

MSK_RES_ERR_CONE_OVERLAP_APPEND

The cone to be appended has one variable which is already member of another cone.

MSK_RES_ERR_REMOVE_CONE_VARIABLE

A variable cannot be removed because it will make a cone invalid.

MSK_RES_ERR_SOL_FILE_INVALID_NUMBER

An invalid number is specified in a solution file.

MSK_RES_ERR_HUGE_C

A huge value in absolute size is specified for one c_j .

MSK_RES_ERR_HUGE_AIJ

A numerically huge value is specified for an $a_{i,j}$ element in A . The parameter *MSK_DPAR_DATA_TOL_AIJ_HUGE* controls when an $a_{i,j}$ is considered huge.

MSK_RES_ERR_DUPLICATE_AIJ

An element in the A matrix is specified twice.

MSK_RES_ERR_LOWER_BOUND_IS_A_NAN

The lower bound specified is not a number (nan).

MSK_RES_ERR_UPPER_BOUND_IS_A_NAN

The upper bound specified is not a number (nan).

MSK_RES_ERR_INFINITY_BOUND

A numerically huge bound value is specified.

MSK_RES_ERR_INV_QOBJ_SUBI

Invalid value in qosubi.

MSK_RES_ERR_INV_QOBJ_SUBJ

Invalid value in qosubj.

MSK_RES_ERR_INV_QOBJ_VAL

Invalid value in qoval.

MSK_RES_ERR_INV_QCON_SUBK

Invalid value in qcsbk.

MSK_RES_ERR_INV_QCON_SUBI

Invalid value in qcsubi.

MSK_RES_ERR_INV_QCON_SUBJ

Invalid value in qcsubj.

MSK_RES_ERR_INV_QCON_VAL

Invalid value in qcval.

MSK_RES_ERR_QCON_SUBI_TOO_SMALL

Invalid value in qcsubi.

MSK_RES_ERR_QCON_SUBI_TOO_LARGE

Invalid value in qcsubi.

MSK_RES_ERR_QOBJ_UPPER_TRIANGLE

An element in the upper triangle of Q^o is specified. Only elements in the lower triangle should be specified.

MSK_RES_ERR_QCON_UPPER_TRIANGLE

An element in the upper triangle of a Q^k is specified. Only elements in the lower triangle should be specified.

MSK_RES_ERR_FIXED_BOUND_VALUES

A fixed constraint/variable has been specified using the bound keys but the numerical value of the lower and upper bound is different.

MSK_RES_ERR_NONLINEAR_FUNCTIONS_NOT_ALLOWED

An operation that is invalid for problems with nonlinear functions defined has been attempted.

MSK_RES_ERR_USER_FUNC_RET

An user function reported an error.

MSK_RES_ERR_USER_FUNC_RET_DATA

An user function returned invalid data.

MSK_RES_ERR_USER_NLO_FUNC

The user-defined nonlinear function reported an error.

MSK_RES_ERR_USER_NLO_EVAL

The user-defined nonlinear function reported an error.

MSK_RES_ERR_USER_NLO_EVAL_HESSUBI

The user-defined nonlinear function reported an invalid subscript in the Hessian.

MSK_RES_ERR_USER_NLO_EVAL_HESSUBJ

The user-defined nonlinear function reported an invalid subscript in the Hessian.

MSK_RES_ERR_INVALID_OBJECTIVE_SENSE

An invalid objective sense is specified.

MSK_RES_ERR_UNDEFINED_OBJECTIVE_SENSE

The objective sense has not been specified before the optimization.

MSK_RES_ERR_Y_IS_UNDEFINED

The solution item y is undefined.

MSK_RES_ERR_NAN_IN_DOUBLE_DATA

An invalid floating point value was used in some double data.

MSK_RES_ERR_NAN_IN_BLC

l^c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BUC

u^c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_C

c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BLX

l^x contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BUX

u^x contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_INVALID_AIJ

$a_{i,j}$ contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK_RES_ERR_SYM_MAT_INVALID

A symmetric matrix contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK_RES_ERR_SYM_MAT_HUGE

A symmetric matrix contains a huge value in absolute size. The parameter `MSK_DPAR_DATA_SYM_MAT_TOL_HUGE` controls when an $e_{i,j}$ is considered huge.

MSK_RES_ERR_INV_PROBLEM

Invalid problem type. Probably a nonconvex problem has been specified.

MSK_RES_ERR_MIXED_CONIC_AND_NL

The problem contains nonlinear terms conic constraints. The requested operation cannot be applied to this type of problem.

MSK_RES_ERR_GLOBAL_INV_CONIC_PROBLEM

The global optimizer can only be applied to problems without semidefinite variables.

MSK_RES_ERR_INV_OPTIMIZER

An invalid optimizer has been chosen for the problem. This means that the simplex or the conic optimizer is chosen to optimize a nonlinear problem.

MSK_RES_ERR_MIO_NO_OPTIMIZER

No optimizer is available for the current class of integer optimization problems.

MSK_RES_ERR_NO_OPTIMIZER_VAR_TYPE

No optimizer is available for this class of optimization problems.

MSK_RES_ERR_FINAL_SOLUTION

An error occurred during the solution finalization.

MSK_RES_ERR_POSTSOLVE

An error occurred during the postsolve. Please contact **MOSEK** support.

MSK_RES_ERR_OVERFLOW

A computation produced an overflow i.e. a very large number.

MSK_RES_ERR_NO_BASIS_SOL

No basic solution is defined.

MSK_RES_ERR_BASIS_FACTOR

The factorization of the basis is invalid.

MSK_RES_ERR_BASIS_SINGULAR

The basis is singular and hence cannot be factored.

MSK_RES_ERR_FACTOR

An error occurred while factorizing a matrix.

MSK_RES_ERR_FEASREPAIR_CANNOT_RELAX

An optimization problem cannot be relaxed. This is the case e.g. for general nonlinear optimization problems.

MSK_RES_ERR_FEASREPAIR_SOLVING_RELAXED

The relaxed problem could not be solved to optimality. Please consult the log file for further details.

MSK_RES_ERR_FEASREPAIR_INCONSISTENT_BOUND

The upper bound is less than the lower bound for a variable or a constraint. Please correct this before running the feasibility repair.

MSK_RES_ERR_REPAIR_INVALID_PROBLEM

The feasibility repair does not support the specified problem type.

MSK_RES_ERR_REPAIR_OPTIMIZATION_FAILED

Computation the optimal relaxation failed. The cause may have been numerical problems.

MSK_RES_ERR_NAME_MAX_LEN

A name is longer than the buffer that is supposed to hold it.

MSK_RES_ERR_NAME_IS_NULL

The name buffer is a NULL pointer.

MSK_RES_ERR_INVALID_COMPRESSION

Invalid compression type.

MSK_RES_ERR_INVALID_IOMODE

Invalid io mode.

MSK_RES_ERR_NO_PRIMAL_INFEAS_CER

A certificate of primal infeasibility is not available.

MSK_RES_ERR_NO_DUAL_INFEAS_CER

A certificate of infeasibility is not available.

MSK_RES_ERR_NO_SOLUTION_IN_CALLBACK

The required solution is not available.

MSK_RES_ERR_INV_MARKI

Invalid value in marki.

MSK_RES_ERR_INV_MARKJ

Invalid value in markj.

MSK_RES_ERR_INV_NUMI

Invalid numi.

MSK_RES_ERR_INV_NUMJ

Invalid numj.

MSK_RES_ERR_CANNOT_CLONE_NL

A task with a nonlinear function callback cannot be cloned.

MSK_RES_ERR_CANNOT_HANDLE_NL

A function cannot handle a task with nonlinear function callbacks.

MSK_RES_ERR_INVALID_ACCMODE

An invalid access mode is specified.

MSK_RES_ERR_TASK_INCOMPATIBLE

The Task file is incompatible with this platform. This results from reading a file on a 32 bit platform generated on a 64 bit platform.

MSK_RES_ERR_TASK_INVALID

The Task file is invalid.

MSK_RES_ERR_TASK_WRITE

Failed to write the task file.

MSK_RES_ERR_LU_MAX_NUM_TRIES

Could not compute the LU factors of the matrix within the maximum number of allowed tries.

MSK_RES_ERR_INVALID_UTF8

An invalid UTF8 string is encountered.

MSK_RES_ERR_INVALID_WCHAR

An invalid `wchar` string is encountered.

MSK_RES_ERR_NO_DUAL_FOR_ITG_SOL

No dual information is available for the integer solution.

MSK_RES_ERR_NO_SNX_FOR_BAS_SOL

s_n^x is not available for the basis solution.

MSK_RES_ERR_INTERNAL

An internal error occurred. Please report this problem.

MSK_RES_ERR_API_ARRAY_TOO_SMALL

An input array was too short.

MSK_RES_ERR_API_CB_CONNECT

Failed to connect a callback object.

MSK_RES_ERR_API_FATAL_ERROR

An internal error occurred in the API. Please report this problem.

MSK_RES_ERR_API_INTERNAL

An internal fatal error occurred in an interface function.

MSK_RES_ERR_SEN_FORMAT

Syntax error in sensitivity analysis file.

MSK_RES_ERR_SEN_UNDEF_NAME

An undefined name was encountered in the sensitivity analysis file.

MSK_RES_ERR_SEN_INDEX_RANGE

Index out of range in the sensitivity analysis file.

MSK_RES_ERR_SEN_BOUND_INVALID_UP

Analysis of upper bound requested for an index, where no upper bound exists.

MSK_RES_ERR_SEN_BOUND_INVALID_LO

Analysis of lower bound requested for an index, where no lower bound exists.

MSK_RES_ERR_SEN_INDEX_INVALID

Invalid range given in the sensitivity file.

MSK_RES_ERR_SEN_INVALID_REGEX

Syntax error in regexp or regexp longer than 1024.

MSK_RES_ERR_SEN_SOLUTION_STATUS

No optimal solution found to the original problem given for sensitivity analysis.

MSK_RES_ERR_SEN_NUMERICAL

Numerical difficulties encountered performing the sensitivity analysis.

MSK_RES_ERR_SEN_UNHANDLED_PROBLEM_TYPE

Sensitivity analysis cannot be performed for the specified problem. Sensitivity analysis is only possible for linear problems.

MSK_RES_ERR_UNB_STEP_SIZE

A step size in an optimizer was unexpectedly unbounded. For instance, if the step-size becomes unbounded in phase 1 of the simplex algorithm then an error occurs. Normally this will happen only if the problem is badly formulated. Please contact **MOSEK** support if this error occurs.

MSK_RES_ERR_IDENTICAL_TASKS

Some tasks related to this function call were identical. Unique tasks were expected.

MSK_RES_ERR_AD_INVALID_CODELIST

The code list data was invalid.

MSK_RES_ERR_INTERNAL_TEST_FAILED

An internal unit test function failed.

MSK_RES_ERR_XML_INVALID_PROBLEM_TYPE

The problem type is not supported by the XML format.

MSK_RES_ERR_INVALID_AMPL_STUB

Invalid AMPL stub.

MSK_RES_ERR_INT64_TO_INT32_CAST

An 32 bit integer could not cast to a 64 bit integer.

MSK_RES_ERR_SIZE_LICENSE_NUMCORES

The computer contains more cpu cores than the license allows for.

MSK_RES_ERR_INFEAS_UNDEFINED

The requested value is not defined for this solution type.

MSK_RES_ERR_NO_BARX_FOR_SOLUTION

There is no \bar{X} available for the solution specified. In particular note there are no \bar{X} defined for the basic and integer solutions.

MSK_RES_ERR_NO_BARS_FOR_SOLUTION

There is no \bar{s} available for the solution specified. In particular note there are no \bar{s} defined for the basic and integer solutions.

MSK_RES_ERR_BAR_VAR_DIM

The dimension of a symmetric matrix variable has to be greater than 0.

MSK_RES_ERR_SYM_MAT_INVALID_ROW_INDEX

A row index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_INVALID_COL_INDEX

A column index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_NOT_LOWER_TRINGULAR

Only the lower triangular part of sparse symmetric matrix should be specified.

MSK_RES_ERR_SYM_MAT_INVALID_VALUE

The numerical value specified in a sparse symmetric matrix is not a floating value.

MSK_RES_ERR_SYM_MAT_DUPLICATE

A value in a symmetric matrix has been specified more than once.

MSK_RES_ERR_INVALID_SYM_MAT_DIM

A sparse symmetric matrix of invalid dimension is specified.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_SYM_MAT

The file format does not support a problem with symmetric matrix variables.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_CONES

The file format does not support a problem with conic constraints.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_GENERAL_NL

The file format does not support a problem with general nonlinear terms.

MSK_RES_ERR_DUPLICATE_CONSTRAINT_NAMES

Two constraint names are identical.

MSK_RES_ERR_DUPLICATE_VARIABLE_NAMES

Two variable names are identical.

MSK_RES_ERR_DUPLICATE_BARVARIABLE_NAMES

Two barvariable names are identical.

MSK_RES_ERR_DUPLICATE_CONE_NAMES

Two cone names are identical.

MSK_RES_ERR_NON_UNIQUE_ARRAY

An array does not contain unique elements.

MSK_RES_ERR_ARGUMENT_IS_TOO_LARGE

The value of a function argument is too large.

MSK_RES_ERR_MIO_INTERNAL

A fatal error occurred in the mixed integer optimizer. Please contact **MOSEK** support.

MSK_RES_ERR_INVALID_PROBLEM_TYPE

An invalid problem type.

MSK_RES_ERR_UNHANDLED_SOLUTION_STATUS

Unhandled solution status.

MSK_RES_ERR_UPPER_TRIANGLE

An element in the upper triangle of a lower triangular matrix is specified.

MSK_RES_ERR_LAU_SINGULAR_MATRIX

A matrix is singular.

MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE

A matrix is not positive definite.

MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX

An invalid lower triangular matrix.

MSK_RES_ERR_LAU_UNKNOWN

An unknown error.

MSK_RES_ERR_LAU_ARG_M

Invalid argument m.

MSK_RES_ERR_LAU_ARG_N

Invalid argument n.

MSK_RES_ERR_LAU_ARG_K

Invalid argument k.

MSK_RES_ERR_LAU_ARG_TRANSA

Invalid argument transa.

MSK_RES_ERR_LAU_ARG_TRANSB

Invalid argument transb.

MSK_RES_ERR_LAU_ARG_UPLO

Invalid argument uplo.

MSK_RES_ERR_LAU_ARG_TRANS

Invalid argument trans.

MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX

An invalid sparse symmetric matrix is specified. Note only the lower triangular part with no duplicates is specified.

MSK_RES_ERR_CBF_PARSE

An error occurred while parsing an CBF file.

MSK_RES_ERR_CBF_OBJ_SENSE

An invalid objective sense is specified.

MSK_RES_ERR_CBF_NO_VARIABLES

No variables are specified.

MSK_RES_ERR_CBF_TOO_MANY_CONSTRAINTS
Too many constraints specified.

MSK_RES_ERR_CBF_TOO_MANY_VARIABLES
Too many variables specified.

MSK_RES_ERR_CBF_NO_VERSION_SPECIFIED
No version specified.

MSK_RES_ERR_CBF_SYNTAX
Invalid syntax.

MSK_RES_ERR_CBF_DUPLICATE_OBJ
Duplicate OBJ keyword.

MSK_RES_ERR_CBF_DUPLICATE_CON
Duplicate CON keyword.

MSK_RES_ERR_CBF_DUPLICATE_VAR
Duplicate VAR keyword.

MSK_RES_ERR_CBF_DUPLICATE_INT
Duplicate INT keyword.

MSK_RES_ERR_CBF_INVALID_VAR_TYPE
Invalid variable type.

MSK_RES_ERR_CBF_INVALID_CON_TYPE
Invalid constraint type.

MSK_RES_ERR_CBF_INVALID_DOMAIN_DIMENSION
Invalid domain dimension.

MSK_RES_ERR_CBF_DUPLICATE_OBJCOORD
Duplicate index in OBJCOORD.

MSK_RES_ERR_CBF_DUPLICATE_BCOORD
Duplicate index in BCOORD.

MSK_RES_ERR_CBF_DUPLICATE_ACOORD
Duplicate index in ACOORD.

MSK_RES_ERR_CBF_TOO_FEW_VARIABLES
Too few variables defined.

MSK_RES_ERR_CBF_TOO_FEW_CONSTRAINTS
Too few constraints defined.

MSK_RES_ERR_CBF_TOO_FEW_INTS
Too few ints are specified.

MSK_RES_ERR_CBF_TOO_MANY_INTS
Too many ints are specified.

MSK_RES_ERR_CBF_INVALID_INT_INDEX
Invalid INT index.

MSK_RES_ERR_CBF_UNSUPPORTED
Unsupported feature is present.

MSK_RES_ERR_CBF_DUPLICATE_PSDVAR
Duplicate PSDVAR keyword.

MSK_RES_ERR_CBF_INVALID_PSDVAR_DIMENSION
Invalid PSDVAR dimension.

MSK_RES_ERR_CBF_TOO_FEW_PSDVAR
Too few variables defined.

MSK_RES_ERR_MIO_INVALID_ROOT_OPTIMIZER

An invalid root optimizer was selected for the problem type.

MSK_RES_ERR_MIO_INVALID_NODE_OPTIMIZER

An invalid node optimizer was selected for the problem type.

MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD

The matrix defining the quadratic part of constraint is not positive semidefinite.

MSK_RES_ERR_TOCONIC_CONSTRAINT_FX

The quadratic constraint is an equality, thus not convex.

MSK_RES_ERR_TOCONIC_CONSTRAINT_RA

The quadratic constraint has finite lower and upper bound, and therefore it is not convex.

MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC

The constraint is not conic representable.

MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD

The matrix defining the quadratic part of the objective function is not positive semidefinite.

MSK_RES_ERR_SERVER_CONNECT

Failed to connect to remote solver server. The server string or the port string were invalid, or the server did not accept connection.

MSK_RES_ERR_SERVER_PROTOCOL

Unexpected message or data from solver server.

MSK_RES_ERR_SERVER_STATUS

Server returned non-ok HTTP status code

MSK_RES_ERR_SERVER_TOKEN

The job ID specified is incorrect or invalid

13.4 Constants

13.4.1 Language selection constants

MSK_LANG_ENG

English language selection

MSK_LANG_DAN

Danish language selection

13.4.2 Constraint or variable access modes. All functions using this enum are deprecated. Use separate functions for rows/columns instead.

MSK_ACC_VAR

Access data by columns (variable oriented)

MSK_ACC_CON

Access data by rows (constraint oriented)

13.4.3 Basis identification

MSK_BI_NEVER

Never do basis identification.

MSK_BI_ALWAYS

Basis identification is always performed even if the interior-point optimizer terminates abnormally.

MSK_BI_NO_ERROR

Basis identification is performed if the interior-point optimizer terminates without an error.

MSK_BI_IF_FEASIBLE

Basis identification is not performed if the interior-point optimizer terminates with a problem status saying that the problem is primal or dual infeasible.

MSK_BI_RESERVED

Not currently in use.

13.4.4 Bound keys

MSK_BK_LO

The constraint or variable has a finite lower bound and an infinite upper bound.

MSK_BK_UP

The constraint or variable has an infinite lower bound and a finite upper bound.

MSK_BK_FX

The constraint or variable is fixed.

MSK_BK_FR

The constraint or variable is free.

MSK_BK_RA

The constraint or variable is ranged.

13.4.5 Mark

MSK_MARK_LO

The lower bound is selected for sensitivity analysis.

MSK_MARK_UP

The upper bound is selected for sensitivity analysis.

13.4.6 Degeneracy strategies

MSK_SIM_DEGEN_NONE

The simplex optimizer should use no degeneration strategy.

MSK_SIM_DEGEN_FREE

The simplex optimizer chooses the degeneration strategy.

MSK_SIM_DEGEN_AGGRESSIVE

The simplex optimizer should use an aggressive degeneration strategy.

MSK_SIM_DEGEN_MODERATE

The simplex optimizer should use a moderate degeneration strategy.

MSK_SIM_DEGEN_MINIMUM

The simplex optimizer should use a minimum degeneration strategy.

13.4.7 Transposed matrix.

MSK_TRANSPOSE_NO

No transpose is applied.

MSK_TRANSPOSE_YES

A transpose is applied.

13.4.8 Triangular part of a symmetric matrix.

MSK_UPLO_LO
Lower part.

MSK_UPLO_UP
Upper part

13.4.9 Problem reformulation.

MSK_SIM_REFORMULATION_ON
Allow the simplex optimizer to reformulate the problem.

MSK_SIM_REFORMULATION_OFF
Disallow the simplex optimizer to reformulate the problem.

MSK_SIM_REFORMULATION_FREE
The simplex optimizer can choose freely.

MSK_SIM_REFORMULATION_AGGRESSIVE
The simplex optimizer should use an aggressive reformulation strategy.

13.4.10 Exploit duplicate columns.

MSK_SIM_EXPLOIT_DUPVEC_ON
Allow the simplex optimizer to exploit duplicated columns.

MSK_SIM_EXPLOIT_DUPVEC_OFF
Disallow the simplex optimizer to exploit duplicated columns.

MSK_SIM_EXPLOIT_DUPVEC_FREE
The simplex optimizer can choose freely.

13.4.11 Hot-start type employed by the simplex optimizer

MSK_SIM_HOTSTART_NONE
The simplex optimizer performs a coldstart.

MSK_SIM_HOTSTART_FREE
The simplex optimizer chooses the hot-start type.

MSK_SIM_HOTSTART_STATUS_KEYS
Only the status keys of the constraints and variables are used to choose the type of hot-start.

13.4.12 Hot-start type employed by the interior-point optimizers.

MSK_INTPNT_HOTSTART_NONE
The interior-point optimizer performs a coldstart.

MSK_INTPNT_HOTSTART_PRIMAL
The interior-point optimizer exploits the primal solution only.

MSK_INTPNT_HOTSTART_DUAL
The interior-point optimizer exploits the dual solution only.

MSK_INTPNT_HOTSTART_PRIMAL_DUAL
The interior-point optimizer exploits both the primal and dual solution.

13.4.13 Progress callback codes

`MSK_CALLBACK_BEGIN_BI`

The basis identification procedure has been started.

`MSK_CALLBACK_BEGIN_CONIC`

The callback function is called when the conic optimizer is started.

`MSK_CALLBACK_BEGIN_DUAL_BI`

The callback function is called from within the basis identification procedure when the dual phase is started.

`MSK_CALLBACK_BEGIN_DUAL_SENSITIVITY`

Dual sensitivity analysis is started.

`MSK_CALLBACK_BEGIN_DUAL_SETUP_BI`

The callback function is called when the dual BI phase is started.

`MSK_CALLBACK_BEGIN_DUAL_SIMPLEX`

The callback function is called when the dual simplex optimizer started.

`MSK_CALLBACK_BEGIN_DUAL_SIMPLEX_BI`

The callback function is called from within the basis identification procedure when the dual simplex clean-up phase is started.

`MSK_CALLBACK_BEGIN_FULL_CONVEXITY_CHECK`

Begin full convexity check.

`MSK_CALLBACK_BEGIN_INFEAS_ANA`

The callback function is called when the infeasibility analyzer is started.

`MSK_CALLBACK_BEGIN_INTPNT`

The callback function is called when the interior-point optimizer is started.

`MSK_CALLBACK_BEGIN_LICENSE_WAIT`

Begin waiting for license.

`MSK_CALLBACK_BEGIN_MIO`

The callback function is called when the mixed-integer optimizer is started.

`MSK_CALLBACK_BEGIN_OPTIMIZER`

The callback function is called when the optimizer is started.

`MSK_CALLBACK_BEGIN_PRESOLVE`

The callback function is called when the presolve is started.

`MSK_CALLBACK_BEGIN_PRIMAL_BI`

The callback function is called from within the basis identification procedure when the primal phase is started.

`MSK_CALLBACK_BEGIN_PRIMAL_REPAIR`

Begin primal feasibility repair.

`MSK_CALLBACK_BEGIN_PRIMAL_SENSITIVITY`

Primal sensitivity analysis is started.

`MSK_CALLBACK_BEGIN_PRIMAL_SETUP_BI`

The callback function is called when the primal BI setup is started.

`MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX`

The callback function is called when the primal simplex optimizer is started.

`MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX_BI`

The callback function is called from within the basis identification procedure when the primal simplex clean-up phase is started.

`MSK_CALLBACK_BEGIN_QCQO_REFORMULATE`

Begin QCQO reformulation.

MSK_CALLBACK_BEGIN_READ

MOSEK has started reading a problem file.

MSK_CALLBACK_BEGIN_ROOT_CUTGEN

The callback function is called when root cut generation is started.

MSK_CALLBACK_BEGIN_SIMPLEX

The callback function is called when the simplex optimizer is started.

MSK_CALLBACK_BEGIN_SIMPLEX_BI

The callback function is called from within the basis identification procedure when the simplex clean-up phase is started.

MSK_CALLBACK_BEGIN_TO_CONIC

Begin conic reformulation.

MSK_CALLBACK_BEGIN_WRITE

MOSEK has started writing a problem file.

MSK_CALLBACK_CONIC

The callback function is called from within the conic optimizer after the information database has been updated.

MSK_CALLBACK_DUAL_SIMPLEX

The callback function is called from within the dual simplex optimizer.

MSK_CALLBACK_END_BI

The callback function is called when the basis identification procedure is terminated.

MSK_CALLBACK_END_CONIC

The callback function is called when the conic optimizer is terminated.

MSK_CALLBACK_END_DUAL_BI

The callback function is called from within the basis identification procedure when the dual phase is terminated.

MSK_CALLBACK_END_DUAL_SENSITIVITY

Dual sensitivity analysis is terminated.

MSK_CALLBACK_END_DUAL_SETUP_BI

The callback function is called when the dual BI phase is terminated.

MSK_CALLBACK_END_DUAL_SIMPLEX

The callback function is called when the dual simplex optimizer is terminated.

MSK_CALLBACK_END_DUAL_SIMPLEX_BI

The callback function is called from within the basis identification procedure when the dual clean-up phase is terminated.

MSK_CALLBACK_END_FULL_CONVEXITY_CHECK

End full convexity check.

MSK_CALLBACK_END_INFEAS_ANA

The callback function is called when the infeasibility analyzer is terminated.

MSK_CALLBACK_END_INTPNT

The callback function is called when the interior-point optimizer is terminated.

MSK_CALLBACK_END_LICENSE_WAIT

End waiting for license.

MSK_CALLBACK_END_MIO

The callback function is called when the mixed-integer optimizer is terminated.

MSK_CALLBACK_END_OPTIMIZER

The callback function is called when the optimizer is terminated.

MSK_CALLBACK_END_PRESOLVE

The callback function is called when the presolve is completed.

MSK_CALLBACK_END_PRIMAL_BI

The callback function is called from within the basis identification procedure when the primal phase is terminated.

MSK_CALLBACK_END_PRIMAL_REPAIR

End primal feasibility repair.

MSK_CALLBACK_END_PRIMAL_SENSITIVITY

Primal sensitivity analysis is terminated.

MSK_CALLBACK_END_PRIMAL_SETUP_BI

The callback function is called when the primal BI setup is terminated.

MSK_CALLBACK_END_PRIMAL_SIMPLEX

The callback function is called when the primal simplex optimizer is terminated.

MSK_CALLBACK_END_PRIMAL_SIMPLEX_BI

The callback function is called from within the basis identification procedure when the primal clean-up phase is terminated.

MSK_CALLBACK_END_QCQO_REFORMULATE

End QCQO reformulation.

MSK_CALLBACK_END_READ

MOSEK has finished reading a problem file.

MSK_CALLBACK_END_ROOT_CUTGEN

The callback function is called when root cut generation is terminated.

MSK_CALLBACK_END_SIMPLEX

The callback function is called when the simplex optimizer is terminated.

MSK_CALLBACK_END_SIMPLEX_BI

The callback function is called from within the basis identification procedure when the simplex clean-up phase is terminated.

MSK_CALLBACK_END_TO_CONIC

End conic reformulation.

MSK_CALLBACK_END_WRITE

MOSEK has finished writing a problem file.

MSK_CALLBACK_IM_BI

The callback function is called from within the basis identification procedure at an intermediate point.

MSK_CALLBACK_IM_CONIC

The callback function is called at an intermediate stage within the conic optimizer where the information database has not been updated.

MSK_CALLBACK_IM_DUAL_BI

The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

MSK_CALLBACK_IM_DUAL_SENSITIVITY

The callback function is called at an intermediate stage of the dual sensitivity analysis.

MSK_CALLBACK_IM_DUAL_SIMPLEX

The callback function is called at an intermediate point in the dual simplex optimizer.

MSK_CALLBACK_IM_FULL_CONVEXITY_CHECK

The callback function is called at an intermediate stage of the full convexity check.

MSK_CALLBACK_IM_INTPNT

The callback function is called at an intermediate stage within the interior-point optimizer where the information database has not been updated.

MSK_CALLBACK_IM_LICENSE_WAIT

MOSEK is waiting for a license.

MSK_CALLBACK_IM_LU

The callback function is called from within the LU factorization procedure at an intermediate point.

MSK_CALLBACK_IM_MIO

The callback function is called at an intermediate point in the mixed-integer optimizer.

MSK_CALLBACK_IM_MIO_DUAL_SIMPLEX

The callback function is called at an intermediate point in the mixed-integer optimizer while running the dual simplex optimizer.

MSK_CALLBACK_IM_MIO_INTPNT

The callback function is called at an intermediate point in the mixed-integer optimizer while running the interior-point optimizer.

MSK_CALLBACK_IM_MIO_PRIMAL_SIMPLEX

The callback function is called at an intermediate point in the mixed-integer optimizer while running the primal simplex optimizer.

MSK_CALLBACK_IM_ORDER

The callback function is called from within the matrix ordering procedure at an intermediate point.

MSK_CALLBACK_IM_PRESOLVE

The callback function is called from within the presolve procedure at an intermediate stage.

MSK_CALLBACK_IM_PRIMAL_BI

The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

MSK_CALLBACK_IM_PRIMAL_SENSIVITY

The callback function is called at an intermediate stage of the primal sensitivity analysis.

MSK_CALLBACK_IM_PRIMAL_SIMPLEX

The callback function is called at an intermediate point in the primal simplex optimizer.

MSK_CALLBACK_IM_QO_REFORMULATE

The callback function is called at an intermediate stage of the conic quadratic reformulation.

MSK_CALLBACK_IM_READ

Intermediate stage in reading.

MSK_CALLBACK_IM_ROOT_CUTGEN

The callback is called from within root cut generation at an intermediate stage.

MSK_CALLBACK_IM_SIMPLEX

The callback function is called from within the simplex optimizer at an intermediate point.

MSK_CALLBACK_IM_SIMPLEX_BI

The callback function is called from within the basis identification procedure at an intermediate point in the simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK_IPAR_LOG_SIM_FREQ* parameter.

MSK_CALLBACK_INTPNT

The callback function is called from within the interior-point optimizer after the information database has been updated.

MSK_CALLBACK_NEW_INT_MIO

The callback function is called after a new integer solution has been located by the mixed-integer optimizer.

MSK_CALLBACK_PRIMAL_SIMPLEX

The callback function is called from within the primal simplex optimizer.

MSK_CALLBACK_READ_OPF

The callback function is called from the OPF reader.

MSK_CALLBACK_READ_OPF_SECTION

A chunk of Q non-zeros has been read from a problem file.

MSK_CALLBACK_SOLVING_REMOTE

The callback function is called while the task is being solved on a remote server.

MSK_CALLBACK_UPDATE_DUAL_BI

The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

MSK_CALLBACK_UPDATE_DUAL_SIMPLEX

The callback function is called in the dual simplex optimizer.

MSK_CALLBACK_UPDATE_DUAL_SIMPLEX_BI

The callback function is called from within the basis identification procedure at an intermediate point in the dual simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK_IPAR_LOG_SIM_FREQ* parameter.

MSK_CALLBACK_UPDATE_PRESOLVE

The callback function is called from within the presolve procedure.

MSK_CALLBACK_UPDATE_PRIMAL_BI

The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX

The callback function is called in the primal simplex optimizer.

MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX_BI

The callback function is called from within the basis identification procedure at an intermediate point in the primal simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK_IPAR_LOG_SIM_FREQ* parameter.

MSK_CALLBACK_WRITE_OPF

The callback function is called from the OPF writer.

13.4.14 Types of convexity checks.

MSK_CHECK_CONVEXITY_NONE

No convexity check.

MSK_CHECK_CONVEXITY_SIMPLE

Perform simple and fast convexity check.

MSK_CHECK_CONVEXITY_FULL

Perform a full convexity check.

13.4.15 Compression types

MSK_COMPRESS_NONE

No compression is used.

MSK_COMPRESS_FREE

The type of compression used is chosen automatically.

MSK_COMPRESS_GZIP

The type of compression used is gzip compatible.

13.4.16 Cone types

MSK_CT_QUAD

The cone is a quadratic cone.

MSK_CT_RQUAD

The cone is a rotated quadratic cone.

13.4.17 Name types

MSK_NAME_TYPE_GEN

General names. However, no duplicate and blank names are allowed.

MSK_NAME_TYPE_MPS

MPS type names.

MSK_NAME_TYPE_LP

LP type names.

13.4.18 Cone types

MSK_SYMMAT_TYPE_SPARSE

Sparse symmetric matrix.

13.4.19 Data format types

MSK_DATA_FORMAT_EXTENSION

The file extension is used to determine the data file format.

MSK_DATA_FORMAT_MPS

The data file is MPS formatted.

MSK_DATA_FORMAT_LP

The data file is LP formatted.

MSK_DATA_FORMAT_OP

The data file is an optimization problem formatted file.

MSK_DATA_FORMAT_XML

The data file is an XML formatted file.

MSK_DATA_FORMAT_FREE_MPS

The data a free MPS formatted file.

MSK_DATA_FORMAT_TASK

Generic task dump file.

MSK_DATA_FORMAT_CB

Conic benchmark format,

MSK_DATA_FORMAT_JSON_TASK

JSON based task format.

13.4.20 Double information items

MSK_DINF_BI_CLEAN_DUAL_TIME

Time spent within the dual clean-up optimizer of the basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_PRIMAL_TIME

Time spent within the primal clean-up optimizer of the basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_TIME

Time spent within the clean-up phase of the basis identification procedure since its invocation.

MSK_DINF_BI_DUAL_TIME

Time spent within the dual phase basis identification procedure since its invocation.

MSK_DINF_BI_PRIMAL_TIME

Time spent within the primal phase of the basis identification procedure since its invocation.

MSK_DINF_BI_TIME

Time spent within the basis identification procedure since its invocation.

MSK_DINF_INTPNT_DUAL_FEAS

Dual feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure is not directly related to the original problem because a homogeneous model is employed.)

MSK_DINF_INTPNT_DUAL_OBJ

Dual objective value reported by the interior-point optimizer.

MSK_DINF_INTPNT_FACTOR_NUM_FLOPS

An estimate of the number of flops used in the factorization.

MSK_DINF_INTPNT_OPT_STATUS

A measure of optimality of the solution. It should converge to +1 if the problem has a primal-dual optimal solution, and converge to -1 if the problem is (strictly) primal or dual infeasible. If the measure converges to another constant, or fails to settle, the problem is usually ill-posed.

MSK_DINF_INTPNT_ORDER_TIME

Order time (in seconds).

MSK_DINF_INTPNT_PRIMAL_FEAS

Primal feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure is not directly related to the original problem because a homogeneous model is employed).

MSK_DINF_INTPNT_PRIMAL_OBJ

Primal objective value reported by the interior-point optimizer.

MSK_DINF_INTPNT_TIME

Time spent within the interior-point optimizer since its invocation.

MSK_DINF_MIO_CLIQUE_SEPARATION_TIME

Separation time for clique cuts.

MSK_DINF_MIO_CMIR_SEPARATION_TIME

Separation time for CMIR cuts.

MSK_DINF_MIO_CONSTRUCT_SOLUTION_OBJ

If **MOSEK** has successfully constructed an integer feasible solution, then this item contains the optimal objective value corresponding to the feasible solution.

MSK_DINF_MIO_DUAL_BOUND_AFTER_PREOLVE

Value of the dual bound after presolve but before cut generation.

MSK_DINF_MIO_GMI_SEPARATION_TIME

Separation time for GMI cuts.

MSK_DINF_MIO_HEURISTIC_TIME

Total time spent in the optimizer.

MSK_DINF_MIO IMPLIED_BOUND_TIME

Separation time for implied bound cuts.

MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME

Separation time for knapsack cover.

MSK_DINF_MIO_OBJ_ABS_GAP

Given the mixed-integer optimizer has computed a feasible solution and a bound on the optimal

objective value, then this item contains the absolute gap defined by

$$|(\text{objective value of feasible solution}) - (\text{objective bound})|.$$

Otherwise it has the value -1.0.

MSK_DINF_MIO_OBJ_BOUND

The best known bound on the objective function. This value is undefined until at least one relaxation has been solved: To see if this is the case check that *MSK_IINF_MIO_NUM_RELAX* is strictly positive.

MSK_DINF_MIO_OBJ_INT

The primal objective value corresponding to the best integer feasible solution. Please note that at least one integer feasible solution must have been located i.e. check *MSK_IINF_MIO_NUM_INT_SOLUTIONS*.

MSK_DINF_MIO_OBJ_REL_GAP

Given that the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the relative gap defined by

$$\frac{|(\text{objective value of feasible solution}) - (\text{objective bound})|}{\max(\delta, |(\text{objective value of feasible solution})|)}.$$

where δ is given by the parameter *MSK_DPAR_MIO_REL_GAP_CONST*. Otherwise it has the value -1.0.

MSK_DINF_MIO_OPTIMIZER_TIME

Total time spent in the optimizer.

MSK_DINF_MIO_PROBING_TIME

Total time for probing.

MSK_DINF_MIO_ROOT_CUTGEN_TIME

Total time for cut generation.

MSK_DINF_MIO_ROOT_OPTIMIZER_TIME

Time spent in the optimizer while solving the root relaxation.

MSK_DINF_MIO_ROOT_PRESOLVE_TIME

Time spent in while presolving the root relaxation.

MSK_DINF_MIO_TIME

Time spent in the mixed-integer optimizer.

MSK_DINF_MIO_USER_OBJ_CUT

If the objective cut is used, then this information item has the value of the cut.

MSK_DINF_OPTIMIZER_TIME

Total time spent in the optimizer since it was invoked.

MSK_DINF_PRESOLVE_ELI_TIME

Total time spent in the eliminator since the presolve was invoked.

MSK_DINF_PRESOLVE_LINDEP_TIME

Total time spent in the linear dependency checker since the presolve was invoked.

MSK_DINF_PRESOLVE_TIME

Total time (in seconds) spent in the presolve since it was invoked.

MSK_DINF_PRIMAL_REPAIR_PENALTY_OBJ

The optimal objective value of the penalty function.

MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION

Maximum absolute diagonal perturbation occurring during the QCQO reformulation.

MSK_DINF_QCQO_REFORMULATE_TIME

Time spent with conic quadratic reformulation.

MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING
Worst Cholesky column scaling.

MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING
Worst Cholesky diagonal scaling.

MSK_DINF_RD_TIME
Time spent reading the data file.

MSK_DINF_SIM_DUAL_TIME
Time spent in the dual simplex optimizer since invoking it.

MSK_DINF_SIM_FEAS
Feasibility measure reported by the simplex optimizer.

MSK_DINF_SIM_OBJ
Objective value reported by the simplex optimizer.

MSK_DINF_SIM_PRIMAL_TIME
Time spent in the primal simplex optimizer since invoking it.

MSK_DINF_SIM_TIME
Time spent in the simplex optimizer since invoking it.

MSK_DINF_SOL_BAS_DUAL_OBJ
Dual objective value of the basic solution.

MSK_DINF_SOL_BAS_DVIOLCON
Maximal dual bound violation for x^c in the basic solution.

MSK_DINF_SOL_BAS_DVIOLVAR
Maximal dual bound violation for x^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_BARX
Infinity norm of \bar{X} in the basic solution.

MSK_DINF_SOL_BAS_NRM_SLC
Infinity norm of s_l^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_SLX
Infinity norm of s_l^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_SUC
Infinity norm of s_u^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_SUX
Infinity norm of s_u^X in the basic solution.

MSK_DINF_SOL_BAS_NRM_XC
Infinity norm of x^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_XX
Infinity norm of x^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_Y
Infinity norm of y in the basic solution.

MSK_DINF_SOL_BAS_PRIMAL_OBJ
Primal objective value of the basic solution.

MSK_DINF_SOL_BAS_PVIOLCON
Maximal primal bound violation for x^c in the basic solution.

MSK_DINF_SOL_BAS_PVIOLVAR
Maximal primal bound violation for x^x in the basic solution.

MSK_DINF_SOL_ITG_NRM_BARX
Infinity norm of \bar{X} in the integer solution.

MSK_DINF_SOL_ITG_NRM_XC	Infinity norm of x^c in the integer solution.
MSK_DINF_SOL_ITG_NRM_XX	Infinity norm of x^x in the integer solution.
MSK_DINF_SOL_ITG_PRIMAL_OBJ	Primal objective value of the integer solution.
MSK_DINF_SOL_ITG_PVIOLBARVAR	Maximal primal bound violation for \bar{X} in the integer solution.
MSK_DINF_SOL_ITG_PVIOLCON	Maximal primal bound violation for x^c in the integer solution.
MSK_DINF_SOL_ITG_PVIOLCONES	Maximal primal violation for primal conic constraints in the integer solution.
MSK_DINF_SOL_ITG_PVIOLITG	Maximal violation for the integer constraints in the integer solution.
MSK_DINF_SOL_ITG_PVIOLVAR	Maximal primal bound violation for x^x in the integer solution.
MSK_DINF_SOL_ITR_DUAL_OBJ	Dual objective value of the interior-point solution.
MSK_DINF_SOL_ITR_DVIOLBARVAR	Maximal dual bound violation for \bar{X} in the interior-point solution.
MSK_DINF_SOL_ITR_DVIOLCON	Maximal dual bound violation for x^c in the interior-point solution.
MSK_DINF_SOL_ITR_DVIOLCONES	Maximal dual violation for dual conic constraints in the interior-point solution.
MSK_DINF_SOL_ITR_DVIOLVAR	Maximal dual bound violation for x^x in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_BARS	Infinity norm of \bar{S} in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_BARX	Infinity norm of \bar{X} in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_SLC	Infinity norm of s_l^c in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_SLX	Infinity norm of s_l^x in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_SNX	Infinity norm of s_n^x in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_SUC	Infinity norm of s_u^c in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_SUX	Infinity norm of s_u^X in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_XC	Infinity norm of x^c in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_XX	Infinity norm of x^x in the interior-point solution.
MSK_DINF_SOL_ITR_NRM_Y	Infinity norm of y in the interior-point solution.

MSK_DINF_SOL_ITR_PRIMAL_OBJ

Primal objective value of the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLBARVAR

Maximal primal bound violation for \bar{X} in the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLCON

Maximal primal bound violation for x^c in the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLCONES

Maximal primal violation for primal conic constraints in the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLVAR

Maximal primal bound violation for x^x in the interior-point solution.

MSK_DINF_TO_CONIC_TIME

Time spent in the last to conic reformulation.

13.4.21 License feature

MSK_FEATURE_PTS

Base system.

MSK_FEATURE_PTON

Nonlinear extension.

13.4.22 Long integer information items.

MSK_LIINF_BI_CLEAN_DUAL_DEG_ITER

Number of dual degenerate clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_DUAL_ITER

Number of dual clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_PRIMAL_DEG_ITER

Number of primal degenerate clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_PRIMAL_ITER

Number of primal clean iterations performed in the basis identification.

MSK_LIINF_BI_DUAL_ITER

Number of dual pivots performed in the basis identification.

MSK_LIINF_BI_PRIMAL_ITER

Number of primal pivots performed in the basis identification.

MSK_LIINF_INTPNT_FACTOR_NUM_NZ

Number of non-zeros in factorization.

MSK_LIINF_MIO_INTPNT_ITER

Number of interior-point iterations performed by the mixed-integer optimizer.

MSK_LIINF_MIO_PRESOLVED_ANZ

Number of non-zero entries in the constraint matrix of presolved problem.

MSK_LIINF_MIO_SIM_MAXITER_SETBACKS

Number of times the the simplex optimizer has hit the maximum iteration limit when re-optimizing.

MSK_LIINF_MIO_SIMPLEX_ITER

Number of simplex iterations performed by the mixed-integer optimizer.

MSK_LIINF_RD_NUMANZ

Number of non-zeros in A that is read.

MSK_IINF_RD_NUMQNZ
Number of Q non-zeros.

13.4.23 Integer information items.

MSK_IINF_ANA_PRO_NUM_CON
Number of constraints in the problem.

MSK_IINF_ANA_PRO_NUM_CON_EQ
Number of equality constraints.

MSK_IINF_ANA_PRO_NUM_CON_FR
Number of unbounded constraints.

MSK_IINF_ANA_PRO_NUM_CON_LO
Number of constraints with a lower bound and an infinite upper bound.

MSK_IINF_ANA_PRO_NUM_CON_RA
Number of constraints with finite lower and upper bounds.

MSK_IINF_ANA_PRO_NUM_CON_UP
Number of constraints with an upper bound and an infinite lower bound.

MSK_IINF_ANA_PRO_NUM_VAR
Number of variables in the problem.

MSK_IINF_ANA_PRO_NUM_VAR_BIN
Number of binary (0-1) variables.

MSK_IINF_ANA_PRO_NUM_VAR_CONT
Number of continuous variables.

MSK_IINF_ANA_PRO_NUM_VAR_EQ
Number of fixed variables.

MSK_IINF_ANA_PRO_NUM_VAR_FR
Number of free variables.

MSK_IINF_ANA_PRO_NUM_VAR_INT
Number of general integer variables.

MSK_IINF_ANA_PRO_NUM_VAR_LO
Number of variables with a lower bound and an infinite upper bound.

MSK_IINF_ANA_PRO_NUM_VAR_RA
Number of variables with finite lower and upper bounds.

MSK_IINF_ANA_PRO_NUM_VAR_UP
Number of variables with an upper bound and an infinite lower bound. This value is set by

MSK_IINF_INTPNT_FACTOR_DIM_DENSE
Dimension of the dense sub system in factorization.

MSK_IINF_INTPNT_ITER
Number of interior-point iterations since invoking the interior-point optimizer.

MSK_IINF_INTPNT_NUM_THREADS
Number of threads that the interior-point optimizer is using.

MSK_IINF_INTPNT_SOLVE_DUAL
Non-zero if the interior-point optimizer is solving the dual problem.

MSK_IINF_MIO_ABSGAP_SATISFIED
Non-zero if absolute gap is within tolerances.

MSK_IINF_MIO_CLIQUE_TABLE_SIZE
Size of the clique table.

MSK_IINF_MIO_CONSTRUCT_NUM_ROUNDINGS

Number of values in the integer solution that is rounded to an integer value.

MSK_IINF_MIO_CONSTRUCT_SOLUTION

If this item has the value 0, then **MOSEK** did not try to construct an initial integer feasible solution. If the item has a positive value, then **MOSEK** successfully constructed an initial integer feasible solution.

MSK_IINF_MIO_INITIAL_SOLUTION

Is non-zero if an initial integer solution is specified.

MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED

Non-zero if absolute gap is within relaxed tolerances.

MSK_IINF_MIO_NEAR_RELGAP_SATISFIED

Non-zero if relative gap is within relaxed tolerances.

MSK_IINF_MIO_NODE_DEPTH

Depth of the last node solved.

MSK_IINF_MIO_NUM_ACTIVE_NODES

Number of active branch bound nodes.

MSK_IINF_MIO_NUM_BRANCH

Number of branches performed during the optimization.

MSK_IINF_MIO_NUM_CLIQUÉ_CUTS

Number of clique cuts.

MSK_IINF_MIO_NUM_CMIR_CUTS

Number of Complemented Mixed Integer Rounding (CMIR) cuts.

MSK_IINF_MIO_NUM_GOMORY_CUTS

Number of Gomory cuts.

MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS

Number of implied bound cuts.

MSK_IINF_MIO_NUM_INT_SOLUTIONS

Number of integer feasible solutions that has been found.

MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS

Number of clique cuts.

MSK_IINF_MIO_NUM_RELAX

Number of relaxations solved during the optimization.

MSK_IINF_MIO_NUM_REPEATED_PRESOLVE

Number of times presolve was repeated at root.

MSK_IINF_MIO_NUMCON

Number of constraints in the problem solved by the mixed-integer optimizer.

MSK_IINF_MIO_NUMINT

Number of integer variables in the problem solved by the mixed-integer optimizer.

MSK_IINF_MIO_NUMVAR

Number of variables in the problem solved by the mixed-integer optimizer.

MSK_IINF_MIO_OBJ_BOUND_DEFINED

Non-zero if a valid objective bound has been found, otherwise zero.

MSK_IINF_MIO_PRESOLVED_NUMBIN

Number of binary variables in the problem solved by the mixed-integer optimizer.

MSK_IINF_MIO_PRESOLVED_NUMCON

Number of constraints in the presolved problem.

MSK_IINF_MIO_PRE SOLVED_NUMCONT	Number of continuous variables in the problem solved by the mixed-integer optimizer.
MSK_IINF_MIO_PRE SOLVED_NUMINT	Number of integer variables in the presolved problem.
MSK_IINF_MIO_PRE SOLVED_NUMVAR	Number of variables in the presolved problem.
MSK_IINF_MIO_RELGAP_SATISFIED	Non-zero if relative gap is within tolerances.
MSK_IINF_MIO_TOTAL_NUM_CUTS	Total number of cuts generated by the mixed-integer optimizer.
MSK_IINF_MIO_USER_OBJ_CUT	If it is non-zero, then the objective cut is used.
MSK_IINF_OPT_NUMCON	Number of constraints in the problem solved when the optimizer is called.
MSK_IINF_OPT_NUMVAR	Number of variables in the problem solved when the optimizer is called
MSK_IINF_OPTIMIZE_RESPONSE	The response code returned by optimize.
MSK_IINF_RD_NUMBARVAR	Number of variables read.
MSK_IINF_RD_NUMCON	Number of constraints read.
MSK_IINF_RD_NUMCONE	Number of conic constraints read.
MSK_IINF_RD_NUMINTVAR	Number of integer-constrained variables read.
MSK_IINF_RD_NUMQ	Number of nonempty Q matrices read.
MSK_IINF_RD_NUMVAR	Number of variables read.
MSK_IINF_RD_PROTOTYPE	Problem type.
MSK_IINF_SIM_DUAL_DEG_ITER	The number of dual degenerate iterations.
MSK_IINF_SIM_DUAL_HOTSTART	If 1 then the dual simplex algorithm is solving from an advanced basis.
MSK_IINF_SIM_DUAL_HOTSTART_LU	If 1 then a valid basis factorization of full rank was located and used by the dual simplex algorithm.
MSK_IINF_SIM_DUAL_INF_ITER	The number of iterations taken with dual infeasibility.
MSK_IINF_SIM_DUAL_ITER	Number of dual simplex iterations during the last optimization.
MSK_IINF_SIM_NUMCON	Number of constraints in the problem solved by the simplex optimizer.
MSK_IINF_SIM_NUMVAR	Number of variables in the problem solved by the simplex optimizer.

MSK_IINF_SIM_PRIMAL_DEG_ITER

The number of primal degenerate iterations.

MSK_IINF_SIM_PRIMAL_HOTSTART

If 1 then the primal simplex algorithm is solving from an advanced basis.

MSK_IINF_SIM_PRIMAL_HOTSTART_LU

If 1 then a valid basis factorization of full rank was located and used by the primal simplex algorithm.

MSK_IINF_SIM_PRIMAL_INF_ITER

The number of iterations taken with primal infeasibility.

MSK_IINF_SIM_PRIMAL_ITER

Number of primal simplex iterations during the last optimization.

MSK_IINF_SIM_SOLVE_DUAL

Is non-zero if dual problem is solved.

MSK_IINF_SOL_BAS_PROSTA

Problem status of the basic solution. Updated after each optimization.

MSK_IINF_SOL_BAS_SOLSTA

Solution status of the basic solution. Updated after each optimization.

MSK_IINF_SOL_ITG_PROSTA

Problem status of the integer solution. Updated after each optimization.

MSK_IINF_SOL_ITG_SOLSTA

Solution status of the integer solution. Updated after each optimization.

MSK_IINF_SOL_ITR_PROSTA

Problem status of the interior-point solution. Updated after each optimization.

MSK_IINF_SOL_ITR_SOLSTA

Solution status of the interior-point solution. Updated after each optimization.

MSK_IINF_STO_NUM_A_REALLOC

Number of times the storage for storing A has been changed. A large value may indicate that memory fragmentation may occur.

13.4.24 Information item types

MSK_INF_DOU_TYPE

Is a double information type.

MSK_INF_INT_TYPE

Is an integer.

MSK_INF_LINT_TYPE

Is a long integer.

13.4.25 Input/output modes

MSK_IOMODE_READ

The file is read-only.

MSK_IOMODE_WRITE

The file is write-only. If the file exists then it is truncated when it is opened. Otherwise it is created when it is opened.

MSK_IOMODE_READWRITE

The file is to read and written.

13.4.26 Specifies the branching direction.

MSK_BRANCH_DIR_FREE

The mixed-integer optimizer decides which branch to choose.

MSK_BRANCH_DIR_UP

The mixed-integer optimizer always chooses the up branch first.

MSK_BRANCH_DIR_DOWN

The mixed-integer optimizer always chooses the down branch first.

MSK_BRANCH_DIR_NEAR

Branch in direction nearest to selected fractional variable.

MSK_BRANCH_DIR_FAR

Branch in direction farthest from selected fractional variable.

MSK_BRANCH_DIR_ROOT_LP

Chose direction based on root lp value of selected variable.

MSK_BRANCH_DIR_GUIDED

Branch in direction of current incumbent.

MSK_BRANCH_DIR_PSEUDOCOST

Branch based on the pseudocost of the variable.

13.4.27 Continuous mixed-integer solution type

MSK_MIO_CONT_SOL_NONE

No interior-point or basic solution are reported when the mixed-integer optimizer is used.

MSK_MIO_CONT_SOL_ROOT

The reported interior-point and basic solutions are a solution to the root node problem when mixed-integer optimizer is used.

MSK_MIO_CONT_SOL_ITG

The reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. A solution is only reported in case the problem has a primal feasible solution.

MSK_MIO_CONT_SOL_ITG_REL

In case the problem is primal feasible then the reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. If the problem is primal infeasible, then the solution to the root node problem is reported.

13.4.28 Integer restrictions

MSK_MIO_MODE_IGNORED

The integer constraints are ignored and the problem is solved as a continuous problem.

MSK_MIO_MODE_SATISFIED

Integer restrictions should be satisfied.

13.4.29 Mixed-integer node selection types

MSK_MIO_NODE_SELECTION_FREE

The optimizer decides the node selection strategy.

MSK_MIO_NODE_SELECTION_FIRST

The optimizer employs a depth first node selection strategy.

MSK_MIO_NODE_SELECTION_BEST

The optimizer employs a best bound node selection strategy.

MSK_MIO_NODE_SELECTION_WORST

The optimizer employs a worst bound node selection strategy.

MSK_MIO_NODE_SELECTION_HYBRID

The optimizer employs a hybrid strategy.

MSK_MIO_NODE_SELECTION_PSEUDO

The optimizer employs selects the node based on a pseudo cost estimate.

13.4.30 MPS file format type

MSK_MPS_FORMAT_STRICT

It is assumed that the input file satisfies the MPS format strictly.

MSK_MPS_FORMAT_RELAXED

It is assumed that the input file satisfies a slightly relaxed version of the MPS format.

MSK_MPS_FORMAT_FREE

It is assumed that the input file satisfies the free MPS format. This implies that spaces are not allowed in names. Otherwise the format is free.

MSK_MPS_FORMAT_CPLEX

The CPLEX compatible version of the MPS format is employed.

13.4.31 Objective sense types

MSK_OBJECTIVE_SENSE_MINIMIZE

The problem should be minimized.

MSK_OBJECTIVE_SENSE_MAXIMIZE

The problem should be maximized.

13.4.32 On/off

MSK_ON

Switch the option on.

MSK_OFF

Switch the option off.

13.4.33 Optimizer types

MSK_OPTIMIZER_CONIC

The optimizer for problems having conic constraints.

MSK_OPTIMIZER_DUAL_SIMPLEX

The dual simplex optimizer is used.

MSK_OPTIMIZER_FREE

The optimizer is chosen automatically.

MSK_OPTIMIZER_FREE_SIMPLEX

One of the simplex optimizers is used.

MSK_OPTIMIZER_INTPNT

The interior-point optimizer is used.

MSK_OPTIMIZER_MIXED_INT

The mixed-integer optimizer.

MSK_OPTIMIZER_PRIMAL_SIMPLEX

The primal simplex optimizer is used.

13.4.34 Ordering strategies

MSK_ORDER_METHOD_FREE

The ordering method is chosen automatically.

MSK_ORDER_METHOD_APPMINLOC

Approximate minimum local fill-in ordering is employed.

MSK_ORDER_METHOD_EXPERIMENTAL

This option should not be used.

MSK_ORDER_METHOD_TRY_GRAPHPAR

Always try the graph partitioning based ordering.

MSK_ORDER_METHOD_FORCE_GRAPHPAR

Always use the graph partitioning based ordering even if it is worse than the approximate minimum local fill ordering.

MSK_ORDER_METHOD_NONE

No ordering is used.

13.4.35 Presolve method.

MSK_PRESOLVE_MODE_OFF

The problem is not presolved before it is optimized.

MSK_PRESOLVE_MODE_ON

The problem is presolved before it is optimized.

MSK_PRESOLVE_MODE_FREE

It is decided automatically whether to presolve before the problem is optimized.

13.4.36 Parameter type

MSK_PAR_INVALID_TYPE

Not a valid parameter.

MSK_PAR_DOUB_TYPE

Is a double parameter.

MSK_PAR_INT_TYPE

Is an integer parameter.

MSK_PAR_STR_TYPE

Is a string parameter.

13.4.37 Problem data items

MSK_PI_VAR

Item is a variable.

MSK_PI_CON

Item is a constraint.

MSK_PI_CONE

Item is a cone.

13.4.38 Problem types

MSK_PROBTYPE_LO

The problem is a linear optimization problem.

MSK_PROBTYPE_QO

The problem is a quadratic optimization problem.

MSK_PROBTYPE_QCQO

The problem is a quadratically constrained optimization problem.

MSK_PROBTYPE_GECO

General convex optimization.

MSK_PROBTYPE_CONIC

A conic optimization.

MSK_PROBTYPE_MIXED

General nonlinear constraints and conic constraints. This combination can not be solved by MOSEK.

13.4.39 Problem status keys

MSK_PRO_STA_UNKNOWN

Unknown problem status.

MSK_PRO_STA_PRIM_AND_DUAL_FEAS

The problem is primal and dual feasible.

MSK_PRO_STA_PRIM_FEAS

The problem is primal feasible.

MSK_PRO_STA_DUAL_FEAS

The problem is dual feasible.

MSK_PRO_STA_NEAR_PRIM_AND_DUAL_FEAS

The problem is at least nearly primal and dual feasible.

MSK_PRO_STA_NEAR_PRIM_FEAS

The problem is at least nearly primal feasible.

MSK_PRO_STA_NEAR_DUAL_FEAS

The problem is at least nearly dual feasible.

MSK_PRO_STA_PRIM_INFEAS

The problem is primal infeasible.

MSK_PRO_STA_DUAL_INFEAS

The problem is dual infeasible.

MSK_PRO_STA_PRIM_AND_DUAL_INFEAS

The problem is primal and dual infeasible.

MSK_PRO_STA_ILL_POSED

The problem is ill-posed. For example, it may be primal and dual feasible but have a positive duality gap.

MSK_PRO_STA_PRIM_INFEAS_OR_UNBOUNDED

The problem is either primal infeasible or unbounded. This may occur for mixed-integer problems.

13.4.40 XML writer output mode

MSK_WRITE_XML_MODE_ROW

Write in row order.

MSK_WRITE_XML_MODE_COL

Write in column order.

13.4.41 Response code type

MSK_RESPONSE_OK

The response code is OK.

MSK_RESPONSE_WRN

The response code is a warning.

MSK_RESPONSE_TRM

The response code is an optimizer termination status.

MSK_RESPONSE_ERR

The response code is an error.

MSK_RESPONSE_UNK

The response code does not belong to any class.

13.4.42 Scaling type

MSK_SCALING_FREE

The optimizer chooses the scaling heuristic.

MSK_SCALING_NONE

No scaling is performed.

MSK_SCALING_MODERATE

A conservative scaling is performed.

MSK_SCALING_AGGRESSIVE

A very aggressive scaling is performed.

13.4.43 Scaling method

MSK_SCALING_METHOD_POW2

Scales only with power of 2 leaving the mantissa untouched.

MSK_SCALING_METHOD_FREE

The optimizer chooses the scaling heuristic.

13.4.44 Sensitivity types

MSK_SENSITIVITY_TYPE_BASIS

Basis sensitivity analysis is performed.

MSK_SENSITIVITY_TYPE_OPTIMAL_PARTITION

Optimal partition sensitivity analysis is performed.

13.4.45 Simplex selection strategy

MSK_SIM_SELECTION_FREE

The optimizer chooses the pricing strategy.

MSK_SIM_SELECTION_FULL

The optimizer uses full pricing.

MSK_SIM_SELECTION_ASE

The optimizer uses approximate steepest-edge pricing.

MSK_SIM_SELECTION_DEVEX

The optimizer uses devex steepest-edge pricing (or if it is not available an approximate steep-edge selection).

MSK_SIM_SELECTION_SE

The optimizer uses steepest-edge selection (or if it is not available an approximate steep-edge selection).

MSK_SIM_SELECTION_PARTIAL

The optimizer uses a partial selection approach. The approach is usually beneficial if the number of variables is much larger than the number of constraints.

13.4.46 Solution items

MSK_SOL_ITEM_XC

Solution for the constraints.

MSK_SOL_ITEM_XX

Variable solution.

MSK_SOL_ITEM_Y

Lagrange multipliers for equations.

MSK_SOL_ITEM_SLC

Lagrange multipliers for lower bounds on the constraints.

MSK_SOL_ITEM_SUC

Lagrange multipliers for upper bounds on the constraints.

MSK_SOL_ITEM_SLX

Lagrange multipliers for lower bounds on the variables.

MSK_SOL_ITEM_SUX

Lagrange multipliers for upper bounds on the variables.

MSK_SOL_ITEM_SNX

Lagrange multipliers corresponding to the conic constraints on the variables.

13.4.47 Solution status keys

MSK_SOL_STA_UNKNOWN

Status of the solution is unknown.

MSK_SOL_STA_OPTIMAL

The solution is optimal.

MSK_SOL_STA_PRIM_FEAS

The solution is primal feasible.

MSK_SOL_STA_DUAL_FEAS

The solution is dual feasible.

MSK_SOL_STA_PRIM_AND_DUAL_FEAS

The solution is both primal and dual feasible.

MSK_SOL_STA_NEAR_OPTIMAL

The solution is nearly optimal.

MSK_SOL_STA_NEAR_PRIM_FEAS

The solution is nearly primal feasible.

MSK_SOL_STA_NEAR_DUAL_FEAS

The solution is nearly dual feasible.

MSK_SOL_STA_NEAR_PRIM_AND_DUAL_FEAS

The solution is nearly both primal and dual feasible.

MSK_SOL_STA_PRIM_INFEAS_CER

The solution is a certificate of primal infeasibility.

MSK_SOL_STA_DUAL_INFEAS_CER

The solution is a certificate of dual infeasibility.

MSK_SOL_STA_NEAR_PRIM_INFEAS_CER

The solution is almost a certificate of primal infeasibility.

MSK_SOL_STA_NEAR_DUAL_INFEAS_CER

The solution is almost a certificate of dual infeasibility.

MSK_SOL_STA_PRIM_ILLPOSED_CER

The solution is a certificate that the primal problem is illposed.

MSK_SOL_STA_DUAL_ILLPOSED_CER

The solution is a certificate that the dual problem is illposed.

MSK_SOL_STA_INTEGER_OPTIMAL

The primal solution is integer optimal.

MSK_SOL_STA_NEAR_INTEGER_OPTIMAL

The primal solution is near integer optimal.

13.4.48 Solution types

MSK_SOL_BAS

The basic solution.

MSK_SOL_ITR

The interior solution.

MSK_SOL_ITG

The integer solution.

13.4.49 Solve primal or dual form

MSK_SOLVE_FREE

The optimizer is free to solve either the primal or the dual problem.

MSK_SOLVE_PRIMAL

The optimizer should solve the primal problem.

MSK_SOLVE_DUAL

The optimizer should solve the dual problem.

13.4.50 Status keys

MSK_SK_UNK

The status for the constraint or variable is unknown.

MSK_SK_BAS

The constraint or variable is in the basis.

MSK_SK_SUPBAS

The constraint or variable is super basic.

MSK_SK_LOW

The constraint or variable is at its lower bound.

MSK_SK_UPR

The constraint or variable is at its upper bound.

MSK_SK_FIX

The constraint or variable is fixed.

MSK_SK_INF

The constraint or variable is infeasible in the bounds.

13.4.51 Starting point types

MSK_STARTING_POINT_FREE

The starting point is chosen automatically.

MSK_STARTING_POINT_GUESS

The optimizer guesses a starting point.

MSK_STARTING_POINT_CONSTANT

The optimizer constructs a starting point by assigning a constant value to all primal and dual variables. This starting point is normally robust.

MSK_STARTING_POINT_SATISFY_BOUNDS

The starting point is chosen to satisfy all the simple bounds on nonlinear variables. If this starting point is employed, then more care than usual should be employed when choosing the bounds on the nonlinear variables. In particular very tight bounds should be avoided.

13.4.52 Stream types

MSK_STREAM_LOG

Log stream. Contains the aggregated contents of all other streams. This means that a message written to any other stream will also be written to this stream.

MSK_STREAM_MSG

Message stream. Log information relating to performance and progress of the optimization is written to this stream.

MSK_STREAM_ERR

Error stream. Error messages are written to this stream.

MSK_STREAM_WRN

Warning stream. Warning messages are written to this stream.

13.4.53 Integer values

MSK_MAX_STR_LEN

Maximum string length allowed in **MOSEK**.

MSK_LICENSE_BUFFER_LENGTH

The length of a license key buffer.

13.4.54 Variable types

MSK_VAR_TYPE_CONT

Is a continuous variable.

MSK_VAR_TYPE_INT

Is an integer variable.

SUPPORTED FILE FORMATS

MOSEK supports a range of problem and solution formats listed in [Table 14.1](#) and [Table 14.2](#). The **Task format** is **MOSEK**'s native binary format and it supports all features that **MOSEK** supports. The **OPF format** is **MOSEK**'s human-readable alternative that supports nearly all features (everything except semidefinite problems). In general, text formats are significantly slower to read, but can be examined and edited directly in any text editor.

Problem formats

See [Table 14.1](#).

Table 14.1: List of supported file formats for optimization problems.

Format Type	Ext.	Binary/Text	LP	QO	CQO	SDP
<i>LP</i>	lp	plain text	X	X		
<i>MPS</i>	mps	plain text	X	X		
<i>OPF</i>	opf	plain text	X	X	X	
<i>CBF</i>	cbf	plain text	X		X	X
<i>OSiL</i>	xml	xml text	X	X		
<i>Task format</i>	task	binary	X	X	X	X
<i>Jtask format</i>	jtask	text	X	X	X	X

Solution formats

See [Table 14.2](#).

Table 14.2: List of supported solution formats.

Format Type	Ext.	Binary/Text	Description
<i>SOL</i>	sol	plain text	Interior Solution
	bas	plain text	Basic Solution
	int	plain text	Integer
<i>Jsol format</i>	jsol	text	Solution

Compression

MOSEK supports GZIP compression of files. Problem files with an additional `.gz` extension are assumed to be compressed when read, and are automatically compressed when written. For example, a file called

problem.mps.gz

will be considered as a GZIP compressed MPS file.

14.1 The LP File Format

MOSEK supports the LP file format with some extensions. The LP format is not a completely well-defined standard and hence different optimization packages may interpret the same LP file in slightly different ways. **MOSEK** tries to emulate as closely as possible CPLEX's behavior, but tries to stay backward compatible.

The LP file format can specify problems on the form

$$\begin{array}{ll} \text{minimize/maximize} & c^T x + \frac{1}{2} q^o(x) \\ \text{subject to} & \begin{array}{lll} l^c \leq & Ax + \frac{1}{2} q(x) & \leq u^c, \\ l^x \leq & x & \leq u^x, \\ & x_{\mathcal{J}} \text{ integer,} \end{array} \end{array}$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear term in the objective.
- $q^o : \mathbb{R}^n \rightarrow \mathbb{R}$ is the quadratic term in the objective where

$$q^o(x) = x^T Q^o x$$

and it is assumed that

$$Q^o = (Q^o)^T.$$

- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $q : \mathbb{R}^n \rightarrow \mathbb{R}$ is a vector of quadratic functions. Hence,

$$q_i(x) = x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

- $\mathcal{J} \subseteq \{1, 2, \dots, n\}$ is an index set of the integer constrained variables.

14.1.1 File Sections

An LP formatted file contains a number of sections specifying the objective, constraints, variable bounds, and variable types. The section keywords may be any mix of upper and lower case letters.

Objective Function

The first section beginning with one of the keywords

```

max
maximum
maximize
min
minimum
minimize

```

defines the objective sense and the objective function, i.e.

$$c^T x + \frac{1}{2} x^T Q^o x.$$

The objective may be given a name by writing

```
myname:
```

before the expressions. If no name is given, then the objective is named `obj`.

The objective function contains linear and quadratic terms. The linear terms are written as:

```
4 x1 + x2 - 0.1 x3
```

and so forth. The quadratic terms are written in square brackets (`[]`) and are either squared or multiplied as in the examples

```
x1^2
```

and

```
x1 * x2
```

There may be zero or more pairs of brackets containing quadratic expressions.

An example of an objective section is

```

minimize
myobj: 4 x1 + x2 - 0.1 x3 + [ x1^2 + 2.1 x1 * x2 ]/2

```

Please note that the quadratic expressions are multiplied with $\frac{1}{2}$, so that the above expression means

$$\text{minimize } 4x_1 + x_2 - 0.1 \cdot x_3 + \frac{1}{2}(x_1^2 + 2.1 \cdot x_1 \cdot x_2)$$

If the same variable occurs more than once in the linear part, the coefficients are added, so that `4 x1 + 2 x1` is equivalent to `6 x1`. In the quadratic expressions `x1 * x2` is equivalent to `x2 * x1` and, as in the linear part, if the same variables multiplied or squared occur several times their coefficients are added.

Constraints

The second section beginning with one of the keywords

```

subj to
subject to
s.t.
st

```

defines the linear constraint matrix A and the quadratic matrices Q^i .

A constraint contains a name (optional), expressions adhering to the same rules as in the objective and a bound:

```

subject to
con1: x1 + x2 + [ x3^2 ]/2 <= 5.1

```

The bound type (here \leq) may be any of $<$, \leq , $=$, $>$, \geq ($<$ and \leq mean the same), and the bound may be any number.

In the standard LP format it is not possible to define more than one bound, but **MOSEK** supports defining ranged constraints by using double-colon ($::$) instead of a single-colon ($:$) after the constraint name, i.e.

$$-5 \leq x_1 + x_2 \leq 5 \tag{14.1}$$

may be written as

```
con:: -5 < x_1 + x_2 < 5
```

By default **MOSEK** writes ranged constraints this way.

If the files must adhere to the LP standard, ranged constraints must either be split into upper bounded and lower bounded constraints or be written as an equality with a slack variable. For example the expression (14.1) may be written as

$$x_1 + x_2 - sl_1 = 0, \quad -5 \leq sl_1 \leq 5.$$

Bounds

Bounds on the variables can be specified in the bound section beginning with one of the keywords

```
bound
bounds
```

The bounds section is optional but should, if present, follow the **subject to** section. All variables listed in the bounds section must occur in either the objective or a constraint.

The default lower and upper bounds are 0 and $+\infty$. A variable may be declared free with the keyword **free**, which means that the lower bound is $-\infty$ and the upper bound is $+\infty$. Furthermore it may be assigned a finite lower and upper bound. The bound definitions for a given variable may be written in one or two lines, and bounds can be any number or $\pm\infty$ (written as **+inf/-inf/+infinity/-infinity**) as in the example

```
bounds
x1 free
x2 <= 5
0.1 <= x2
x3 = 42
2 <= x4 < +inf
```

Variable Types

The final two sections are optional and must begin with one of the keywords

```
bin
binaries
binary
```

and

```
gen
general
```

Under **general** all integer variables are listed, and under **binary** all binary (integer variables with bounds 0 and 1) are listed:


```

general
x1 x2
binary
x3 x4

```

Again, all variables listed in the binary or general sections must occur in either the objective or a constraint.

Terminating Section

Finally, an LP formatted file must be terminated with the keyword

```
end
```

14.1.2 LP File Examples

Linear example lo1.lp

```

\ File: lo1.lp
maximize
obj: 3 x1 + x2 + 5 x3 + x4
subject to
c1: 3 x1 + x2 + 2 x3 = 30
c2: 2 x1 + x2 + 3 x3 + x4 >= 15
c3: 2 x2 + 3 x4 <= 25
bounds
0 <= x1 <= +infinity
0 <= x2 <= 10
0 <= x3 <= +infinity
0 <= x4 <= +infinity
end

```

Mixed integer example milo1.lp

```

maximize
obj: x1 + 6.4e-01 x2
subject to
c1: 5e+01 x1 + 3.1e+01 x2 <= 2.5e+02
c2: 3e+00 x1 - 2e+00 x2 >= -4e+00
bounds
0 <= x1 <= +infinity
0 <= x2 <= +infinity
general
x1 x2
end

```

14.1.3 LP Format peculiarities

Comments

Anything on a line after a \ is ignored and is treated as a comment.

Names

A name for an objective, a constraint or a variable may contain the letters *a-z*, *A-Z*, the digits *0-9* and the characters

!"#\$%&()/,.;?@_`'|~

The first character in a name must not be a number, a period or the letter *e* or *E*. Keywords must not be used as names.

MOSEK accepts any character as valid for names, except `\0`. A name that is not allowed in LP file will be changed and a warning will be issued.

The algorithm for making names LP valid works as follows: The name is interpreted as an `utf-8` string. For a unicode character *c*:

- If *c*==`_` (underscore), the output is `__` (two underscores).
- If *c* is a valid LP name character, the output is just *c*.
- If *c* is another character in the ASCII range, the output is `_XX`, where *XX* is the hexadecimal code for the character.
- If *c* is a character in the range *127-65535*, the output is `_uXXXX`, where *XXXX* is the hexadecimal code for the character.
- If *c* is a character above 65535, the output is `_UXXXXXXXX`, where *XXXXXXXX* is the hexadecimal code for the character.

Invalid `utf-8` substrings are escaped as `_XX'`, and if a name starts with a period, *e* or *E*, that character is escaped as `_XX`.

Variable Bounds

Specifying several upper or lower bounds on one variable is possible but **MOSEK** uses only the tightest bounds. If a variable is fixed (with `=`), then it is considered the tightest bound.

MOSEK Extensions to the LP Format

Some optimization software packages employ a more strict definition of the LP format than the one used by **MOSEK**. The limitations imposed by the strict LP format are the following:

- Quadratic terms in the constraints are not allowed.
- Names can be only 16 characters long.
- Lines must not exceed 255 characters in length.

If an LP formatted file created by **MOSEK** should satisfy the strict definition, then the parameter

- `MSK_IPAR_WRITE_LP_STRICT_FORMAT`

should be set; note, however, that some problems cannot be written correctly as a strict LP formatted file. For instance, all names are truncated to 16 characters and hence they may lose their uniqueness and change the problem.

To get around some of the inconveniences converting from other problem formats, **MOSEK** allows lines to contain 1024 characters and names may have any length (shorter than the 1024 characters).

Internally in **MOSEK** names may contain any (printable) character, many of which cannot be used in LP names. Setting the parameters

- `MSK_IPAR_READ_LP_QUOTED_NAMES` and
- `MSK_IPAR_WRITE_LP_QUOTED_NAMES`

allows **MOSEK** to use quoted names. The first parameter tells **MOSEK** to remove quotes from quoted names e.g, "x1", when reading LP formatted files. The second parameter tells **MOSEK** to put quotes around any semi-illegal name (names beginning with a number or a period) and fully illegal name (containing illegal characters). As double quote is a legal character in the LP format, quoting semi-illegal names makes them legal in the pure LP format as long as they are still shorter than 16 characters. Fully illegal names are still illegal in a pure LP file.

14.1.4 The strict LP format

The LP format is not a formal standard and different vendors have slightly different interpretations of the LP format. To make **MOSEK**'s definition of the LP format more compatible with the definitions of other vendors, use the parameter setting

- `MSK_IPAR_WRITE_LP_STRICT_FORMAT = MSK_ON`

This setting may lead to truncation of some names and hence to an invalid LP file. The simple solution to this problem is to use the parameter setting

- `MSK_IPAR_WRITE_GENERIC_NAMES = MSK_ON`

which will cause all names to be renamed systematically in the output file.

14.1.5 Formatting of an LP File

A few parameters control the visual formatting of LP files written by **MOSEK** in order to make it easier to read the files. These parameters are

- `MSK_IPAR_WRITE_LP_LINE_WIDTH`
- `MSK_IPAR_WRITE_LP_TERMS_PER_LINE`

The first parameter sets the maximum number of characters on a single line. The default value is 80 corresponding roughly to the width of a standard text document.

The second parameter sets the maximum number of terms per line; a term means a sign, a coefficient, and a name (for example + 42 elephants). The default value is 0, meaning that there is no maximum.

Unnamed Constraints

Reading and writing an LP file with **MOSEK** may change it superficially. If an LP file contains unnamed constraints or objective these are given their generic names when the file is read (however unnamed constraints in **MOSEK** are written without names).

14.2 The MPS File Format

MOSEK supports the standard MPS format with some extensions. For a detailed description of the MPS format see the book by Nazareth [Naz87].

14.2.1 MPS File Structure

The version of the MPS format supported by **MOSEK** allows specification of an optimization problem of the form

$$\begin{aligned} l^c &\leq Ax + q(x) &&\leq u^c, \\ l^x &\leq x &&\leq u^x, \\ &x \in \mathcal{K}, \\ &x_{\mathcal{J}} \text{ integer}, \end{aligned} \tag{14.2}$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $q : \mathbb{R}^n \rightarrow \mathbb{R}$ is a vector of quadratic functions. Hence,

$$q_i(x) = \frac{1}{2} x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

Please note the explicit $\frac{1}{2}$ in the quadratic term and that Q^i is required to be symmetric.

- \mathcal{K} is a convex cone.
- $\mathcal{J} \subseteq \{1, 2, \dots, n\}$ is an index set of the integer-constrained variables.

An MPS file with one row and one column can be illustrated like this:

```
*          1          2          3          4          5          6
*23456789012345678901234567890123456789012345678901234567890
NAME          [name]
OBJSENSE
[objsense]
OBJNAME
[objname]
ROWS
? [cname1]
COLUMNS
[vname1] [cname1] [value1] [vname3] [value2]
RHS
[name] [cname1] [value1] [cname2] [value2]
RANGES
[name] [cname1] [value1] [cname2] [value2]
QSECTION      [cname1]
[vname1] [vname2] [value1] [vname3] [value2]
QMATRIX
[vname1] [vname2] [value1]
QUADOBJ
[vname1] [vname2] [value1]
QCMATRIX      [cname1]
[vname1] [vname2] [value1]
BOUNDS
?? [name] [vname1] [value1]
CSECTION      [kname1] [value1] [ktype]
[vname1]
ENDATA
```

Here the names in capitals are keywords of the MPS format and names in brackets are custom defined names or values. A couple of notes on the structure:

- Fields: All items surrounded by brackets appear in *fields*. The fields named “valueN” are numerical values. Hence, they must have the format

```
[+|-]XXXXXXXX.XXXXXX[[e|E][+|-]XXX]
```

where

```
.. code-block:: text
```

```
X = [0|1|2|3|4|5|6|7|8|9].
```

- Sections: The MPS file consists of several sections where the names in capitals indicate the beginning of a new section. For example, COLUMNS denotes the beginning of the columns section.
- Comments: Lines starting with an * are comment lines and are ignored by **MOSEK**.
- Keys: The question marks represent keys to be specified later.
- Extensions: The sections QSECTION and CSECTION are specific **MOSEK** extensions of the MPS format. The sections QMATRIX, QUADOBJ and QCMATRIX are included for sake of compatibility with other vendors extensions to the MPS format.

The standard MPS format is a fixed format, i.e. everything in the MPS file must be within certain fixed positions. **MOSEK** also supports a *free format*. See [Sec. 14.2.9](#) for details.

Linear example lo1.mps

A concrete example of a MPS file is presented below:

```
* File: lo1.mps
NAME          lo1
OBJSENSE
    MAX
ROWS
N   obj
E   c1
G   c2
L   c3
COLUMNS
    x1      obj      3
    x1      c1       3
    x1      c2       2
    x2      obj      1
    x2      c1       1
    x2      c2       1
    x2      c3       2
    x3      obj      5
    x3      c1       2
    x3      c2       3
    x4      obj      1
    x4      c2       1
    x4      c3       3
RHS
    rhs     c1      30
    rhs     c2      15
    rhs     c3      25
RANGES
BOUNDS
UP bound    x2      10
ENDATA
```

Subsequently each individual section in the MPS format is discussed.

Section NAME

In this section a name ([name]) is assigned to the problem.

OBJSENSE (optional)

This is an optional section that can be used to specify the sense of the objective function. The **OBJSENSE** section contains one line at most which can be one of the following

```
MIN
MINIMIZE
MAX
MAXIMIZE
```

It should be obvious what the implication is of each of these four lines.

OBJNAME (optional)

This is an optional section that can be used to specify the name of the row that is used as objective function. The **OBJNAME** section contains one line at most which has the form

```
objname
```

`objname` should be a valid row name.

ROWS

A record in the **ROWS** section has the form

```
? [cname1]
```

where the requirements for the fields are as follows:

Field	Starting Position	Max Width	required	Description
?	2	1	Yes	Constraint key
[cname1]	5	8	Yes	Constraint name

Hence, in this section each constraint is assigned an unique name denoted by `[cname1]`. Please note that `[cname1]` starts in position 5 and the field can be at most 8 characters wide. An initial key `?` must be present to specify the type of the constraint. The key can have the values **E**, **G**, **L**, or **N** with the following interpretation:

Constraint type	l_i^c	u_i^c
E	finite	l_i^c
G	finite	∞
L	$-\infty$	finite
N	$-\infty$	∞

In the MPS format an objective vector is not specified explicitly, but one of the constraints having the key **N** will be used as the objective vector c . In general, if multiple **N** type constraints are specified, then the first will be used as the objective vector c .

COLUMNS

In this section the elements of A are specified using one or more records having the form:

```
[vname1] [cname1] [value1] [cname2] [value2]
```

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

Hence, a record specifies one or two elements a_{ij} of A using the principle that [vname1] and [cname1] determines j and i respectively. Please note that [cname1] must be a constraint name specified in the ROWS section. Finally, [value1] denotes the numerical value of a_{ij} . Another optional element is specified by [cname2], and [value2] for the variable specified by [vname1]. Some important comments are:

- All elements belonging to one variable must be grouped together.
- Zero elements of A should not be specified.
- At least one element for each variable should be specified.

RHS (optional)

A record in this section has the format

[name]	[cname1]	[value1]	[cname2]	[value2]
--------	----------	----------	----------	----------

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RHS vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The interpretation of a record is that [name] is the name of the RHS vector to be specified. In general, several vectors can be specified. [cname1] denotes a constraint name previously specified in the ROWS section. Now, assume that this name has been assigned to the i th constraint and v_1 denotes the value specified by [value1], then the interpretation of v_1 is:

Constraint type	l_i^c	u_i^c
E	v_1	v_1
G	v_1	
L		v_1
N		

An optional second element is specified by [cname2] and [value2] and is interpreted in the same way. Please note that it is not necessary to specify zero elements, because elements are assumed to be zero.

RANGES (optional)

A record in this section has the form

[name]	[cname1]	[value1]	[cname2]	[value2]
--------	----------	----------	----------	----------

where the requirements for each fields are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RANGE vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The records in this section are used to modify the bound vectors for the constraints, i.e. the values in l^c and u^c . A record has the following interpretation: [name] is the name of the RANGE vector and [cname1] is a valid constraint name. Assume that [cname1] is assigned to the i th constraint and let v_1 be the value specified by [value1], then a record has the interpretation:

Constraint type	Sign of v_1	l_i^c	u_i^c
E	—	$u_i^c + v_1$	
E	+		$l_i^c + v_1$
G	— or +	$l_i^c + v_1 $	
L	— or +	$u_i^c - v_1 $	
N			

QSECTION (optional)

Within the QSECTION the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the QSECTION has the form

[vname1]	[vname2]	[value1]	[vname3]	[value2]
----------	----------	----------	----------	----------

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value
[vname3]	40	8	No	Variable name
[value2]	50	12	No	Numerical value

A record specifies one or two elements in the lower triangular part of the Q^i matrix where [cname1] specifies the i . Hence, if the names [vname1] and [vname2] have been assigned to the k th and j th variable, then Q_{kj}^i is assigned the value given by [value1]. An optional second element is specified in the same way by the fields [vname1], [vname3], and [value2].

The example

$$\begin{aligned}
 &\text{minimize} && -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) \\
 &\text{subject to} && x_1 + x_2 + x_3 \geq 1, \\
 &&& x \geq 0
 \end{aligned}$$

has the following MPS file representation

```

* File: qo1.mps
NAME          qo1
ROWS
N   obj
G   c1
COLUMNS

```



```

x1      c1      1.0
x2      obj     -1.0
x2      c1      1.0
x3      c1      1.0
RHS
rhs     c1      1.0
QSECTION      obj
x1      x1      2.0
x1      x3     -1.0
x2      x2      0.2
x3      x3      2.0
ENDATA

```

Regarding the QSECTIONs please note that:

- Only one QSECTION is allowed for each constraint.
- The QSECTIONs can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QSECTION must already be specified in the COLUMNS section.
- All entries specified in a QSECTION are assumed to belong to the lower triangular part of the quadratic term of Q .

QMATRIX/QUADOBJ (optional)

The QMATRIX and QUADOBJ sections allow to define the quadratic term of the objective function. They differ in how the quadratic term of the objective function is stored:

- **QMATRIX** It stores all the nonzeros coefficients, without taking advantage of the symmetry of the Q matrix.
- **QUADOBJ** It only store the upper diagonal nonzero elements of the Q matrix.

A record in both sections has the form:

```
[vname1] [vname2] [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies one elements of the Q matrix in the objective function. Hence, if the names [vname1] and [vname2] have been assigned to the k th and j th variable, then Q_{kj} is assigned the value given by [value1]. Note that a line must appear for each off-diagonal coefficient if using a QMATRIX section, while only one entry is required in a QUADOBJ section. The quadratic part of the objective function will be evaluated as $1/2x^T Qx$.

The example

$$\begin{aligned}
 &\text{minimize} && -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) \\
 &\text{subject to} && x_1 + x_2 + x_3 \geq 1, \\
 &&& x \geq 0
 \end{aligned}$$

has the following MPS file representation using QMATRIX

```

* File: qo1_matrix.mps
NAME          qo1_qmatrix
ROWS

```

```

N  obj
G  c1
COLUMNS
    x1      c1      1.0
    x2      obj     -1.0
    x2      c1      1.0
    x3      c1      1.0
RHS
    rhs      c1      1.0
QMATRIX
    x1      x1      2.0
    x1      x3     -1.0
    x3      x1     -1.0
    x2      x2      0.2
    x3      x3      2.0
ENDATA

```

or the following using QUADOBJ

```

* File: qo1_quadobj.mps
NAME          qo1_quadobj
ROWS
  N  obj
  G  c1
COLUMNS
    x1      c1      1.0
    x2      obj     -1.0
    x2      c1      1.0
    x3      c1      1.0
RHS
    rhs      c1      1.0
QUADOBJ
    x1      x1      2.0
    x1      x3     -1.0
    x2      x2      0.2
    x3      x3      2.0
ENDATA

```

Please also note that:

- A QMATRIX/QUADOBJ section can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QMATRIX/QUADOBJ section must already be specified in the COLUMNS section.

14.2.2 QCMATRIX (optional)

A QCMATRIX section allows to specify the quadratic part of a given constraints. Within the QCMATRIX the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the QSECTION has the form

[vname1]	[vname2]	[value1]
----------	----------	----------

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies an entry of the Q^i matrix where [cname1] specifies the i . Hence, if the names [vname1] and [vname2] have been assigned to the k th and j th variable, then Q_{kj}^i is assigned the value given by [value1]. Moreover, the quadratic term is represented as $1/2x^T Qx$.

The example

$$\begin{aligned} & \text{minimize} && x_2 \\ & \text{subject to} && x_1 + x_2 + x_3 \geq 1, \\ & && \frac{1}{2}(-2x_1x_3 + 0.2x_2^2 + 2x_3^2) \leq 10, \\ & && x \geq 0 \end{aligned}$$

has the following MPS file representation

```
* File: qo1.mps
NAME          qo1
ROWS
 N  obj
 G  c1
 L  q1
COLUMNS
  x1      c1      1.0
  x2      obj     -1.0
  x2      c1      1.0
  x3      c1      1.0
RHS
  rhs     c1      1.0
  rhs     q1     10.0
QCMATRIX   q1
  x1      x1      2.0
  x1      x3     -1.0
  x3      x1     -1.0
  x2      x2      0.2
  x3      x3      2.0
ENDATA
```

Regarding the QCMATRIXs please note that:

- Only one QCMATRIX is allowed for each constraint.
- The QCMATRIXs can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QSECTION must already be specified in the COLUMNS section.
- A QCMATRIX does not exploit the symmetry of Q : an off-diagonal entry (i, j) should appear twice.

14.2.3 BOUNDS (optional)

In the BOUNDS section changes to the default bounds vectors l^x and u^x are specified. The default bounds vectors are $l^x = 0$ and $u^x = \infty$. Moreover, it is possible to specify several sets of bound vectors. A record in this section has the form

```
?? [name]    [vname1]    [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	Required	Description
??	2	2	Yes	Bound key
[name]	5	8	Yes	Name of the BOUNDS vector
[vname1]	15	8	Yes	Variable name
[value1]	25	12	No	Numerical value

Hence, a record in the BOUNDS section has the following interpretation: `[name]` is the name of the bound vector and `[vname1]` is the name of the variable which bounds are modified by the record. `??` and `[value1]` are used to modify the bound vectors according to the following table:

??	l_j^x	u_j^x	Made integer (added to \mathcal{J})
FR	$-\infty$	∞	No
FX	v_1	v_1	No
LO	v_1	unchanged	No
MI	$-\infty$	unchanged	No
PL	unchanged	∞	No
UP	unchanged	v_1	No
BV	0	1	Yes
LI	$\lceil v_1 \rceil$	unchanged	Yes
UI	unchanged	$\lfloor v_1 \rfloor$	Yes

v_1 is the value specified by `[value1]`.

14.2.4 CSECTION (optional)

The purpose of the CSECTION is to specify the constraint

$$x \in \mathcal{K}.$$

in (14.2). It is assumed that \mathcal{K} satisfies the following requirements. Let

$$x^t \in \mathbb{R}^{n^t}, \quad t = 1, \dots, k$$

be vectors comprised of parts of the decision variables x so that each decision variable is a member of exactly **one** vector x^t , for example

$$x^1 = \begin{bmatrix} x_1 \\ x_4 \\ x_7 \end{bmatrix} \quad \text{and} \quad x^2 = \begin{bmatrix} x_6 \\ x_5 \\ x_3 \\ x_2 \end{bmatrix}.$$

Next define

$$\mathcal{K} := \{x \in \mathbb{R}^n : x^t \in \mathcal{K}_t, \quad t = 1, \dots, k\}$$

where \mathcal{K}_t must have one of the following forms

- \mathbb{R} set:

$$\mathcal{K}_t = \{x \in \mathbb{R}^{n^t}\}.$$

- Quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : x_1 \geq \sqrt{\sum_{j=2}^{n^t} x_j^2} \right\}. \quad (14.3)$$

- Rotated quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : 2x_1x_2 \geq \sum_{j=3}^{n^t} x_j^2, \quad x_1, x_2 \geq 0 \right\}. \quad (14.4)$$

In general, only quadratic and rotated quadratic cones are specified in the MPS file whereas membership of the \mathbb{R} set is not. If a variable is not a member of any other cone then it is assumed to be a member of an \mathbb{R} cone.

Next, let us study an example. Assume that the quadratic cone

$$x_4 \geq \sqrt{x_5^2 + x_8^2}$$

and the rotated quadratic cone

$$x_3 x_7 \geq x_1^2 + x_0^2, \quad x_3, x_7 \geq 0,$$

should be specified in the MPS file. One CSECTION is required for each cone and they are specified as follows:

```

*      1      2      3      4      5      6
*2345678901234567890123456789012345678901234567890
CSECTION      konea      0.0      QUAD
x4
x5
x8
CSECTION      koneb      0.0      RQUAD
x7
x3
x1
x0

```

This first CSECTION specifies the cone (14.3) which is given the name **konea**. This is a quadratic cone which is specified by the keyword **QUAD** in the CSECTION header. The 0.0 value in the CSECTION header is not used by the QUAD cone.

The second CSECTION specifies the rotated quadratic cone (14.4). Please note the keyword **RQUAD** in the CSECTION which is used to specify that the cone is a rotated quadratic cone instead of a quadratic cone. The 0.0 value in the CSECTION header is not used by the RQUAD cone.

In general, a CSECTION header has the format

CSECTION	[kname1]	[value1]	[ktype]
----------	----------	----------	---------

where the requirement for each field are as follows:

Field	Starting Position	Max Width	Required	Description
[kname1]	5	8	Yes	Name of the cone
[value1]	15	12	No	Cone parameter
[ktype]	25		Yes	Type of the cone.

The possible cone type keys are:

Cone type key	Members	Interpretation.
QUAD	≤ 1	Quadratic cone i.e. (14.3).
RQUAD	≤ 2	Rotated quadratic cone i.e. (14.4).

Please note that a quadratic cone must have at least one member whereas a rotated quadratic cone must have at least two members. A record in the CSECTION has the format

[vname1]

where the requirements for each field are

Field	Starting Position	Max Width	required	Description
[vname1]	2	8	Yes	A valid variable name

The most important restriction with respect to the CSECTION is that a variable must occur in only one CSECTION.

14.2.5 ENDATA

This keyword denotes the end of the MPS file.

14.2.6 Integer Variables

Using special bound keys in the BOUNDS section it is possible to specify that some or all of the variables should be integer-constrained i.e. be members of \mathcal{J} . However, an alternative method is available.

This method is available only for backward compatibility and we recommend that it is not used. This method requires that markers are placed in the COLUMNS section as in the example:

COLUMNS				
x1	obj	-10.0	c1	0.7
x1	c2	0.5	c3	1.0
x1	c4	0.1		
* Start of integer-constrained variables.				
MARK000	'MARKER'		'INTORG'	
x2	obj	-9.0	c1	1.0
x2	c2	0.8333333333	c3	0.66666667
x2	c4	0.25		
x3	obj	1.0	c6	2.0
MARK001	'MARKER'		'INTEND'	

- End of integer-constrained variables.

Please note that special marker lines are used to indicate the start and the end of the integer variables. Furthermore be aware of the following

- **IMPORTANT:** All variables between the markers are assigned a default lower bound of 0 and a default upper bound of 1. **This may not be what is intended.** If it is not intended, the correct bounds should be defined in the BOUNDS section of the MPS formatted file.
- **MOSEK** ignores field 1, i.e. MARK0001 and MARK001, however, other optimization systems require them.
- Field 2, i.e. **MARKER**, must be specified including the single quotes. This implies that no row can be assigned the name **MARKER**.
- Field 3 is ignored and should be left blank.
- Field 4, i.e. **INTORG** and **INTEND**, must be specified.
- It is possible to specify several such integer marker sections within the COLUMNS section.

14.2.7 General Limitations

- An MPS file should be an ASCII file.

14.2.8 Interpretation of the MPS Format

Several issues related to the MPS format are not well-defined by the industry standard. However, **MOSEK** uses the following interpretation:

- If a matrix element in the COLUMNS section is specified multiple times, then the multiple entries are added together.

- If a matrix element in a QSECTION section is specified multiple times, then the multiple entries are added together.

14.2.9 The Free MPS Format

MOSEK supports a free format variation of the MPS format. The free format is similar to the MPS file format but less restrictive, e.g. it allows longer names. However, it also presents two main limitations:

- A name must not contain any blanks.
- By default a line in the MPS file must not contain more than 1024 characters. However, by modifying the parameter `MSK_IPAR_READ_MPS_WIDTH` an arbitrary large line width will be accepted.

To use the free MPS format instead of the default MPS format the MOSEK parameter `MSK_IPAR_READ_MPS_FORMAT` should be changed.

14.3 The OPF Format

The *Optimization Problem Format (OPF)* is an alternative to LP and MPS files for specifying optimization problems. It is row-oriented, inspired by the CPLEX LP format.

Apart from containing objective, constraints, bounds etc. it may contain complete or partial solutions, comments and extra information relevant for solving the problem. It is designed to be easily read and modified by hand and to be forward compatible with possible future extensions.

Intended use

The OPF file format is meant to replace several other files:

- The LP file format: Any problem that can be written as an LP file can be written as an OPF file too; furthermore it naturally accommodates ranged constraints and variables as well as arbitrary characters in names, fixed expressions in the objective, empty constraints, and conic constraints.
- Parameter files: It is possible to specify integer, double and string parameters along with the problem (or in a separate OPF file).
- Solution files: It is possible to store a full or a partial solution in an OPF file and later reload it.

14.3.1 The File Format

The format uses tags to structure data. A simple example with the basic sections may look like this:

```
[comment]
This is a comment. You may write almost anything here...
[/comment]

# This is a single-line comment.

[objective min 'myobj']
x + 3 y + x^2 + 3 y^2 + z + 1
[/objective]

[constraints]
[con 'con01'] 4 <= x + y  [/con]
[/constraints]

[bounds]
[b] -10 <= x,y <= 10  [/b]
```

```
[cone quad] x,y,z [/cone]
[/bounds]
```

A scope is opened by a tag of the form `[tag]` and closed by a tag of the form `[/tag]`. An opening tag may accept a list of unnamed and named arguments, for examples:

```
[tag value] tag with one unnamed argument [/tag]
[tag arg=value] tag with one named argument in quotes [/tag]
```

Unnamed arguments are identified by their order, while named arguments may appear in any order, but never before an unnamed argument. The `value` can be a quoted, single-quoted or double-quoted text string, i.e.

```
[tag 'value']      single-quoted value [/tag]
[tag arg='value']  single-quoted value [/tag]
[tag "value"]     double-quoted value [/tag]
[tag arg="value"] double-quoted value [/tag]
```

Sections

The recognized tags are

`[comment]`

A comment section. This can contain *almost* any text: Between single quotes (') or double quotes (") any text may appear. Outside quotes the markup characters ([and]) must be prefixed by backslashes. Both single and double quotes may appear alone or inside a pair of quotes if it is prefixed by a backslash.

`[objective]`

The objective function: This accepts one or two parameters, where the first one (in the above example `min`) is either `min` or `max` (regardless of case) and defines the objective sense, and the second one (above `myobj`), if present, is the objective name. The section may contain linear and quadratic expressions. If several objectives are specified, all but the last are ignored.

`[constraints]`

This does not directly contain any data, but may contain the subsection `con` defining a linear constraint.

`[con]` defines a single constraint; if an argument is present (`[con NAME]`) this is used as the name of the constraint, otherwise it is given a null-name. The section contains a constraint definition written as linear and quadratic expressions with a lower bound, an upper bound, with both or with an equality. Examples:

```
[constraints]
[con 'con1'] 0 <= x + y      [/con]
[con 'con2'] 0 >= x + y      [/con]
[con 'con3'] 0 <= x + y <= 10 [/con]
[con 'con4']      x + y  = 10 [/con]
[/constraints]
```

Constraint names are unique. If a constraint is specified which has the same name as a previously defined constraint, the new constraint replaces the existing one.

[bounds]

This does not directly contain any data, but may contain the subsections **b** (linear bounds on variables) and **cone** (quadratic cone).

[b]. Bound definition on one or several variables separated by comma (,). An upper or lower bound on a variable replaces any earlier defined bound on that variable. If only one bound (upper or lower) is given only this bound is replaced. This means that upper and lower bounds can be specified separately. So the OPF bound definition:

```
[b]  x,y >= -10  [/b]
[b]  x,y <= 10   [/b]
```

results in the bound $-10 \leq x, y \leq 10$.

[cone]. currently supports the *quadratic cone* and the *rotated quadratic cone*.

A conic constraint is defined as a set of variables which belong to a single unique cone.

- A quadratic cone of n variables x_1, \dots, x_n defines a constraint of the form

$$x_1^2 \geq \sum_{i=2}^n x_i^2, \quad x_1 \geq 0.$$

- A rotated quadratic cone of n variables x_1, \dots, x_n defines a constraint of the form

$$2x_1x_2 \geq \sum_{i=3}^n x_i^2, \quad x_1, x_2 \geq 0.$$

A [bounds]-section example:

```
[bounds]
[b]  0 <= x,y <= 10  [/b] # ranged bound
[b]  10 >= x,y >= 0  [/b] # ranged bound
[b]  0 <= x,y <= inf [/b] # using inf
[b]      x,y free    [/b] # free variables
# Let (x,y,z,w) belong to the cone K
[cone quad] x,y,z,w [/cone] # quadratic cone
[cone rquad] x,y,z,w [/cone] # rotated quadratic cone
[/bounds]
```

By default all variables are free.

[variables]

This defines an ordering of variables as they should appear in the problem. This is simply a space-separated list of variable names. Optionally, an attribute can be added [variables disallow_new_variables] indicating that if any variable not listed here occurs later in the file it is an error.

[integer]

This contains a space-separated list of variables and defines the constraint that the listed variables must be integer values.

[hints]

This may contain only non-essential data; for example estimates of the number of variables, constraints and non-zeros. Placed before all other sections containing data this may reduce the time spent reading the file.

In the `hints` section, any subsection which is not recognized by **MOSEK** is simply ignored. In this section a hint in a subsection is defined as follows:

```
[hint ITEM] value [/hint]
```

where ITEM may be replaced by `numvar` (number of variables), `numcon` (number of linear/quadratic constraints), `numanz` (number of linear non-zeros in constraints) and `numqnz` (number of quadratic non-zeros in constraints).

[solutions]

This section can contain a set of full or partial solutions to a problem. Each solution must be specified using a `[solution]`-section, i.e.

```
[solutions]
[solution]...[/solution] #solution 1
[solution]...[/solution] #solution 2
#other solutions....
[solution]...[/solution] #solution n
[/solutions]
```

Note that a `[solution]`-section must be always specified inside a `[solutions]`-section. The syntax of a `[solution]`-section is the following:

```
[solution SOLTYPE status=STATUS]...[/solution]
```

where SOLTYPE is one of the strings

- `interior`, a non-basic solution,
- `basic`, a basic solution,
- `integer`, an integer solution,

and STATUS is one of the strings

- `UNKNOWN`,
- `OPTIMAL`,
- `INTEGER_OPTIMAL`,
- `PRIM_FEAS`,
- `DUAL_FEAS`,
- `PRIM_AND_DUAL_FEAS`,
- `NEAR_OPTIMAL`,
- `NEAR_PRIM_FEAS`,
- `NEAR_DUAL_FEAS`,
- `NEAR_PRIM_AND_DUAL_FEAS`,
- `PRIM_INFEAS_CER`,
- `DUAL_INFEAS_CER`,
- `NEAR_PRIM_INFEAS_CER`,

- NEAR_DUAL_INFEAS_CER,
- NEAR_INTEGER_OPTIMAL.

Most of these values are irrelevant for input solutions; when constructing a solution for simplex hot-start or an initial solution for a mixed integer problem the safe setting is UNKNOWN.

A [solution]-section contains [con] and [var] sections. Each [con] and [var] section defines solution information for a single variable or constraint, specified as list of KEYWORD/value pairs, in any order, written as

```
KEYWORD=value
```

Allowed keywords are as follows:

- **sk**. The status of the item, where the **value** is one of the following strings:
 - **LOW**, the item is on its lower bound.
 - **UPR**, the item is on its upper bound.
 - **FIX**, it is a fixed item.
 - **BAS**, the item is in the basis.
 - **SUPBAS**, the item is super basic.
 - **UNK**, the status is unknown.
 - **INF**, the item is outside its bounds (infeasible).
- **lvl** Defines the level of the item.
- **s1** Defines the level of the dual variable associated with its lower bound.
- **su** Defines the level of the dual variable associated with its upper bound.
- **sn** Defines the level of the variable associated with its cone.
- **y** Defines the level of the corresponding dual variable (for constraints only).

A [var] section should always contain the items **sk**, **lvl**, **s1** and **su**. Items **s1** and **su** are not required for **integer** solutions.

A [con] section should always contain **sk**, **lvl**, **s1**, **su** and **y**.

An example of a solution section

```
[solution basic status=UNKNOWN]
[var x0] sk=LOW    lvl=5.0    [/var]
[var x1] sk=UPR    lvl=10.0   [/var]
[var x2] sk=SUPBAS lvl=2.0    s1=1.5 su=0.0 [/var]

[con c0] sk=LOW    lvl=3.0 y=0.0 [/con]
[con c0] sk=UPR    lvl=0.0 y=5.0 [/con]
[/solution]
```

- **[vendor]** This contains solver/vendor specific data. It accepts one argument, which is a vendor ID – for **MOSEK** the ID is simply **mosek** – and the section contains the subsection **parameters** defining solver parameters. When reading a vendor section, any unknown vendor can be safely ignored. This is described later.

Comments using the **#** may appear anywhere in the file. Between the **#** and the following line-break any text may be written, including markup characters.

Numbers

Numbers, when used for parameter values or coefficients, are written in the usual way by the `printf` function. That is, they may be prefixed by a sign (+ or -) and may contain an integer part, decimal part and an exponent. The decimal point is always . (a dot). Some examples are

```
1
1.0
.0
1.
1e10
1e+10
1e-10
```

Some *invalid* examples are

```
e10    # invalid, must contain either integer or decimal part
.       # invalid
.e10   # invalid
```

More formally, the following standard regular expression describes numbers as used:

```
[+|-]?([0-9]+[.][0-9]*|.[0-9]+)([eE][+|-]?[0-9]+)?
```

Names

Variable names, constraint names and objective name may contain arbitrary characters, which in some cases must be enclosed by quotes (single or double) that in turn must be preceded by a backslash. Unquoted names must begin with a letter (a-z or A-Z) and contain only the following characters: the letters a-z and A-Z, the digits 0-9, braces { and } and underscore (_).

Some examples of legal names:

```
an_unquoted_name
another_name{123}
'single quoted name'
"double quoted name"
"name with \"quote\" in it"
"name with []s in it"
```

14.3.2 Parameters Section

In the `vendor` section solver parameters are defined inside the `parameters` subsection. Each parameter is written as

```
[p PARAMETER_NAME] value [/p]
```

where `PARAMETER_NAME` is replaced by a **MOSEK** parameter name, usually of the form `MSK_IPAR_...`, `MSK_DPAR_...` or `MSK_SPAR_...`, and the `value` is replaced by the value of that parameter; both integer values and named values may be used. Some simple examples are

```
[vendor mosek]
[parameters]
[p MSK_IPAR_OPF_MAX_TERMS_PER_LINE] 10      [/p]
[p MSK_IPAR_OPF_WRITE_PARAMETERS]   MSK_ON  [/p]
[p MSK_DPAR_DATA_TOL_BOUND_INF]     1.0e18  [/p]
[/parameters]
[/vendor]
```

14.3.3 Writing OPF Files from MOSEK

To write an OPF file set the parameter `MSK_IPAR_WRITE_DATA_FORMAT` to `MSK_DATA_FORMAT_OP` as this ensures that OPF format is used.

Then modify the following parameters to define what the file should contain:

<code>MSK_IPAR_OPF_WRITE_SOL_BAS</code>	Include basic solution, if defined.
<code>MSK_IPAR_OPF_WRITE_SOL_ITG</code>	Include integer solution, if defined.
<code>MSK_IPAR_OPF_WRITE_SOL_ITR</code>	Include interior solution, if defined.
<code>MSK_IPAR_OPF_WRITE_SOLUTIONS</code>	Include solutions if they are defined. If this is off, no solutions are included.
<code>MSK_IPAR_OPF_WRITE_HEADER</code>	Include a small header with comments.
<code>MSK_IPAR_OPF_WRITE_PROBLEM</code>	Include the problem itself — objective, constraints and bounds.
<code>MSK_IPAR_OPF_WRITE_PARAMETERS</code>	Include all parameter settings.
<code>MSK_IPAR_OPF_WRITE_HINTS</code>	Include hints about the size of the problem.

14.3.4 Examples

This section contains a set of small examples written in OPF and describing how to formulate linear, quadratic and conic problems.

Linear Example `lo1.opf`

Consider the example:

$$\begin{array}{llllll}
 \text{maximize} & 3x_0 & + & 1x_1 & + & 5x_2 & + & 1x_3 \\
 \text{subject to} & 3x_0 & + & 1x_1 & + & 2x_2 & & = & 30, \\
 & 2x_0 & + & 1x_1 & + & 3x_2 & + & 1x_3 & \geq & 15, \\
 & & & 2x_1 & & & + & 3x_3 & \leq & 25,
 \end{array}$$

having the bounds

$$\begin{array}{llll}
 0 & \leq & x_0 & \leq & \infty, \\
 0 & \leq & x_1 & \leq & 10, \\
 0 & \leq & x_2 & \leq & \infty, \\
 0 & \leq & x_3 & \leq & \infty.
 \end{array}$$

In the OPF format the example is displayed as shown in [Listing 14.1](#).

Listing 14.1: Example of an OPF file for a linear problem.

```

[comment]
  The lo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 4 [/hint]
  [hint NUMCON] 3 [/hint]
  [hint NUMANZ] 9 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4
[/variables]

[objective maximize 'obj']
  3 x1 + x2 + 5 x3 + x4
[/objective]
```

```
[constraints]
[con 'c1'] 3 x1 +   x2 + 2 x3           = 30 [/con]
[con 'c2'] 2 x1 +   x2 + 3 x3 +   x4 >= 15 [/con]
[con 'c3']           2 x2           + 3 x4 <= 25 [/con]
[/constraints]

[bounds]
[b] 0 <= * [/b]
[b] 0 <= x2 <= 10 [/b]
[/bounds]
```

Quadratic Example qo1.opf

An example of a quadratic optimization problem is

$$\begin{array}{ll}\text{minimize} & x_1^2 + 0.1x_2^2 + x_3^2 - x_1x_3 - x_2 \\ \text{subject to} & 1 \leq x_1 + x_2 + x_3, \\ & x \geq 0.\end{array}$$

This can be formulated in **opf** as shown below.

Listing 14.2: Example of an OPF file for a quadratic problem.

```
[comment]
  The qo1 example in OPF format
[/comment]

[hints]
[hint NUMVAR] 3 [/hint]
[hint NUMCON] 1 [/hint]
[hint NUMANZ] 3 [/hint]
[hint NUMQNZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3
[/variables]

[objective minimize 'obj']
  # The quadratic terms are often written with a factor of 1/2 as here,
  # but this is not required.

  - x2 + 0.5 ( 2.0 x1 ^ 2 - 2.0 x3 * x1 + 0.2 x2 ^ 2 + 2.0 x3 ^ 2 )
[/objective]

[constraints]
[con 'c1'] 1.0 <= x1 + x2 + x3 [/con]
[/constraints]

[bounds]
[b] 0 <= * [/b]
[/bounds]
```

Conic Quadratic Example `cqo1.opf`

Consider the example:

$$\begin{aligned}
 &\text{minimize} && x_3 + x_4 + x_5 \\
 &\text{subject to} && x_0 + x_1 + 2x_2 = 1, \\
 & && x_0, x_1, x_2 \geq 0, \\
 & && x_3 \geq \sqrt{x_0^2 + x_1^2}, \\
 & && 2x_4x_5 \geq x_2^2.
 \end{aligned}$$

Please note that the type of the cones is defined by the parameter to `[cone ...]`; the content of the `cone`-section is the names of variables that belong to the cone. The resulting OPF file is in [Listing 14.3](#).

Listing 14.3: Example of an OPF file for a conic quadratic problem.

```

[comment]
  The cqo1 example in OPF format.
[/comment]

[hints]
  [hint NUMVAR] 6 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4 x5 x6
[/variables]

[objective minimize 'obj']
  x4 + x5 + x6
[/objective]

[constraints]
  [con 'c1'] x1 + x2 + 2e+00 x3 = 1e+00 [/con]
[/constraints]

[bounds]
  # We let all variables default to the positive orthant
  [b] 0 <= * [/b]

  # ...and change those that differ from the default
  [b] x4,x5,x6 free [/b]

  # Define quadratic cone: x4 >= sqrt( x1^2 + x2^2 )
  [cone quad 'k1'] x4, x1, x2 [/cone]

  # Define rotated quadratic cone: 2 x5 x6 >= x3^2
  [cone rquad 'k2'] x5, x6, x3 [/cone]
[/bounds]

```

Mixed Integer Example `mil01.opf`

Consider the mixed integer problem:

$$\begin{aligned}
 &\text{maximize} && x_0 + 0.64x_1 \\
 &\text{subject to} && 50x_0 + 31x_1 \leq 250, \\
 & && 3x_0 - 2x_1 \geq -4, \\
 & && x_0, x_1 \geq 0 \quad \text{and integer}
 \end{aligned}$$

This can be implemented in OPF with the file in [Listing 14.4](#).

Listing 14.4: Example of an OPF file for a mixed-integer linear problem.

```

[comment]
  The milo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 2 [/hint]
  [hint NUMCON] 2 [/hint]
  [hint NUMANZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2
[/variables]

[objective maximize 'obj']
  x1 + 6.4e-1 x2
[/objective]

[constraints]
  [con 'c1'] 5e+1 x1 + 3.1e+1 x2 <= 2.5e+2 [/con]
  [con 'c2'] -4 <= 3 x1 - 2 x2 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]

[integer]
  x1 x2
[/integer]

```

14.4 The CBF Format

This document constitutes the technical reference manual of the *Conic Benchmark Format* with file extension: `.cbf` or `.CBF`. It unifies linear, second-order cone (also known as conic quadratic) and semidefinite optimization with mixed-integer variables. The format has been designed with benchmark libraries in mind, and therefore focuses on compact and easily parsable representations. The problem structure is separated from the problem data, and the format moreover facilitates benchmarking of hotstart capability through sequences of changes.

14.4.1 How Instances Are Specified

This section defines the spectrum of conic optimization problems that can be formulated in terms of the keywords of the CBF format.

In the CBF format, conic optimization problems are considered in the following form:

$$\begin{aligned}
 & \min / \max && g^{obj} \\
 \text{s.t.} &&& g_i \in \mathcal{K}_i, \quad i \in \mathcal{I}, \\
 &&& G_i \in \mathcal{K}_i, \quad i \in \mathcal{I}^{PSD}, \\
 &&& x_j \in \mathcal{K}_j, \quad j \in \mathcal{J}, \\
 &&& \overline{X}_j \in \mathcal{K}_j, \quad j \in \mathcal{J}^{PSD}.
 \end{aligned} \tag{14.5}$$

- **Variables** are either scalar variables, x_j for $j \in \mathcal{J}$, or variables, \overline{X}_j for $j \in \mathcal{J}^{PSD}$. Scalar variables can also be declared as integer.

- **Constraints** are affine expressions of the variables, either scalar-valued g_i for $i \in \mathcal{I}$, or matrix-valued G_i for $i \in \mathcal{I}^{PSD}$

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i.$$

- The **objective function** is a scalar-valued affine expression of the variables, either to be minimized or maximized. We refer to this expression as g^{obj}

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj}.$$

CBF format can represent the following cones \mathcal{K} :

- **Free domain** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n\}, \text{ for } n \geq 1.$$

- **Positive orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \geq 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \geq 1.$$

- **Negative orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \leq 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \geq 1.$$

- **Fixpoint zero** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j = 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \geq 1.$$

- **Quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R}^{n-1}, p^2 \geq x^T x, p \geq 0 \right\}, \text{ for } n \geq 2.$$

- **Rotated quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ q \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R} \times \mathbb{R}^{n-2}, 2pq \geq x^T x, p \geq 0, q \geq 0 \right\}, \text{ for } n \geq 3.$$

14.4.2 The Structure of CBF Files

This section defines how information is written in the CBF format, without being specific about the type of information being communicated.

All information items belong to exactly one of the three groups of information. These information groups, and the order they must appear in, are:

1. File format.
2. Problem structure.
3. Problem data.

The first group, file format, provides information on how to interpret the file. The second group, problem structure, provides the information needed to deduce the type and size of the problem instance. Finally, the third group, problem data, specifies the coefficients and constants of the problem instance.

Information items

The format is composed as a list of information items. The first line of an information item is the **KEYWORD**, revealing the type of information provided. The second line - of some keywords only - is the **HEADER**, typically revealing the size of information that follows. The remaining lines are the **BODY** holding the actual information to be specified.

KEYWORD
BODY
KEYWORD
HEADER
BODY

The **KEYWORD** determines how each line in the **HEADER** and **BODY** is structured. Moreover, the number of lines in the **BODY** follows either from the **KEYWORD**, the **HEADER**, or from another information item required to precede it.

Embedded hotstart-sequences

A sequence of problem instances, based on the same problem structure, is within a single file. This is facilitated via the **CHANGE** within the problem data information group, as a separator between the information items of each instance. The information items following a **CHANGE** keyword are appending to, or changing (e.g., setting coefficients back to their default value of zero), the problem data of the preceding instance.

The sequence is intended for benchmarking of hotstart capability, where the solvers can reuse their internal state and solution (subject to the achieved accuracy) as warmpoint for the succeeding instance. Whenever this feature is unsupported or undesired, the keyword **CHANGE** should be interpreted as the end of file.

File encoding and line width restrictions

The format is based on the US-ASCII printable character set with two extensions as listed below. Note, by definition, that none of these extensions can be misinterpreted as printable US-ASCII characters:

- A line feed marks the end of a line, carriage returns are ignored.
- Comment-lines may contain unicode characters in UTF-8 encoding.

The line width is restricted to 512 bytes, with 3 bytes reserved for the potential carriage return, line feed and null-terminator.

Integers and floating point numbers must follow the ISO C decimal string representation in the standard C locale. The format does not impose restrictions on the magnitude of, or number of significant digits in numeric data, but the use of 64-bit integers and 64-bit IEEE 754 floating point numbers should be sufficient to avoid loss of precision.

Comment-line and whitespace rules

The format allows single-line comments respecting the following rule:

- Lines having first byte equal to '#' (US-ASCII 35) are comments, and should be ignored. Comments are only allowed between information items.

Given that a line is not a comment-line, whitespace characters should be handled according to the following rules:

- Leading and trailing whitespace characters should be ignored.
 - The separator between multiple pieces of information on one line, is either one or more whitespace characters.
- Lines containing only whitespace characters are empty, and should be ignored. Empty lines are only allowed between information items.

14.4.3 Problem Specification

The problem structure

The problem structure defines the objective sense, whether it is minimization and maximization. It also defines the index sets, \mathcal{J} , \mathcal{J}^{PSD} , \mathcal{I} and \mathcal{I}^{PSD} , which are all numbered from zero, $\{0, 1, \dots\}$, and empty until explicitly constructed.

- **Scalar variables** are constructed in vectors restricted to a conic domain, such as $(x_0, x_1) \in \mathbb{R}_+^2$, $(x_2, x_3, x_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$x \in \mathcal{K}_1^{n_1} \times \mathcal{K}_2^{n_2} \times \dots \times \mathcal{K}_k^{n_k}$$

which in the CBF format becomes:

```
VAR
n k
K1 n1
K2 n2
...
Kk nk
```

where $\sum_i n_i = n$ is the total number of scalar variables. The list of supported cones is found in [Table 14.3](#). Integrality of scalar variables can be specified afterwards.

- **PSD variables** are constructed one-by-one. That is, $X_j \succeq \mathbf{0}^{n_j \times n_j}$ for $j \in \mathcal{J}^{PSD}$, constructs a matrix-valued variable of size $n_j \times n_j$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes:

```
PSDVAR
N
n1
n2
...
nN
```

where N is the total number of PSD variables.

- **Scalar constraints** are constructed in vectors restricted to a conic domain, such as $(g_0, g_1) \in \mathbb{R}_+^2$, $(g_2, g_3, g_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$g \in \mathcal{K}_1^{m_1} \times \mathcal{K}_2^{m_2} \times \dots \times \mathcal{K}_k^{m_k}$$

which in the CBF format becomes:

```

CON
m k
K1 m1
K2 m2
. .
Kk mk

```

where $\sum_i m_i = m$ is the total number of scalar constraints. The list of supported cones is found in Table 14.3.

- **PSD constraints** are constructed one-by-one. That is, $G_i \succeq \mathbf{0}^{m_i \times m_i}$ for $i \in \mathcal{I}^{PSD}$, constructs a matrix-valued affine expressions of size $m_i \times m_i$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes

```

PSDCON
M
m1
m2
. .
mM

```

where M is the total number of PSD constraints.

With the objective sense, variables (with integer indications) and constraints, the definitions of the many affine expressions follow in problem data.

Problem data

The problem data defines the coefficients and constants of the affine expressions of the problem instance. These are considered zero until explicitly defined, implying that instances with no keywords from this information group are, in fact, valid. Duplicating or conflicting information is a failure to comply with the standard. Consequently, two coefficients written to the same position in a matrix (or to transposed positions in a symmetric matrix) is an error.

The affine expressions of the objective, g^{obj} , of the scalar constraints, g_i , and of the PSD constraints, G_i , are defined separately. The following notation uses the standard trace inner product for matrices, $\langle X, Y \rangle = \sum_{i,j} X_{ij} Y_{ij}$.

- The affine expression of the objective is defined as

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj},$$

in terms of the symmetric matrices, F_j^{obj} , and scalars, a_j^{obj} and b^{obj} .

- The affine expressions of the scalar constraints are defined, for $i \in \mathcal{I}$, as

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

in terms of the symmetric matrices, F_{ij} , and scalars, a_{ij} and b_i .

- The affine expressions of the PSD constraints are defined, for $i \in \mathcal{I}^{PSD}$, as

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i,$$

in terms of the symmetric matrices, H_{ij} and D_i .

List of cones

The format uses an explicit syntax for symmetric positive semidefinite cones as shown above. For scalar variables and constraints, constructed in vectors, the supported conic domains and their minimum sizes are given as follows.

Table 14.3: Cones available in the CBF format

Name	CBF keyword	Cone family
Free domain	F	linear
Positive orthant	L+	linear
Negative orthant	L-	linear
Fixpoint zero	L=	linear
Quadratic cone	Q	second-order
Rotated quadratic cone	QR	second-order

14.4.4 File Format Keywords

VER

Description: The version of the Conic Benchmark Format used to write the file.

HEADER: None

BODY: One line formatted as:

INT

This is the version number.

Must appear exactly once in a file, as the first keyword.

OBJSENSE

Description: Define the objective sense.

HEADER: None

BODY: One line formatted as:

STR

having MIN indicates minimize, and MAX indicates maximize. Capital letters are required.

Must appear exactly once in a file.

PSDVAR

Description: Construct the PSD variables.

HEADER: One line formatted as:

INT

This is the number of PSD variables in the problem.

BODY: A list of lines formatted as:

INT

This indicates the number of rows (equal to the number of columns) in the matrix-valued PSD variable. The number of lines should match the number stated in the header.

VAR

Description: Construct the scalar variables.

HEADER: One line formatted as:

INT INT

This is the number of scalar variables, followed by the number of conic domains they are restricted to.

BODY: A list of lines formatted as:

STR INT

This indicates the cone name (see [Table 14.3](#)), and the number of scalar variables restricted to this cone. These numbers should add up to the number of scalar variables stated first in the header. The number of lines should match the second number stated in the header.

INT

Description: Declare integer requirements on a selected subset of scalar variables.

HEADER: one line formatted as:

INT

This is the number of integer scalar variables in the problem.

BODY: a list of lines formatted as:

INT

This indicates the scalar variable index $j \in \mathcal{J}$. The number of lines should match the number stated in the header.

Can only be used after the keyword **VAR**.

PSDCON

Description: Construct the PSD constraints.

HEADER: One line formatted as:

INT

This is the number of PSD constraints in the problem.

BODY: A list of lines formatted as:

INT

This indicates the number of rows (equal to the number of columns) in the matrix-valued affine expression of the PSD constraint. The number of lines should match the number stated in the header.

Can only be used after these keywords: **PSDVAR**, **VAR**.

CON

Description: Construct the scalar constraints.

HEADER: One line formatted as:

INT INT

This is the number of scalar constraints, followed by the number of conic domains they restrict to.

BODY: A list of lines formatted as:

STR INT

This indicates the cone name (see [Table 14.3](#)), and the number of affine expressions restricted to this cone. These numbers should add up to the number of scalar constraints stated first in the header. The number of lines should match the second number stated in the header.

Can only be used after these keywords: PSDVAR, VAR

OBJFCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices F_j^{obj} , as used in the objective.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT REAL

This indicates the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

OBJACOORD

Description: Input sparse coordinates (pairs) to define the scalars, a_j^{obj} , as used in the objective.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT REAL

This indicates the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

OBJBCOORD

Description: Input the scalar, b^{obj} , as used in the objective.

HEADER: None.

BODY: One line formatted as:

REAL

This indicates the coefficient value.

FCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, F_{ij} , as used in the scalar constraints.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT INT REAL

This indicates the scalar constraint index $i \in \mathcal{I}$, the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

ACOORD

Description: Input sparse coordinates (triplets) to define the scalars, a_{ij} , as used in the scalar constraints.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT REAL

This indicates the scalar constraint index $i \in \mathcal{I}$, the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

BCOORD

Description: Input sparse coordinates (pairs) to define the scalars, b_i , as used in the scalar constraints.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT REAL

This indicates the scalar constraint index $i \in \mathcal{I}$ and the coefficient value. The number of lines should match the number stated in the header.

HCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, H_{ij} , as used in the PSD constraints.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as

INT INT INT INT REAL

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the scalar variable index $j \in \mathcal{J}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

DCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices, D_i , as used in the PSD constraints.

HEADER: One line formatted as

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT REAL

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

CHANGE

Start of a new instance specification based on changes to the previous. Can be interpreted as the end of file when the hotstart-sequence is unsupported or undesired.

BODY: None

Header: None

14.4.5 CBF Format Examples

Minimal Working Example

The conic optimization problem (14.6), has three variables in a quadratic cone - first one is integer - and an affine expression in domain 0 (equality constraint).

$$\begin{aligned} &\text{minimize} && 5.1 x_0 \\ &\text{subject to} && 6.2 x_1 + 7.3 x_2 - 8.4 \in \{0\} \\ &&& x \in \mathcal{Q}^3, x_0 \in \mathbb{Z}. \end{aligned} \tag{14.6}$$

Its formulation in the Conic Benchmark Format begins with the version of the CBF format used, to safeguard against later revisions.

```
VER
1
```

Next follows the problem structure, consisting of the objective sense, the number and domain of variables, the indices of integer variables, and the number and domain of scalar-valued affine expressions (i.e., the equality constraint).

```
OBJSENSE
MIN

VAR
3 1
Q 3

INT
1
0

CON
1 1
L= 1
```

Finally follows the problem data, consisting of the coefficients of the objective, the coefficients of the constraints, and the constant terms of the constraints. All data is specified on a sparse coordinate form.

```
OBJCOORD
1
0 5.1

ACCOORD
2
0 1 6.2
0 2 7.3

BCCOORD
1
0 -8.4
```

This concludes the example.

Mixing Linear, Second-order and Semidefinite Cones

The conic optimization problem (14.7), has a semidefinite cone, a quadratic cone over unordered subindices, and two equality constraints.

$$\begin{aligned}
 & \text{minimize} && \left\langle \begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}, X_1 \right\rangle + x_1 \\
 & \text{subject to} && \left\langle \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 &= 1.0, \\
 & && \left\langle \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, X_1 \right\rangle + x_0 + x_2 &= 0.5, \\
 & && x_1 \geq \sqrt{x_0^2 + x_2^2}, \\
 & && X_1 \succeq \mathbf{0}.
 \end{aligned} \tag{14.7}$$

The equality constraints are easily rewritten to the conic form, $(g_0, g_1) \in \{0\}^2$, by moving constants such that the right-hand-side becomes zero. The quadratic cone does not fit under the **VAR** keyword in this variable permutation. Instead, it takes a scalar constraint $(g_2, g_3, g_4) = (x_1, x_0, x_2) \in \mathcal{Q}^3$, with scalar

variables constructed as $(x_0, x_1, x_2) \in \mathbb{R}^3$. Its formulation in the CBF format is reported in the following list

```
# File written using this version of the Conic Benchmark Format:
#   | Version 1.
VER
1

# The sense of the objective is:
#   | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#   | Three times three.
PSDVAR
1
3

# Three scalar variables in this one conic domain:
#   | Three are free.
VAR
3 1
F 3

# Five scalar constraints with affine expressions in two conic domains:
#   | Two are fixed to zero.
#   | Three are in conic quadratic domain.
CON
5 2
L= 2
Q 3

# Five coordinates in F~{obj}_j coefficients:
#   | F~{obj}[0][0,0] = 2.0
#   | F~{obj}[0][1,0] = 1.0
#   | and more...
OBJFCOORD
5
0 0 0 2.0
0 1 0 1.0
0 1 1 2.0
0 2 1 1.0
0 2 2 2.0

# One coordinate in a~{obj}_j coefficients:
#   | a~{obj}[1] = 1.0
OBJACOORD
1
1 1.0

# Nine coordinates in F_ij coefficients:
#   | F[0,0][0,0] = 1.0
#   | F[0,0][1,1] = 1.0
#   | and more...
FCOORD
9
0 0 0 0 1.0
0 0 1 1 1.0
0 0 2 2 1.0
1 0 0 0 1.0
1 0 1 0 1.0
1 0 2 0 1.0
```

```

1 0 1 1 1.0
1 0 2 1 1.0
1 0 2 2 1.0

# Six coordinates in a_ij coefficients:
#   | a[0,1] = 1.0
#   | a[1,0] = 1.0
#   | and more...
ACCOORD
6
0 1 1.0
1 0 1.0
1 2 1.0
2 1 1.0
3 0 1.0
4 2 1.0

# Two coordinates in b_i coefficients:
#   | b[0] = -1.0
#   | b[1] = -0.5
BCCOORD
2
0 -1.0
1 -0.5

```

Mixing Semidefinite Variables and Linear Matrix Inequalities

The standard forms in semidefinite optimization are usually based either on semidefinite variables or linear matrix inequalities. In the CBF format, both forms are supported and can even be mixed as shown in.

$$\begin{aligned}
& \text{minimize} && \left\langle \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 + x_2 + 1 \\
& \text{subject to} && \left\langle \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, X_1 \right\rangle - x_1 - x_2 \geq 0.0, \\
& && x_1 \begin{bmatrix} 0 & 1 \\ 1 & 3 \end{bmatrix} + x_2 \begin{bmatrix} 3 & 1 \\ 1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \succeq \mathbf{0}, \\
& && X_1 \succeq \mathbf{0}.
\end{aligned} \tag{14.8}$$

Its formulation in the CBF format is written in what follows

```

# File written using this version of the Conic Benchmark Format:
#   | Version 1.
VER
1

# The sense of the objective is:
#   | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#   | Two times two.
PSDVAR
1
2

# Two scalar variables in this one conic domain:
#   | Two are free.
VAR
2 1

```

```

F 2

# One PSD constraint of this size:
#   | Two times two.
PSDCON
1
2

# One scalar constraint with an affine expression in this one conic domain:
#   | One is greater than or equal to zero.
CON
1 1
L+ 1

# Two coordinates in  $F^{\text{obj}}_j$  coefficients:
#   |  $F^{\text{obj}}[0][0,0] = 1.0$ 
#   |  $F^{\text{obj}}[0][1,1] = 1.0$ 
OBJFCOORD
2
0 0 0 1.0
0 1 1 1.0

# Two coordinates in  $a^{\text{obj}}_j$  coefficients:
#   |  $a^{\text{obj}}[0] = 1.0$ 
#   |  $a^{\text{obj}}[1] = 1.0$ 
OBJACOORD
2
0 1.0
1 1.0

# One coordinate in  $b^{\text{obj}}$  coefficient:
#   |  $b^{\text{obj}} = 1.0$ 
OBJBCOORD
1.0

# One coordinate in  $F_{ij}$  coefficients:
#   |  $F[0,0][1,0] = 1.0$ 
FCOORD
1
0 0 1 0 1.0

# Two coordinates in  $a_{ij}$  coefficients:
#   |  $a[0,0] = -1.0$ 
#   |  $a[0,1] = -1.0$ 
ACCOORD
2
0 0 -1.0
0 1 -1.0

# Four coordinates in  $H_{ij}$  coefficients:
#   |  $H[0,0][1,0] = 1.0$ 
#   |  $H[0,0][1,1] = 3.0$ 
#   | and more...
HCOORD
4
0 0 1 0 1.0
0 0 1 1 3.0
0 1 0 0 3.0
0 1 1 0 1.0

# Two coordinates in  $D_i$  coefficients:
#   |  $D[0][0,0] = -1.0$ 
#   |  $D[0][1,1] = -1.0$ 

```

```
DCOORD
2
0 0 0 -1.0
0 1 1 -1.0
```

Optimization Over a Sequence of Objectives

The linear optimization problem (14.9), is defined for a sequence of objectives such that hotstarting from one to the next might be advantages.

$$\begin{aligned} & \text{maximize}_k && g_k^{obj} \\ & \text{subject to} && 50x_0 + 31 \leq 250, \\ & && 3x_0 - 2x_1 \geq -4, \\ & && x \in \mathbb{R}_+^2, \end{aligned} \tag{14.9}$$

given,

1. $g_0^{obj} = x_0 + 0.64x_1$.
2. $g_1^{obj} = 1.11x_0 + 0.76x_1$.
3. $g_2^{obj} = 1.11x_0 + 0.85x_1$.

Its formulation in the CBF format is reported in Listing 14.5.

Listing 14.5: Problem (14.9) in CBF format.

```
# File written using this version of the Conic Benchmark Format:
#   | Version 1.
VER
1

# The sense of the objective is:
#   | Maximize.
OBJSENSE
MAX

# Two scalar variables in this one conic domain:
#   | Two are nonnegative.
VAR
2 1
L+ 2

# Two scalar constraints with affine expressions in these two conic domains:
#   | One is in the nonpositive domain.
#   | One is in the nonnegative domain.
CON
2 2
L- 1
L+ 1

# Two coordinates in a^{obj}_j coefficients:
#   | a^{obj}[0] = 1.0
#   | a^{obj}[1] = 0.64
OBJCOORD
2
0 1.0
1 0.64

# Four coordinates in a_ij coefficients:
#   | a[0,0] = 50.0
#   | a[1,0] = 3.0
```

```

#      | and more...
ACCOORD
4
0 0 50.0
1 0 3.0
0 1 31.0
1 1 -2.0

# Two coordinates in b_i coefficients:
#      | b[0] = -250.0
#      | b[1] = 4.0
BCCOORD
2
0 -250.0
1 4.0

# New problem instance defined in terms of changes.
CHANGE

# Two coordinate changes in a^{obj}_j coefficients. Now it is:
#      | a^{obj}[0] = 1.11
#      | a^{obj}[1] = 0.76
OBJACCOORD
2
0 1.11
1 0.76

# New problem instance defined in terms of changes.
CHANGE

# One coordinate change in a^{obj}_j coefficients. Now it is:
#      | a^{obj}[0] = 1.11
#      | a^{obj}[1] = 0.85
OBJACCOORD
1
1 0.85

```

14.5 The XML (OSiL) Format

MOSEK can write data in the standard OSiL xml format. For a definition of the OSiL format please see <http://www.optimizationservices.org/>.

Only linear constraints (possibly with integer variables) are supported. By default output files with the extension `.xml` are written in the OSiL format.

The parameter `MSK_IPAR_WRITE_XML_MODE` controls if the linear coefficients in the A matrix are written in row or column order.

14.6 The Task Format

The Task format is **MOSEK**'s native binary format. It contains a complete image of a **MOSEK** task, i.e.

- Problem data: Linear, conic quadratic, semidefinite and quadratic data
- Problem item names: Variable names, constraints names, cone names etc.
- Parameter settings
- Solutions

There are a few things to be aware of:

- The task format *does not* support General Convex problems since these are defined by arbitrary user-defined functions.
- Status of a solution read from a file will *always* be unknown.
- Parameter settings in a task file *always override* any parameters set on the command line or in a parameter file.

The format is based on the *TAR* (USTar) file format. This means that the individual pieces of data in a `.task` file can be examined by unpacking it as a *TAR* file. Please note that the inverse may not work: Creating a file using *TAR* will most probably not create a valid **MOSEK** Task file since the order of the entries is important.

14.7 The JSON Format

MOSEK provides the possibility to read/write problems in valid JSON format.

JSON (JavaScript Object Notation) is a lightweight data-interchange format. It is easy for humans to read and write. It is easy for machines to parse and generate. It is based on a subset of the JavaScript Programming Language, Standard ECMA-262 3rd Edition - December 1999. JSON is a text format that is completely language independent but uses conventions that are familiar to programmers of the C-family of languages, including C, C++, C#, Java, JavaScript, Perl, Python, and many others. These properties make JSON an ideal data-interchange language.

The official JSON website <http://www.json.org> provides plenty of information along with the format definition.

MOSEK defines two JSON-like formats:

- *jtask*
- *jsol*

Warning: Despite being text-based human-readable formats, *jtask* and *jsol* files will include no indentation and no new-lines, in order to keep the files as compact as possible. We therefore strongly advise to use JSON viewer tools to inspect *jtask* and *jsol* files.

14.7.1 *jtask* format

It stores a problem instance. The *jtask* format contains the same information as a *task format*.

Even though a *jtask* file is human-readable, we do not recommend users to create it by hand, but to rely on **MOSEK**.

14.7.2 *jsol* format

It stores a problem solution. The *jsol* format contains all solutions and information items.

14.7.3 A *jtask* example

In [Listing 14.6](#) we present a file in the *jtask* format that corresponds to the sample problem from `1o1.1p`. The listing has been formatted for readability.

Listing 14.6: A formatted *jtask* file for the *lo1.lp* example.

```

{
  "$schema": "http://mosek.com/json/schema#",
  "Task/INFO": {
    "taskname": "lo1",
    "numvar": 4,
    "numcon": 3,
    "numcone": 0,
    "numbarvar": 0,
    "numanz": 9,
    "numsymmat": 0,
    "mosekver": [
      8,
      0,
      0,
      9
    ]
  },
  "Task/data": {
    "var": {
      "name": [
        "x1",
        "x2",
        "x3",
        "x4"
      ],
      "bk": [
        "lo",
        "ra",
        "lo",
        "lo"
      ],
      "b1": [
        0.0,
        0.0,
        0.0,
        0.0
      ],
      "bu": [
        1e+30,
        1e+1,
        1e+30,
        1e+30
      ],
      "type": [
        "cont",
        "cont",
        "cont",
        "cont"
      ]
    },
    "con": {
      "name": [
        "c1",
        "c2",
        "c3"
      ],
      "bk": [
        "fx",
        "lo",
        "up"
      ]
    }
  }
}

```

```
    ],
    "bl": [
        3e+1,
        1.5e+1,
        -1e+30
    ],
    "bu": [
        3e+1,
        1e+30,
        2.5e+1
    ]
},
"objective": {
    "sense": "max",
    "name": "obj",
    "c": {
        "subj": [
            0,
            1,
            2,
            3
        ],
        "val": [
            3e+0,
            1e+0,
            5e+0,
            1e+0
        ]
    }
},
"cfix": 0.0
},
"A": {
    "subi": [
        0,
        0,
        0,
        1,
        1,
        1,
        1,
        2,
        2
    ],
    "subj": [
        0,
        1,
        2,
        0,
        1,
        2,
        3,
        1,
        3
    ],
    "val": [
        3e+0,
        1e+0,
        2e+0,
        2e+0,
        1e+0,
        3e+0,
        1e+0,
        2e+0,
```

```

        3e+0
    ]
}
},
"Task/parameters":{
  "iparam":{
    "ANA_SOL_BASIS":"ON",
    "ANA_SOL_PRINT_VIOLATED":"OFF",
    "AUTO_SORT_A_BEFORE_OPT":"OFF",
    "AUTO_UPDATE_SOL_INFO":"OFF",
    "BASIS_SOLVE_USE_PLUS_ONE":"OFF",
    "BI_CLEAN_OPTIMIZER":"OPTIMIZER_FREE",
    "BI_IGNORE_MAX_ITER":"OFF",
    "BI_IGNORE_NUM_ERROR":"OFF",
    "BI_MAX_ITERATIONS":1000000,
    "CACHE_LICENSE":"ON",
    "CHECK_CONVEXITY":"CHECK_CONVEXITY_FULL",
    "COMPRESS_STATFILE":"ON",
    "CONCURRENT_NUM_OPTIMIZERS":2,
    "CONCURRENT_PRIORITY_DUAL_SIMPLEX":2,
    "CONCURRENT_PRIORITY_FREE_SIMPLEX":3,
    "CONCURRENT_PRIORITY_INTPNT":4,
    "CONCURRENT_PRIORITY_PRIMAL_SIMPLEX":1,
    "FEASREPAIR_OPTIMIZE":"FEASREPAIR_OPTIMIZE_NONE",
    "INFEAS_GENERIC_NAMES":"OFF",
    "INFEAS_PREFER_PRIMAL":"ON",
    "INFEAS_REPORT_AUTO":"OFF",
    "INFEAS_REPORT_LEVEL":1,
    "INTPNT_BASIS":"BI_ALWAYS",
    "INTPNT_DIFF_STEP":"ON",
    "INTPNT_FACTOR_DEBUG_LVL":0,
    "INTPNT_FACTOR_METHOD":0,
    "INTPNT_HOTSTART":"INTPNT_HOTSTART_NONE",
    "INTPNT_MAX_ITERATIONS":400,
    "INTPNT_MAX_NUM_COR":-1,
    "INTPNT_MAX_NUM_REFINEMENT_STEPS":-1,
    "INTPNT_OFF_COL_TRH":40,
    "INTPNT_ORDER_METHOD":"ORDER_METHOD_FREE",
    "INTPNT_REGULARIZATION_USE":"ON",
    "INTPNT_SCALING":"SCALING_FREE",
    "INTPNT_SOLVE_FORM":"SOLVE_FREE",
    "INTPNT_STARTING_POINT":"STARTING_POINT_FREE",
    "LIC_TRH_EXPIRY_WRN":7,
    "LICENSE_DEBUG":"OFF",
    "LICENSE_PAUSE_TIME":0,
    "LICENSE_SUPPRESS_EXPIRE_WRNS":"OFF",
    "LICENSE_WAIT":"OFF",
    "LOG":10,
    "LOG_ANA_PRO":1,
    "LOG_BI":4,
    "LOG_BI_FREQ":2500,
    "LOG_CHECK_CONVEXITY":0,
    "LOG_CONCURRENT":1,
    "LOG_CUT_SECOND_OPT":1,
    "LOG_EXPAND":0,
    "LOG_FACTOR":1,
    "LOG_FEAS_REPAIR":1,
    "LOG_FILE":1,
    "LOG_HEAD":1,
    "LOG_INFEAS_ANA":1,
    "LOG_INTPNT":4,
    "LOG_MIO":4,
    "LOG_MIO_FREQ":1000,

```

```

"LOG_OPTIMIZER":1,
"LOG_ORDER":1,
"LOG_PRESOLVE":1,
"LOG_RESPONSE":0,
"LOG_SENSITIVITY":1,
"LOG_SENSITIVITY_OPT":0,
"LOG_SIM":4,
"LOG_SIM_FREQ":1000,
"LOG_SIM_MINOR":1,
"LOG_STORAGE":1,
"MAX_NUM_WARNINGS":10,
"MIO_BRANCH_DIR":"BRANCH_DIR_FREE",
"MIO_CONSTRUCT_SOL":"OFF",
"MIO_CUT_CLIQUE":"ON",
"MIO_CUT_CMIR":"ON",
"MIO_CUT_GMI":"ON",
"MIO_CUT_KNAPSACK_COVER":"OFF",
"MIO_HEURISTIC_LEVEL":-1,
"MIO_MAX_NUM_BRANCHES":-1,
"MIO_MAX_NUM_RELAXS":-1,
"MIO_MAX_NUM_SOLUTIONS":-1,
"MIO_MODE":"MIO_MODE_SATISFIED",
"MIO_MT_USER_CB":"ON",
"MIO_NODE_OPTIMIZER":"OPTIMIZER_FREE",
"MIO_NODE_SELECTION":"MIO_NODE_SELECTION_FREE",
"MIO_PERSPECTIVE_REFORMULATE":"ON",
"MIO_PROBING_LEVEL":-1,
"MIO_RINS_MAX_NODES":-1,
"MIO_ROOT_OPTIMIZER":"OPTIMIZER_FREE",
"MIO_ROOT_REPEAT_PRESOLVE_LEVEL":-1,
"MT_SPINCOUNT":0,
"NUM_THREADS":0,
"OPF_MAX_TERMS_PER_LINE":5,
"OPF_WRITE_HEADER":"ON",
"OPF_WRITE_HINTS":"ON",
"OPF_WRITE_PARAMETERS":"OFF",
"OPF_WRITE_PROBLEM":"ON",
"OPF_WRITE_SOL_BAS":"ON",
"OPF_WRITE_SOL_ITG":"ON",
"OPF_WRITE_SOL_ITR":"ON",
"OPF_WRITE_SOLUTIONS":"OFF",
"OPTIMIZER":"OPTIMIZER_FREE",
"PARAM_READ_CASE_NAME":"ON",
"PARAM_READ_IGN_ERROR":"OFF",
"PRESOLVE_ELIMINATOR_MAX_FILL":-1,
"PRESOLVE_ELIMINATOR_MAX_NUM_TRIES":-1,
"PRESOLVE_LEVEL":-1,
"PRESOLVE_LINDEP_ABS_WORK_TRH":100,
"PRESOLVE_LINDEP_REL_WORK_TRH":100,
"PRESOLVE_LINDEP_USE":"ON",
"PRESOLVE_MAX_NUM_REDUCTIONS":-1,
"PRESOLVE_USE":"PRESOLVE_MODE_FREE",
"PRIMAL_REPAIR_OPTIMIZER":"OPTIMIZER_FREE",
"QO_SEPARABLE_REFORMULATION":"OFF",
"READ_DATA_COMPRESSED":"COMPRESS_FREE",
"READ_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
"READ_DEBUG":"OFF",
"READ_KEEP_FREE_CON":"OFF",
"READ_LP_DROP_NEW_VARS_IN_BOU":"OFF",
"READ_LP_QUOTED_NAMES":"ON",
"READ_MPS_FORMAT":"MPS_FORMAT_FREE",
"READ_MPS_WIDTH":1024,
"READ_TASK_IGNORE_PARAM":"OFF",

```

```

"SENSITIVITY_ALL": "OFF",
"SENSITIVITY_OPTIMIZER": "OPTIMIZER_FREE_SIMPLEX",
"SENSITIVITY_TYPE": "SENSITIVITY_TYPE_BASIS",
"SIM_BASIS_FACTOR_USE": "ON",
"SIM_DEGEN": "SIM_DEGEN_FREE",
"SIM_DUAL_CRASH": 90,
"SIM_DUAL_PHASEONE_METHOD": 0,
"SIM_DUAL_RESTRICT_SELECTION": 50,
"SIM_DUAL_SELECTION": "SIM_SELECTION_FREE",
"SIM_EXPLOIT_DUPVEC": "SIM_EXPLOIT_DUPVEC_OFF",
"SIM_HOTSTART": "SIM_HOTSTART_FREE",
"SIM_HOTSTART_LU": "ON",
"SIM_INTEGER": 0,
"SIM_MAX_ITERATIONS": 10000000,
"SIM_MAX_NUM_SETBACKS": 250,
"SIM_NON_SINGULAR": "ON",
"SIM_PRIMAL_CRASH": 90,
"SIM_PRIMAL_PHASEONE_METHOD": 0,
"SIM_PRIMAL_RESTRICT_SELECTION": 50,
"SIM_PRIMAL_SELECTION": "SIM_SELECTION_FREE",
"SIM_REFACTOR_FREQ": 0,
"SIM_REFORMULATION": "SIM_REFORMULATION_OFF",
"SIM_SAVE_LU": "OFF",
"SIM_SCALING": "SCALING_FREE",
"SIM_SCALING_METHOD": "SCALING_METHOD_POW2",
"SIM_SOLVE_FORM": "SOLVE_FREE",
"SIM_STABILITY_PRIORITY": 50,
"SIM_SWITCH_OPTIMIZER": "OFF",
"SOL_FILTER_KEEP_BASIC": "OFF",
"SOL_FILTER_KEEP_RANGED": "OFF",
"SOL_READ_NAME_WIDTH": -1,
"SOL_READ_WIDTH": 1024,
"SOLUTION_CALLBACK": "OFF",
"TIMING_LEVEL": 1,
"WRITE_BAS_CONSTRAINTS": "ON",
"WRITE_BAS_HEAD": "ON",
"WRITE_BAS_VARIABLES": "ON",
"WRITE_DATA_COMPRESSED": 0,
"WRITE_DATA_FORMAT": "DATA_FORMAT_EXTENSION",
"WRITE_DATA_PARAM": "OFF",
"WRITE_FREE_CON": "OFF",
"WRITE_GENERIC_NAMES": "OFF",
"WRITE_GENERIC_NAMES_IO": 1,
"WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS": "OFF",
"WRITE_IGNORE_INCOMPATIBLE_ITEMS": "OFF",
"WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS": "OFF",
"WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS": "OFF",
"WRITE_INT_CONSTRAINTS": "ON",
"WRITE_INT_HEAD": "ON",
"WRITE_INT_VARIABLES": "ON",
"WRITE_LP_FULL_OBJ": "ON",
"WRITE_LP_LINE_WIDTH": 80,
"WRITE_LP_QUOTED_NAMES": "ON",
"WRITE_LP_STRICT_FORMAT": "OFF",
"WRITE_LP_TERMS_PER_LINE": 10,
"WRITE_MPS_FORMAT": "MPS_FORMAT_FREE",
"WRITE_MPS_INT": "ON",
"WRITE_PRECISION": 15,
"WRITE_SOL_BARVARIABLES": "ON",
"WRITE_SOL_CONSTRAINTS": "ON",
"WRITE_SOL_HEAD": "ON",
"WRITE_SOL_IGNORE_INVALID_NAMES": "OFF",
"WRITE_SOL_VARIABLES": "ON",

```

```

    "WRITE_TASK_INC_SOL": "ON",
    "WRITE_XML_MODE": "WRITE_XML_MODE_ROW"
},
"dparam": {
    "ANA_SOL_INFEAS_TOL": 1e-6,
    "BASIS_REL_TOL_S": 1e-12,
    "BASIS_TOL_S": 1e-6,
    "BASIS_TOL_X": 1e-6,
    "CHECK_CONVEXITY_REL_TOL": 1e-10,
    "DATA_TOL_AIJ": 1e-12,
    "DATA_TOL_AIJ_HUGE": 1e+20,
    "DATA_TOL_AIJ_LARGE": 1e+10,
    "DATA_TOL_BOUND_INF": 1e+16,
    "DATA_TOL_BOUND_WRN": 1e+8,
    "DATA_TOL_C_HUGE": 1e+16,
    "DATA_TOL_CJ_LARGE": 1e+8,
    "DATA_TOL_QIJ": 1e-16,
    "DATA_TOL_X": 1e-8,
    "FEASREPAIR_TOL": 1e-10,
    "INTPNT_CO_TOL_DFEAS": 1e-8,
    "INTPNT_CO_TOL_INFEAS": 1e-10,
    "INTPNT_CO_TOL_MU_RED": 1e-8,
    "INTPNT_CO_TOL_NEAR_REL": 1e+3,
    "INTPNT_CO_TOL_PFEAS": 1e-8,
    "INTPNT_CO_TOL_REL_GAP": 1e-7,
    "INTPNT_NL_MERIT_BAL": 1e-4,
    "INTPNT_NL_TOL_DFEAS": 1e-8,
    "INTPNT_NL_TOL_MU_RED": 1e-12,
    "INTPNT_NL_TOL_NEAR_REL": 1e+3,
    "INTPNT_NL_TOL_PFEAS": 1e-8,
    "INTPNT_NL_TOL_REL_GAP": 1e-6,
    "INTPNT_NL_TOL_REL_STEP": 9.95e-1,
    "INTPNT_QO_TOL_DFEAS": 1e-8,
    "INTPNT_QO_TOL_INFEAS": 1e-10,
    "INTPNT_QO_TOL_MU_RED": 1e-8,
    "INTPNT_QO_TOL_NEAR_REL": 1e+3,
    "INTPNT_QO_TOL_PFEAS": 1e-8,
    "INTPNT_QO_TOL_REL_GAP": 1e-8,
    "INTPNT_TOL_DFEAS": 1e-8,
    "INTPNT_TOL_DSAFE": 1e+0,
    "INTPNT_TOL_INFEAS": 1e-10,
    "INTPNT_TOL_MU_RED": 1e-16,
    "INTPNT_TOL_PATH": 1e-8,
    "INTPNT_TOL_PFEAS": 1e-8,
    "INTPNT_TOL_PSAFE": 1e+0,
    "INTPNT_TOL_REL_GAP": 1e-8,
    "INTPNT_TOL_REL_STEP": 9.999e-1,
    "INTPNT_TOL_STEP_SIZE": 1e-6,
    "LOWER_OBJ_CUT": -1e+30,
    "LOWER_OBJ_CUT_FINITE_TRH": -5e+29,
    "MIO_DISABLE_TERM_TIME": -1e+0,
    "MIO_MAX_TIME": -1e+0,
    "MIO_MAX_TIME_APRX_OPT": 6e+1,
    "MIO_NEAR_TOL_ABS_GAP": 0.0,
    "MIO_NEAR_TOL_REL_GAP": 1e-3,
    "MIO_REL_GAP_CONST": 1e-10,
    "MIO_TOL_ABS_GAP": 0.0,
    "MIO_TOL_ABS_RELAX_INT": 1e-5,
    "MIO_TOL_FEAS": 1e-6,
    "MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT": 0.0,
    "MIO_TOL_REL_GAP": 1e-4,
    "MIO_TOL_X": 1e-6,
    "OPTIMIZER_MAX_TIME": -1e+0,

```

```

        "PRESOLVE_TOL_ABS_LINDEP":1e-6,
        "PRESOLVE_TOL_AIJ":1e-12,
        "PRESOLVE_TOL_REL_LINDEP":1e-10,
        "PRESOLVE_TOL_S":1e-8,
        "PRESOLVE_TOL_X":1e-8,
        "QCQO_REFORMULATE_REL_DROP_TOL":1e-15,
        "SEMIDEFINITE_TOL_APPROX":1e-10,
        "SIM_LU_TOL_REL_PIV":1e-2,
        "SIMPLEX_ABS_TOL_PIV":1e-7,
        "UPPER_OBJ_CUT":1e+30,
        "UPPER_OBJ_CUT_FINITE_TRH":5e+29
    },
    "sparam":{
        "BAS_SOL_FILE_NAME":"",
        "DATA_FILE_NAME":"examples/tools/data/lo1.mps",
        "DEBUG_FILE_NAME":"",
        "INT_SOL_FILE_NAME":"",
        "ITR_SOL_FILE_NAME":"",
        "MIO_DEBUG_STRING":"",
        "PARAM_COMMENT_SIGN":"%%",
        "PARAM_READ_FILE_NAME":"",
        "PARAM_WRITE_FILE_NAME":"",
        "READ_MPS_BOU_NAME":"",
        "READ_MPS_OBJ_NAME":"",
        "READ_MPS_RAN_NAME":"",
        "READ_MPS_RHS_NAME":"",
        "SENSITIVITY_FILE_NAME":"",
        "SENSITIVITY_RES_FILE_NAME":"",
        "SOL_FILTER_XC_LOW":"",
        "SOL_FILTER_XC_UPR":"",
        "SOL_FILTER_XX_LOW":"",
        "SOL_FILTER_XX_UPR":"",
        "STAT_FILE_NAME":"",
        "STAT_KEY":"",
        "STAT_NAME":"",
        "WRITE_LP_GEN_VAR_NAME":"XMSKGEN"
    }
}
}

```

14.8 The Solution File Format

MOSEK provides several solution files depending on the problem type and the optimizer used:

- *basis solution file* (extension `.bas`) if the problem is optimized using the simplex optimizer or basis identification is performed,
- *interior solution file* (extension `.sol`) if a problem is optimized using the interior-point optimizer and no basis identification is required,
- *integer solution file* (extension `.int`) if the problem contains integer constrained variables.

All solution files have the format:

NAME	: <problem name>
PROBLEM STATUS	: <status of the problem>
SOLUTION STATUS	: <status of the solution>
OBJECTIVE NAME	: <name of the objective function>
PRIMAL OBJECTIVE	: <primal objective value corresponding to the solution>
DUAL OBJECTIVE	: <dual objective value corresponding to the solution>
CONSTRAINTS	

INDEX	NAME	AT	ACTIVITY	LOWER LIMIT	UPPER LIMIT	DUAL LOWER	DUAL UPPER
?	<name>	??	<a value>	<a value>	<a value>	<a value>	<a value>
VARIABLES							
INDEX	NAME	AT	ACTIVITY	LOWER LIMIT	UPPER LIMIT	DUAL LOWER	DUAL UPPER
↔DUAL							
?	<name>	??	<a value>	<a value>	<a value>	<a value>	<a value>

In the example the fields ? and <> will be filled with problem and solution specific information. As can be observed a solution report consists of three sections, i.e.

- **HEADER** In this section, first the name of the problem is listed and afterwards the problem and solution status are shown. Next the primal and dual objective values are displayed.
- **CONSTRAINTS** For each constraint i of the form

$$l_i^c \leq \sum_{j=1}^n a_{ij}x_j \leq u_i^c, \quad (14.10)$$

the following information is listed:

- **INDEX:** A sequential index assigned to the constraint by **MOSEK**
- **NAME:** The name of the constraint assigned by the user.
- **AT:** The status of the constraint. In Table 14.4 the possible values of the status keys and their interpretation are shown.

Table 14.4: Status keys.

Status key	Interpretation
UN	Unknown status
BS	Is basic
SB	Is superbasic
LL	Is at the lower limit (bound)
UL	Is at the upper limit (bound)
EQ	Lower limit is identical to upper limit
**	Is infeasible i.e. the lower limit is greater than the upper limit.

- **ACTIVITY:** the quantity $\sum_{j=1}^n a_{ij}x_j^*$, where x^* is the value of the primal solution.
- **LOWER LIMIT:** the quantity l_i^c (see (14.10).)
- **UPPER LIMIT:** the quantity u_i^c (see (14.10).)
- **DUAL LOWER:** the dual multiplier corresponding to the lower limit on the constraint.
- **DUAL UPPER:** the dual multiplier corresponding to the upper limit on the constraint.
- **VARIABLES** The last section of the solution report lists information about the variables. This information has a similar interpretation as for the constraints. However, the column with the header **CONIC DUAL** is included for problems having one or more conic constraints. This column shows the dual variables corresponding to the conic constraints.

Example: lo1.sol

In Listing 14.7 we show the solution file for the lo1.opf problem.

Listing 14.7: An example of .sol file.

NAME	:
PROBLEM STATUS	: PRIMAL_AND_DUAL_FEASIBLE
SOLUTION STATUS	: OPTIMAL
OBJECTIVE NAME	: obj


```

PRIMAL OBJECTIVE      : 8.33333333e+01
DUAL OBJECTIVE        : 8.33333332e+01

CONSTRAINTS
INDEX      NAME          AT ACTIVITY          LOWER LIMIT      UPPER LIMIT      U
↪DUAL LOWER          DUAL UPPER
0          c1            EQ 3.00000000000000e+01  3.00000000e+01   3.00000000e+01   -0.
↪00000000000000e+00  -2.49999999741654e+00
1          c2            SB 5.33333333049188e+01  1.50000000e+01   NONE              2.
↪09157603759397e-10  -0.00000000000000e+00
2          c3            UL 2.49999999842049e+01  NONE              2.50000000e+01   -0.
↪00000000000000e+00  -3.33333332895110e-01

VARIABLES
INDEX      NAME          AT ACTIVITY          LOWER LIMIT      UPPER LIMIT      U
↪DUAL LOWER          DUAL UPPER
0          x1            LL 1.67020427073508e-09  0.00000000e+00   NONE              -4.
↪49999999528055e+00  -0.00000000000000e+00
1          x2            LL 2.93510446280504e-09  0.00000000e+00   1.00000000e+01   -2.
↪16666666494916e+00  6.20863861687316e-10
2          x3            SB 1.49999999899425e+01  0.00000000e+00   NONE              -8.
↪79123177454657e-10  -0.00000000000000e+00
3          x4            SB 8.33333332273116e+00  0.00000000e+00   NONE              -1.
↪69795978899185e-09  -0.00000000000000e+00

```


LIST OF EXAMPLES

List of examples shipped in the distribution of Command Line Tools:

Table 15.1: List of distributed examples

File	Description
25fv47.mps	A large linear problem from the Netlib library
ampl1.res	Interfacing MOSEK from AMPL
ampl2.res	Interfacing MOSEK from AMPL
ampl3.res	Interfacing MOSEK from AMPL
cqo1.mps	A simple conic quadratic problem
dgo.f	Nonlinear part of a geometric optimization example <code>dgo.mps</code>
dgo.mps	Linear part of a geometric optimization example
diet.dat	Data for the diet example <code>diet.mod</code>
diet.mod	A diet balancing AMPL example
dinfeas.lp	A simple dual infeasible linear problem
expopt1.eo	Data file with an exponential optimization problem
feasrepair.lp	An example demonstrating repair of infeasible problems
infeas.lp	A simple primal infeasible problem
lo1.mps	A simple linear problem
qo1.mps	A simple quadratic problem
sensitivity.ssp	Sensitivity analysis specification for <code>transport.lp</code>
transport.lp	A linear problem in the sensitivity analysis example

Additional examples can be found on the **MOSEK** website and in other **MOSEK** publications.

INTERFACE CHANGES

The section show interface-specific changes to the **MOSEK** Command Line Tools in version 8. See the [release notes](#) for general changes and new features of the **MOSEK** Optimization Suite.

16.1 Compatibility

16.2 Parameters

Added

- *MSK_DPAR_DATA_SYM_MAT_TOL*
- *MSK_DPAR_DATA_SYM_MAT_TOL_HUGE*
- *MSK_DPAR_DATA_SYM_MAT_TOL_LARGE*
- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*
- *MSK_DPAR_SEMIDEFINITE_TOL_APPROX*
- *MSK_IPAR_INTPNT_MULTI_THREAD*
- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*
- *MSK_IPAR_LOG_ANA_PRO*
- *MSK_IPAR_MIO_CUT_CLIQUE*
- *MSK_IPAR_MIO_CUT_GMI*
- *MSK_IPAR_MIO_CUT_IMPLIED_BOUND*
- *MSK_IPAR_MIO_CUT_KNAPSACK_COVER*
- *MSK_IPAR_MIO_CUT_SELECTION_LEVEL*
- *MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE*
- *MSK_IPAR_MIO_ROOT_REPEAT PRESOLVE_LEVEL*
- *MSK_IPAR_MIO_VB_DETECTION_LEVEL*
- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL*

- *MSK_IPAR_REMOVE_UNUSED_SOLUTIONS*
- *MSK_IPAR_WRITE_LP_FULL_OBJ*
- *MSK_IPAR_WRITE_MPS_FORMAT*
- *MSK_SPAR_REMOTE_ACCESS_TOKEN*

Removed

- MSK_DPAR_FEASREPAIR_TOL
- MSK_DPAR_MIO_HEURISTIC_TIME
- MSK_DPAR_MIO_MAX_TIME_APRX_OPT
- MSK_DPAR_MIO_REL_ADD_CUT_LIMITED
- MSK_DPAR_MIO_TOL_MAX_CUT_FRAC_RHS
- MSK_DPAR_MIO_TOL_MIN_CUT_FRAC_RHS
- MSK_DPAR_MIO_TOL_REL_RELAX_INT
- MSK_DPAR_MIO_TOL_X
- MSK_DPAR_NONCONVEX_TOL_FEAS
- MSK_DPAR_NONCONVEX_TOL_OPT
- MSK_IPAR_ALLOC_ADD_QNZ
- MSK_IPAR_CONCURRENT_NUM_OPTIMIZERS
- MSK_IPAR_CONCURRENT_PRIORITY_DUAL_SIMPLEX
- MSK_IPAR_CONCURRENT_PRIORITY_FREE_SIMPLEX
- MSK_IPAR_CONCURRENT_PRIORITY_INTPNT
- MSK_IPAR_CONCURRENT_PRIORITY_PRIMAL_SIMPLEX
- MSK_IPAR_FEASREPAIR_OPTIMIZE
- MSK_IPAR_INTPNT_FACTOR_DEBUG_LVL
- MSK_IPAR_INTPNT_FACTOR_METHOD
- MSK_IPAR_LIC_TRH_EXPIRY_WRN
- MSK_IPAR_LOG_CONCURRENT
- MSK_IPAR_LOG_FACTOR
- MSK_IPAR_LOG_HEAD
- MSK_IPAR_LOG_NONCONVEX
- MSK_IPAR_LOG_OPTIMIZER
- MSK_IPAR_LOG_PARAM
- MSK_IPAR_LOG_SIM_NETWORK_FREQ
- MSK_IPAR_MIO_BRANCH_PRIORITIES_USE
- MSK_IPAR_MIO_CONT_SOL
- MSK_IPAR_MIO_CUT_CG
- MSK_IPAR_MIO_CUT_LEVEL_ROOT
- MSK_IPAR_MIO_CUT_LEVEL_TREE
- MSK_IPAR_MIO_FEASPUMP_LEVEL

- MSK_IPAR_MIO_HOTSTART
- MSK_IPAR_MIO_KEEP_BASIS
- MSK_IPAR_MIO_LOCAL_BRANCH_NUMBER
- MSK_IPAR_MIO_OPTIMIZER_MODE
- MSK_IPAR_MIO_PRESOLVE_AGGREGATE
- MSK_IPAR_MIO_PRESOLVE_PROBING
- MSK_IPAR_MIO_PRESOLVE_USE
- MSK_IPAR_MIO_STRONG_BRANCH
- MSK_IPAR_MIO_USE_MULTITHREADED_OPTIMIZER
- MSK_IPAR_NONCONVEX_MAX_ITERATIONS
- MSK_IPAR_PRESOLVE_ELIM_FILL
- MSK_IPAR_PRESOLVE_ELIMINATOR_USE
- MSK_IPAR_QO_SEPARABLE_REFORMULATION
- MSK_IPAR_READ_ANZ
- MSK_IPAR_READ_CON
- MSK_IPAR_READ_CONE
- MSK_IPAR_READ_MPS_KEEP_INT
- MSK_IPAR_READ_MPS_OBJ_SENSE
- MSK_IPAR_READ_MPS_RELAX
- MSK_IPAR_READ_QNZ
- MSK_IPAR_READ_VAR
- MSK_IPAR_SIM_INTEGER
- MSK_IPAR_WARNING_LEVEL
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS
- MSK_SPAR_FEASREPAIR_NAME_PREFIX
- MSK_SPAR_FEASREPAIR_NAME_SEPARATOR
- MSK_SPAR_FEASREPAIR_NAME_WSUMVIOL

16.3 Constants

Added

- *MSK_BRANCH_DIR_FAR*
- *MSK_BRANCH_DIR_GUIDED*
- *MSK_BRANCH_DIR_NEAR*
- *MSK_BRANCH_DIR_PSEUDOCOST*
- *MSK_BRANCH_DIR_ROOT_LP*

- *MSK_CALLBACK_BEGIN_ROOT_CUTGEN*
- *MSK_CALLBACK_BEGIN_TO_CONIC*
- *MSK_CALLBACK_END_ROOT_CUTGEN*
- *MSK_CALLBACK_END_TO_CONIC*
- *MSK_CALLBACK_IM_ROOT_CUTGEN*
- *MSK_CALLBACK_SOLVING_REMOTE*
- *MSK_DATA_FORMAT_JSON_TASK*
- *MSK_DINF_MIO_CLIQUE_SEPARATION_TIME*
- *MSK_DINF_MIO_CMIR_SEPARATION_TIME*
- *MSK_DINF_MIO_GMI_SEPARATION_TIME*
- *MSK_DINF_MIO_IMPLIED_BOUND_TIME*
- *MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME*
- *MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION*
- *MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING*
- *MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING*
- *MSK_DINF_SOL_BAS_NRM_BARX*
- *MSK_DINF_SOL_BAS_NRM_SLC*
- *MSK_DINF_SOL_BAS_NRM_SLX*
- *MSK_DINF_SOL_BAS_NRM_SUC*
- *MSK_DINF_SOL_BAS_NRM_SUX*
- *MSK_DINF_SOL_BAS_NRM_XC*
- *MSK_DINF_SOL_BAS_NRM_XX*
- *MSK_DINF_SOL_BAS_NRM_Y*
- *MSK_DINF_SOL_ITG_NRM_BARX*
- *MSK_DINF_SOL_ITG_NRM_XC*
- *MSK_DINF_SOL_ITG_NRM_XX*
- *MSK_DINF_SOL_ITR_NRM_BARS*
- *MSK_DINF_SOL_ITR_NRM_BARX*
- *MSK_DINF_SOL_ITR_NRM_SLC*
- *MSK_DINF_SOL_ITR_NRM_SLX*
- *MSK_DINF_SOL_ITR_NRM_SNX*
- *MSK_DINF_SOL_ITR_NRM_SUC*
- *MSK_DINF_SOL_ITR_NRM_SUX*
- *MSK_DINF_SOL_ITR_NRM_XC*
- *MSK_DINF_SOL_ITR_NRM_XX*
- *MSK_DINF_SOL_ITR_NRM_Y*
- *MSK_DINF_TO_CONIC_TIME*
- *MSK_IINF_MIO_ABSGAP_SATISFIED*
- *MSK_IINF_MIO_CLIQUE_TABLE_SIZE*

- *MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED*
- *MSK_IINF_MIO_NEAR_RELGAP_SATISFIED*
- *MSK_IINF_MIO_NODE_DEPTH*
- *MSK_IINF_MIO_NUM_CMIR_CUTS*
- *MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS*
- *MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS*
- *MSK_IINF_MIO_NUM_REPEATED_PRESOLVE*
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- *MSK_IINF_MIO_PRESOLVED_NUMCONT*
- *MSK_IINF_MIO_PRESOLVED_NUMINT*
- *MSK_IINF_MIO_PRESOLVED_NUMVAR*
- *MSK_IINF_MIO_RELGAP_SATISFIED*
- *MSK_LIINF_MIO_PRESOLVED_ANZ*
- *MSK_LIINF_MIO_SIM_MAXITER_SETBACKS*
- *MSK_MPS_FORMAT_CPLEX*
- *MSK_SOL_STA_DUAL_ILLPOSED_CER*
- *MSK_SOL_STA_PRIM_ILLPOSED_CER*

Changed

- *MSK_SOL_STA_INTEGER_OPTIMAL*
- *MSK_SOL_STA_NEAR_DUAL_FEAS*
- *MSK_SOL_STA_NEAR_DUAL_INFEAS_CER*
- *MSK_SOL_STA_NEAR_INTEGER_OPTIMAL*
- *MSK_SOL_STA_NEAR_OPTIMAL*
- *MSK_SOL_STA_NEAR_PRIM_AND_DUAL_FEAS*
- *MSK_SOL_STA_NEAR_PRIM_FEAS*
- *MSK_SOL_STA_NEAR_PRIM_INFEAS_CER*
- *MSK_LICENSE_BUFFER_LENGTH*

Removed

- *MSK_CALLBACKCODE_BEGIN_CONCURRENT*
- *MSK_CALLBACKCODE_BEGIN_NETWORK_DUAL_SIMPLEX*
- *MSK_CALLBACKCODE_BEGIN_NETWORK_PRIMAL_SIMPLEX*
- *MSK_CALLBACKCODE_BEGIN_NETWORK_SIMPLEX*
- *MSK_CALLBACKCODE_BEGIN_NONCONVEX*
- *MSK_CALLBACKCODE_BEGIN_PRIMAL_DUAL_SIMPLEX*
- *MSK_CALLBACKCODE_BEGIN_PRIMAL_DUAL_SIMPLEX_BI*

- MSK_CALLBACKCODE_BEGIN_SIMPLEX_NETWORK_DETECT
- MSK_CALLBACKCODE_END_CONCURRENT
- MSK_CALLBACKCODE_END_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_END_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_END_NETWORK_SIMPLEX
- MSK_CALLBACKCODE_END_NONCONVEX
- MSK_CALLBACKCODE_END_PRIMAL_DUAL_SIMPLEX
- MSK_CALLBACKCODE_END_PRIMAL_DUAL_SIMPLEX_BI
- MSK_CALLBACKCODE_END_SIMPLEX_NETWORK_DETECT
- MSK_CALLBACKCODE_IM_MIO_PRESOLVE
- MSK_CALLBACKCODE_IM_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_IM_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_IM_NONCONVEX
- MSK_CALLBACKCODE_IM_PRIMAL_DUAL_SIMPLEX
- MSK_CALLBACKCODE_NONCONVEX
- MSK_CALLBACKCODE_UPDATE_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_NONCONVEX
- MSK_CALLBACKCODE_UPDATE_PRIMAL_DUAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_PRIMAL_DUAL_SIMPLEX_BI
- MSK_DINFITEM_BI_CLEAN_PRIMAL_DUAL_TIME
- MSK_DINFITEM_CONCURRENT_TIME
- MSK_DINFITEM_MIO_CG_SEPERATION_TIME
- MSK_DINFITEM_MIO_CMIR_SEPERATION_TIME
- MSK_DINFITEM_SIM_NETWORK_DUAL_TIME
- MSK_DINFITEM_SIM_NETWORK_PRIMAL_TIME
- MSK_DINFITEM_SIM_NETWORK_TIME
- MSK_DINFITEM_SIM_PRIMAL_DUAL_TIME
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- MSK_FEATURE_PTOX
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- MSK_IINFITEM_MIO_NUM_CARDGUB_CUTS
- MSK_IINFITEM_MIO_NUM_COEF_REDC_CUTS
- MSK_IINFITEM_MIO_NUM_CONTRA_CUTS
- MSK_IINFITEM_MIO_NUM_DISAGG_CUTS
- MSK_IINFITEM_MIO_NUM_FLOW_COVER_CUTS
- MSK_IINFITEM_MIO_NUM_GCD_CUTS
- MSK_IINFITEM_MIO_NUM_GUB_COVER_CUTS

- MSK_IINFITEM_MIO_NUM_KNAPSUR_COVER_CUTS
- MSK_IINFITEM_MIO_NUM_LATTICE_CUTS
- MSK_IINFITEM_MIO_NUM_LIFT_CUTS
- MSK_IINFITEM_MIO_NUM_OBJ_CUTS
- MSK_IINFITEM_MIO_NUM_PLAN_LOC_CUTS
- MSK_IINFITEM_SIM_NETWORK_DUAL_DEG_ITER
- MSK_IINFITEM_SIM_NETWORK_DUAL_HOTSTART
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- MSK_IINFITEM_SOL_INT_SOLSTA
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- MSK_LIINFITEM_BI_CLEAN_PRIMAL_DUAL_SUB_ITER
- MSK_MIOMODE_LAZY
- MSK_OPTIMIZERTYPE_CONCURRENT
- MSK_OPTIMIZERTYPE_MIXED_INT_CONIC
- MSK_OPTIMIZERTYPE_NETWORK_PRIMAL_SIMPLEX
- MSK_OPTIMIZERTYPE_NONCONVEX
- MSK_OPTIMIZERTYPE_PRIMAL_DUAL_SIMPLEX

16.4 Response Codes

Added

- *MSK_RES_ERR_CBF_DUPLICATE_PSDVAR*

- *MSK_RES_ERR_CBF_INVALID_PSDVAR_DIMENSION*
- *MSK_RES_ERR_CBF_TOO_FEW_PSDVAR*
- *MSK_RES_ERR_DUPLICATE_AIJ*
- *MSK_RES_ERR_FINAL_SOLUTION*
- *MSK_RES_ERR_JSON_DATA*
- *MSK_RES_ERR_JSON_FORMAT*
- *MSK_RES_ERR_JSON_MISSING_DATA*
- *MSK_RES_ERR_JSON_NUMBER_OVERFLOW*
- *MSK_RES_ERR_JSON_STRING*
- *MSK_RES_ERR_JSON_SYNTAX*
- *MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX*
- *MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX*
- *MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE*
- *MSK_RES_ERR_MIXED_CONIC_AND_NL*
- *MSK_RES_ERR_SERVER_CONNECT*
- *MSK_RES_ERR_SERVER_PROTOCOL*
- *MSK_RES_ERR_SERVER_STATUS*
- *MSK_RES_ERR_SERVER_TOKEN*
- *MSK_RES_ERR_SYM_MAT_HUGE*
- *MSK_RES_ERR_SYM_MAT_INVALID*
- *MSK_RES_ERR_TASK_WRITE*
- *MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC*
- *MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD*
- *MSK_RES_ERR_TOCONIC_CONSTRAINT_FX*
- *MSK_RES_ERR_TOCONIC_CONSTRAINT_RA*
- *MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD*
- *MSK_RES_WRN_SYM_MAT_LARGE*

Removed

- *MSK_RES_ERR_AD_INVALID_OPERAND*
- *MSK_RES_ERR_AD_INVALID_OPERATOR*
- *MSK_RES_ERR_AD_MISSING_OPERAND*
- *MSK_RES_ERR_AD_MISSING_RETURN*
- *MSK_RES_ERR_CONCURRENT_OPTIMIZER*
- *MSK_RES_ERR_INV_CONIC_PROBLEM*
- *MSK_RES_ERR_INVALID_BRANCH_DIRECTION*
- *MSK_RES_ERR_INVALID_BRANCH_PRIORITY*
- *MSK_RES_ERR_INVALID_NETWORK_PROBLEM*
- *MSK_RES_ERR_MBT_INCOMPATIBLE*

- MSK_RES_ERR_MBT_INVALID
- MSK_RES_ERR_MIO_NOT_LOADED
- MSK_RES_ERR_MIXED_PROBLEM
- MSK_RES_ERR_NO_DUAL_INFO_FOR_ITG_SOL
- MSK_RES_ERR_ORD_INVALID
- MSK_RES_ERR_ORD_INVALID_BRANCH_DIR
- MSK_RES_ERR_TOCONIC_CONVERSION_FAIL
- MSK_RES_ERR_TOO_MANY_CONCURRENT_TASKS
- MSK_RES_WRN_TOO_MANY_THREADS_CONCURRENT

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